

AHEAD

**eROSITA - Science and Data Analysis School**

# eROSITA Optics

*Peter Friedrich, MPE*

*[pfriedrich@mpe.mpg.de](mailto:pfriedrich@mpe.mpg.de)*

# 1. Theoretical Aspects of X-ray Optics

## 1.1. The X-Ray Band in the Electromagnetic Spectrum

## 1.2. Reflectivity

- *Refraction Index, Grazing Angle, Photon Energy (Total External Reflection)*
- *Optical Constants (Material depending)*

## 2. Telescope Designs (for Grazing Incident Telescopes)

### 2.1. Grazing Incident Telescopes

- *Wolter Type Optics (I, II, III)*
- *Modified Wolter Optics*

### 2.2. Basic Telescope Parameters

- *Focal Length  $f$ , Diameter (Radius  $r$ ), Coating*

### 2.3. Design Options

- *Nesting of Mirror Shells*
- *Segmented Optics*
- *Multi-Optic Telescopes*

### 2.4. Characteristics of X-Ray Telescopes

- *Effective Collecting Area*
- *Angular Resolution (Point-Spread Function)*
- *Surface Roughness (Micro-Roughness)*
- *Field-of-View: Vignetting and Off-Axis Blurring*
- *Straylight: Single Reflections (and how to prevent them)*

### 3. X-Ray Mirror Technologies (for Grazing Incident Telescopes)

3.1. Zerodur and Quartz Mirrors

3.2. Nickel Replication (Electroforming)

- *Super-Polished Mandrels*

- *Coating*

- *Galvanic Nickel Electroforming*

3.3. Foil Telescopes and other Replication Techniques

3.4. Silicon Pore Optics

3.5. Slumped Glass

3.6. Polished Silicon Optics

## 4. Building an X-ray telescope at the example of eROSITA

### 4.1. eROSITA Optics Design

### 4.2. Development phase and Demonstrator Model

- *Mandrel polishing and refurbishment*
- *Galvanic Nickel Electroforming (based on XMM experience)*
- *Vertical optical bench for mirror shell integration*
- *X-ray tests*

### 4.3. Mirror shell production and integration

### 4.4. X-ray baffle against straylight

### 4.5. Tests and Calibration

- *X-ray test facility*
- *Imaging performance (PSF)*
- *Effective collecting area*
- *Focal length measurements*

### 4.6. Telescope assembly

## 1.1. The X-Ray Band in the Electromagnetic Spectrum

## The X-Ray Band in the Electromagnetic Spectrum

# The Electromagnetic Spectrum

*low energy  
low frequency  
long wavelength*

*high energy  
high frequency  
short wavelength*

Radio

Infrared

Visual Light

Ultraviolet

X-ray

Gamma

$E = 2.5 \text{ eV}$   
 $\lambda = 500 \text{ nm}$

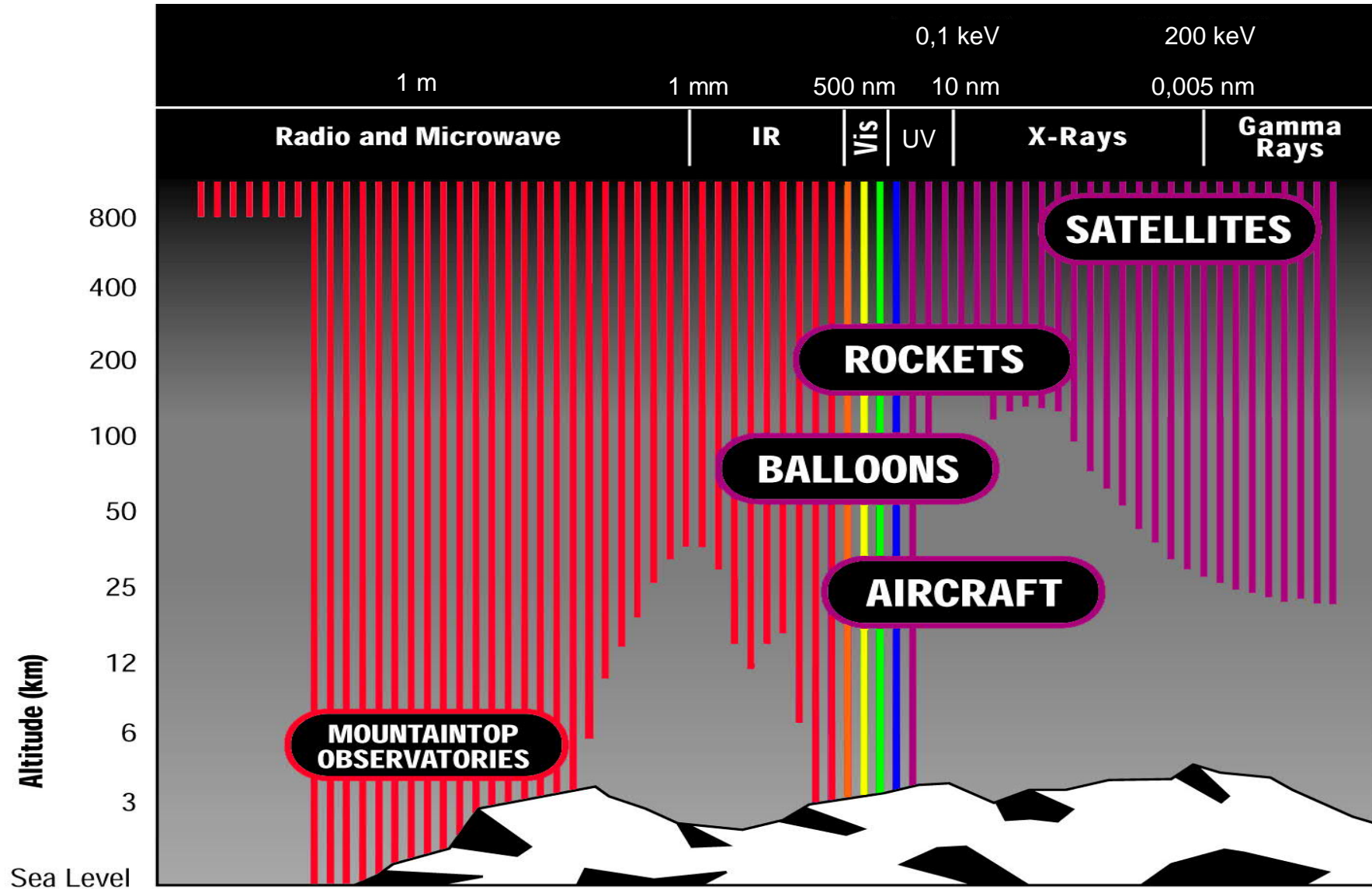
$E = 0.1 \dots 10 \text{ keV}$   
 $\lambda = 12 \dots 0.12 \text{ nm}$

„soft“ X-rays

$E = 10 \dots 100 \text{ keV}$   
 $\lambda < 0.12 \text{ nm}$

„hard“ X-rays

# Absorption in the Atmosphere

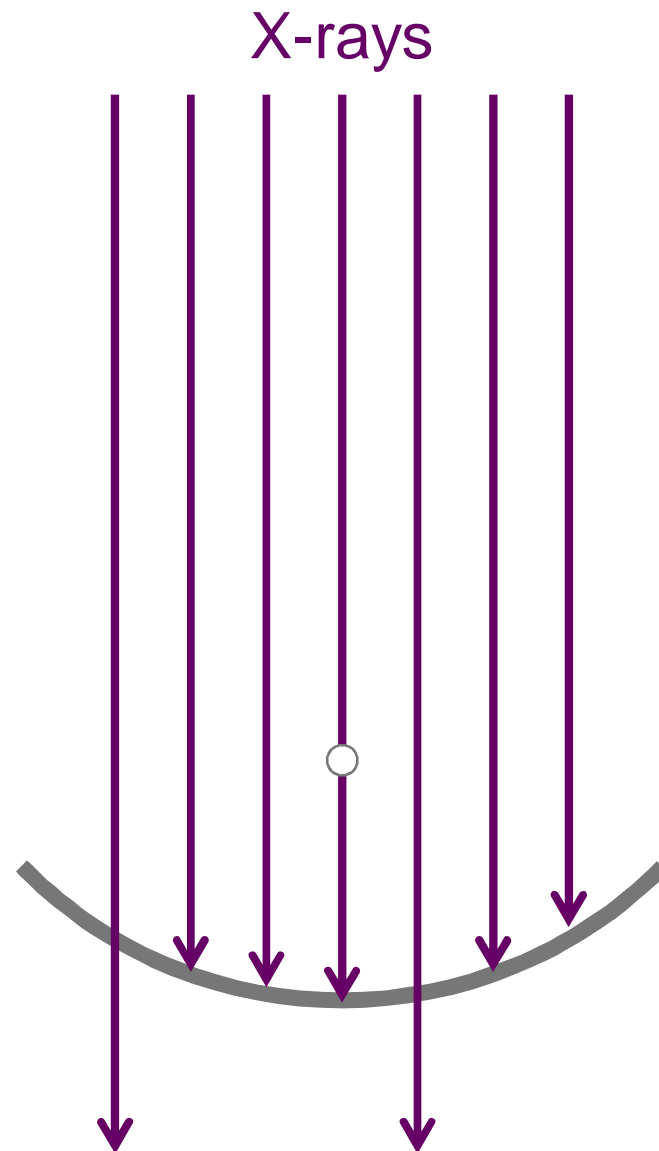
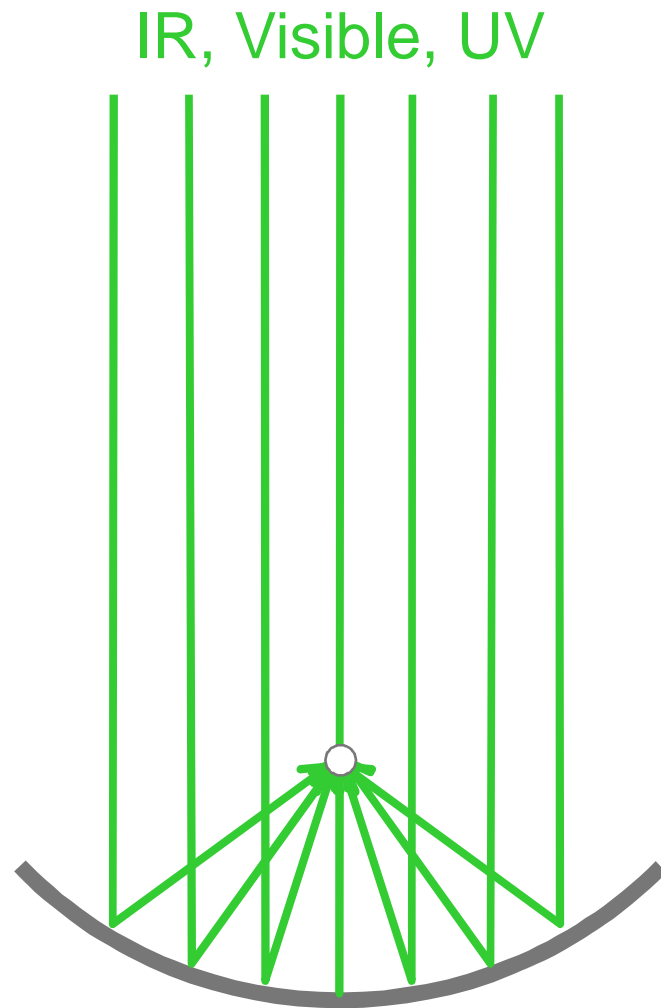




## 1.2. Reflectivity

- *Refraction Index, Grazing Angle, Photon Energy (Total External Reflection)*
- *Optical Constants (Material depending)*

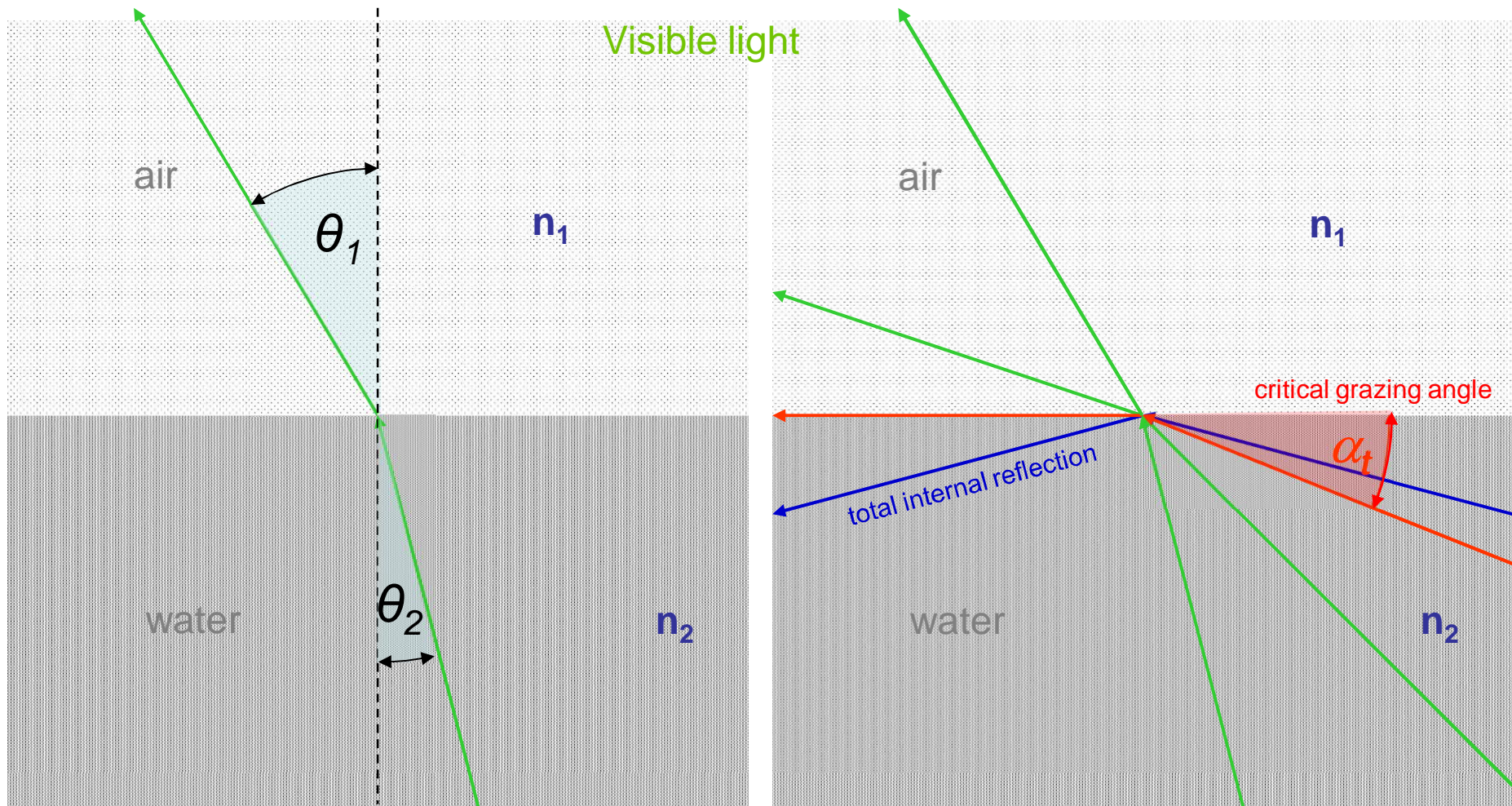
# Reflection and Absorption



## Index of Refraction and Total Internal Reflection

Snell's law:  $n_1 \sin \theta_1 = n_2 \sin \theta_2$

$\rightarrow \cos \alpha_t = n_1 / n_2$



## Index of Refraction and Grazing Angle

Complex refractive index  $n$ :

$$n = 1 - \underbrace{\delta}_{\text{phase change}} - i \underbrace{\beta}_{\text{absorption}}$$

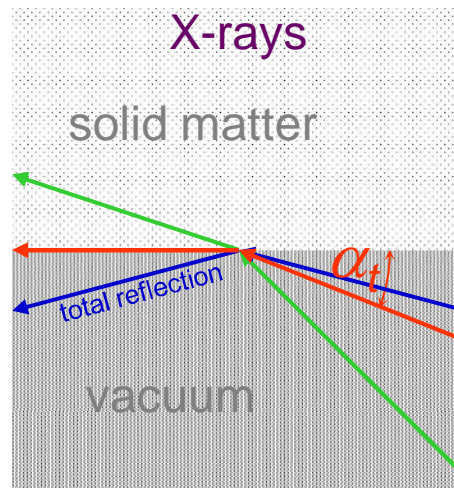
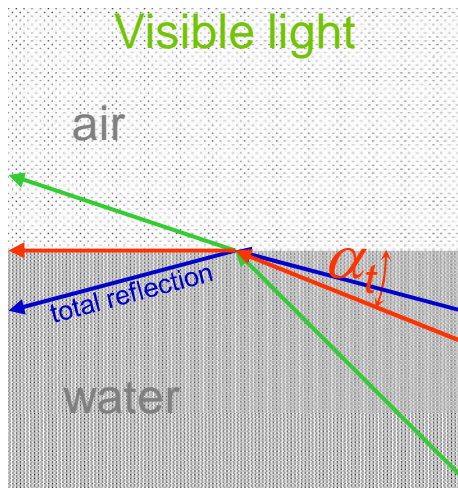
*slightly less than 1  
for X-rays in matter*

*exactly 1 in vacuum*

Critical grazing angle  $\alpha_t$ :

$$\cos \alpha_t = 1 - \delta \quad (\text{Snell's law})$$

$$\text{for } \delta \ll 1: \alpha_t = \sqrt{2\delta}$$



**from theoretical atomic physics:**

$$\delta \sim E^{-2} \quad \delta \sim Z$$

$$\rightarrow \alpha_t \sim E^{-1} \quad \alpha_t \sim \sqrt{Z}$$

**for practical use:**

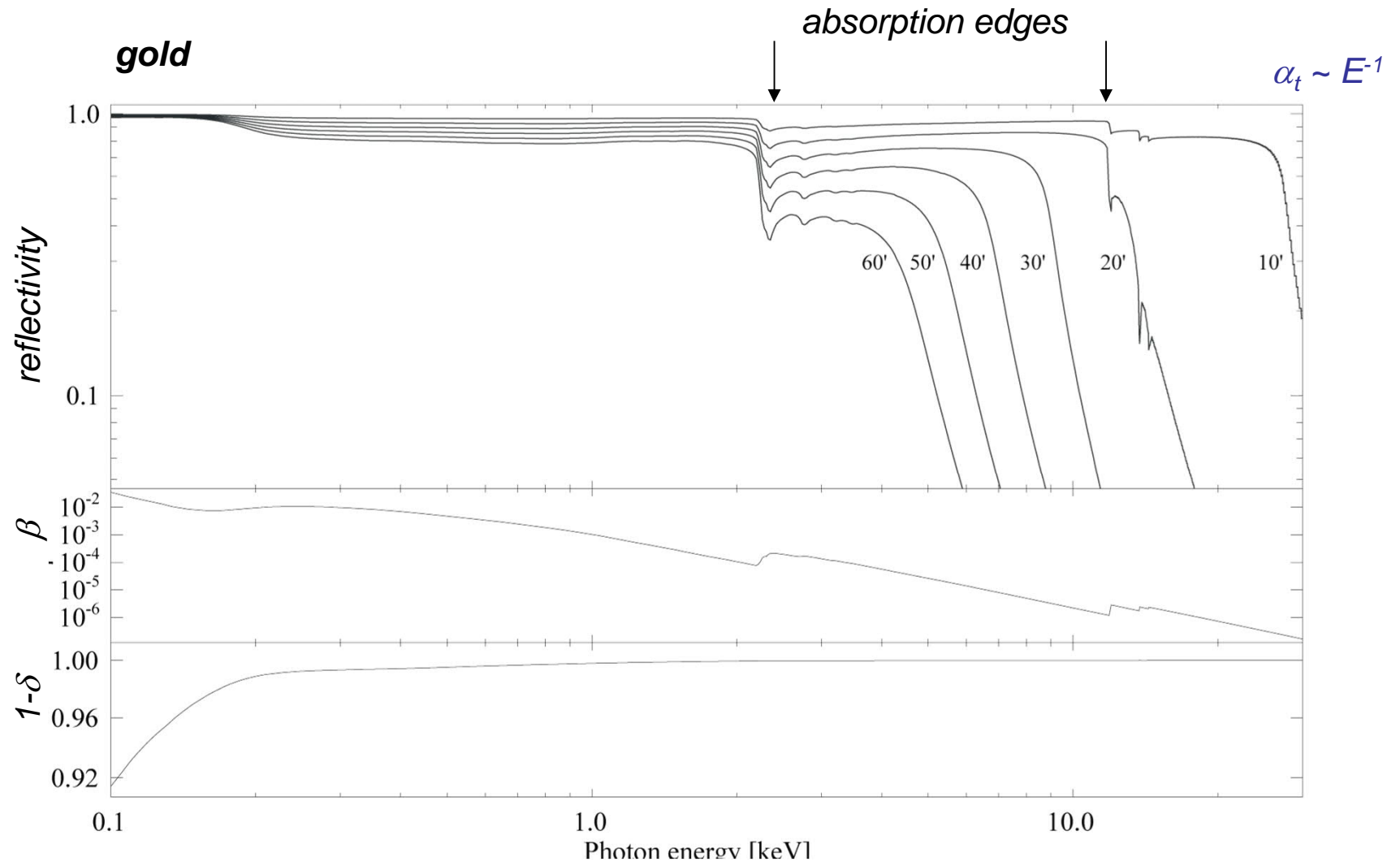
$$\alpha_t \approx 69 \sqrt{\rho} / E$$

$\alpha_t$  in arc minutes

$E$  in keV

$\rho$  in g/cm<sup>3</sup>

# Optical Constants

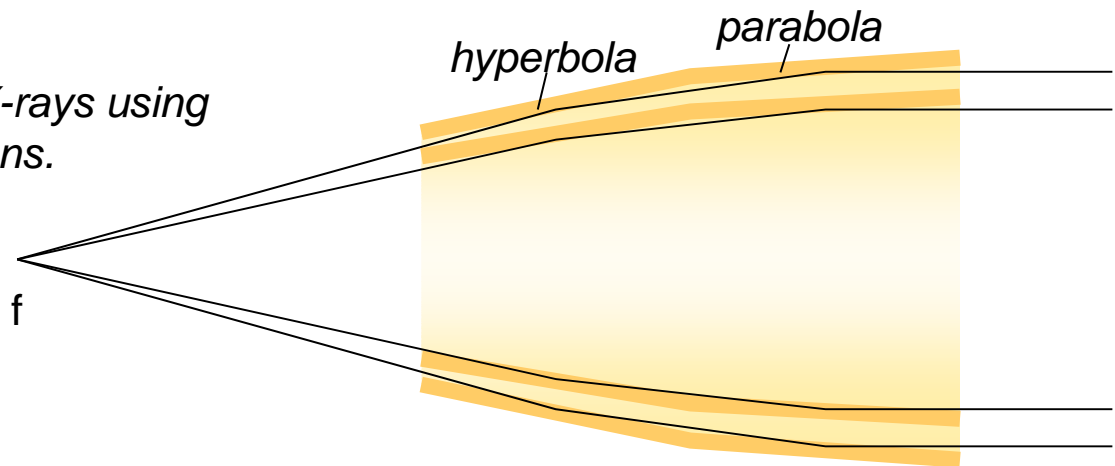


- 2.1. Grazing Incident Telescopes
- *Wolter Type Optics (I, II, III)*
  - *Modified Wolter Optics*

# Grazing Incidence Telescopes

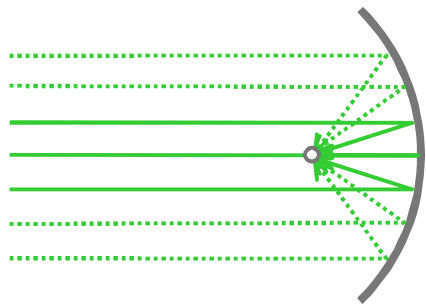
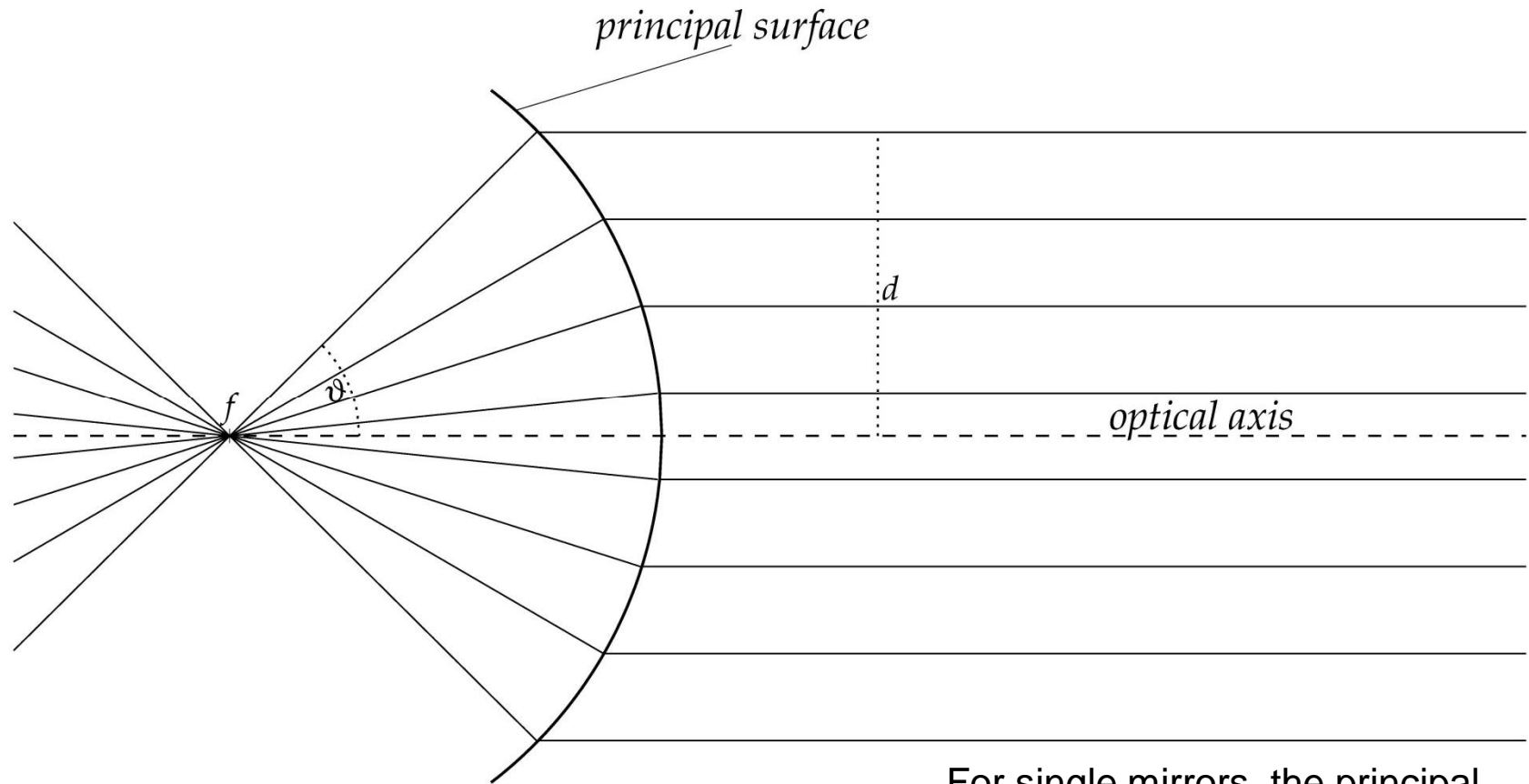


*Wolter telescopes focus X-rays using grazing incidence reflections.*



# Abbe's Sine Condition

$$d / \sin \vartheta = f$$



For single mirrors, the principal surface of is always identical to the mirror surface itself. That means that the sine condition is approximately satisfied only if the reflection is almost perpendicular to the mirror's surface.



Wolter's Publication in 1952 (Annalen der Physik)

***Spiegelsysteme streifenden Einfalls als abbildende Optiken  
für Röntgenstrahlen<sup>1)</sup>***

Von *Hans Wolter*

(Mit 19 Abbildungen)

**Inhaltsübersicht**

Als Optiken zur Röntgenstrahlmikroskopie eignen sich Systeme von total-reflektierenden Spiegeln, die bei Hebung der sphärischen Aberration für einen Achsenpunkt zugleich die Abbesche Sinusbedingung bis zu Aperturen 0,05 befriedigend erfüllen. Für die Lebenduntersuchung biologischer Objekte empfehlen sich Wellenlängen um 24 Å, die im Wasser wenig, aber in kohlenstoffhaltigen oder stickstoffhaltigen Stoffen stark absorbiert werden. Mit diesen weichen Strahlen ist eine Steigerung des Auflösungsvermögens gegenüber dem Lichtmikroskop um mindestens eine Größenordnung unter Verwendung der hier beschriebenen Optiken zu erwarten.

---

**1. Schwierigkeiten der Schattenmikroskopie**

Neben dem Elektronenmikroskop und dem Lichtmikroskop wünschen wir uns ein hochauflösendes Mikroskop für die Beobachtung lebender Objekte, also ein Mikroskop, das die Objekte unter Luftdruck mit einem — z. B. um eine oder mehrere Größenordnungen — gegenüber dem Lichtmikroskop gesteigerten Auflösungsvermögen beobachten läßt.

### 3. Annähernde Erfüllung der Abbesehen Sinusbedingung durch ein Zweispiegelsystem

Ein System aus 2 sich schneidenden Spiegelflächen hat eine Knickfläche, die so durch die Schnittkante der beiden Spiegel geht, wie Abb. 5 das andeutet. Um mit 2 Spiegeln bei streifendem Einfall alle achsenparallelen Strahlen in einem Punkt zu sammeln, verwenden wir ein Rotationsparaboloid (Abb. 6) und ein

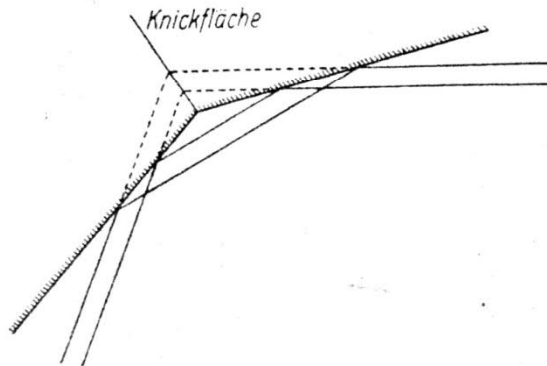


Abb. 5. Knickfläche bei zwei Spiegeln

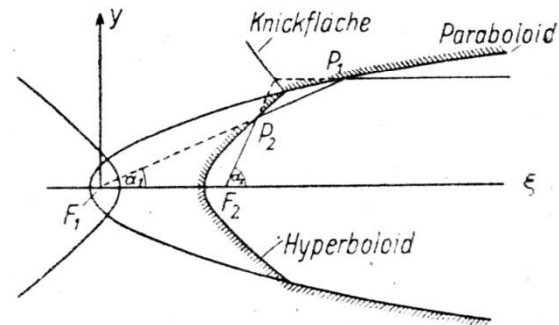


Abb. 6. Paraboloid und Hyperboloid in konfokaler Lage als Spiegelsystem für streifenden Einfall

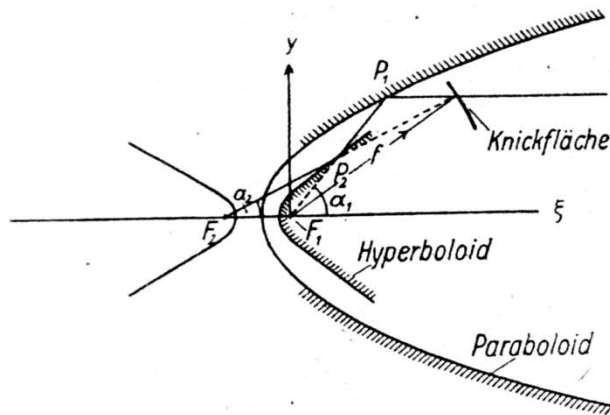


Abb. 15. Spiegelsystem 2. Art

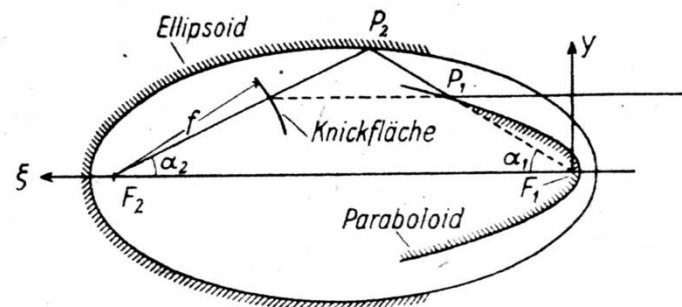
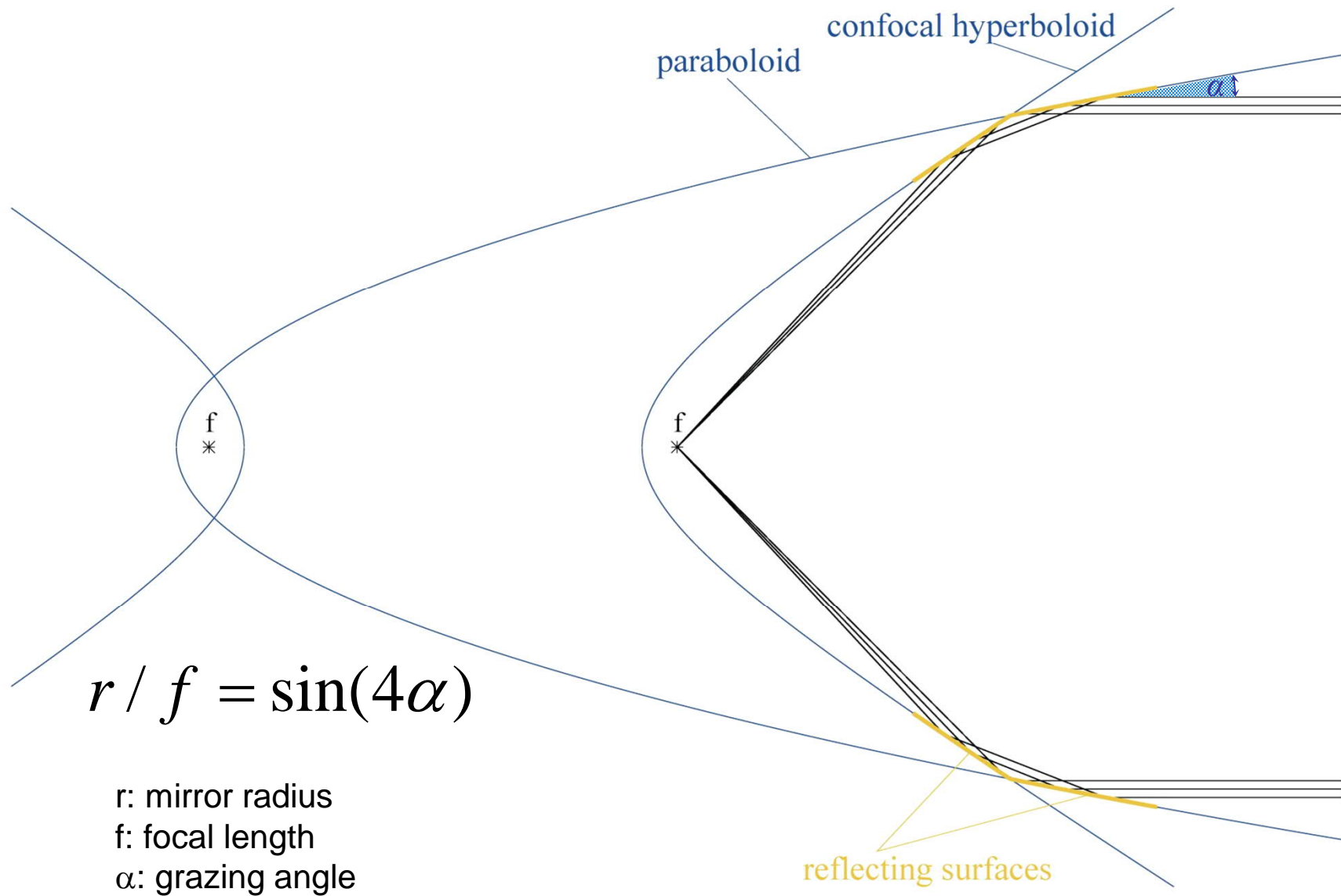


Abb. 16. Spiegelsystem 3. Art

# Wolter I Design



## Modified Wolter Optics: Wolter-Schwarzschild, Wide Field Imager

*Mathematical sequence to describe Wolter optics and modifications:*

*Equation for parabolic mirror:*

$$r_a^2 = r_0^2 \cdot \sum_{i=0}^1 a_i \cdot \left( \frac{x - x_0}{r_0} \right)^i \quad \text{with} \quad a_0 = 1, \quad a_1 = 2 \cdot \tan \alpha \quad \text{for Wolter optics}$$

*Equation for hyperbolic mirror:*

$$r_b^2 = r_0^2 \cdot \sum_{i=0}^2 b_i \cdot \left( \frac{x - x_0}{r_0} \right)^i \quad \text{with} \quad b_0 = 1, \quad b_1 = 2 \cdot \tan \beta, \quad b_2 = \frac{2 \cdot r_0 \cdot \tan \beta}{f + r_0 \cdot \cot(2 \cdot \alpha)} \quad \text{for Wolter optics}$$

*The Wolter systems satisfy Abbe's sine condition approximately only near the optical axis and near the intersection of the primary and secondary.*

*Modified equations were also developed which satisfy the Abbe sine condition strictly and hence exhibit no comatic aberration. These are called Wolter-Schwarzschild designs.*

*Other modifications are proposed in order to optimize the PSF over the field-of-view.*

2.2. Basic Telescope Parameters (for Wolter Telescopes)  
- Focal Length  $f$ , Diameter (Radius  $r$ ), Coating

$$r / f = \sin (4 \alpha)$$

or

$$\alpha = 0.25 \times \arcsin (r / f)$$

$$\alpha_t \approx 69 \sqrt{\rho} / E$$

$\alpha_t$  in arc minutes

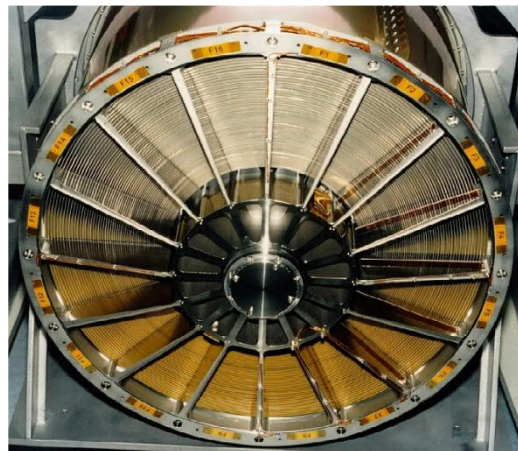
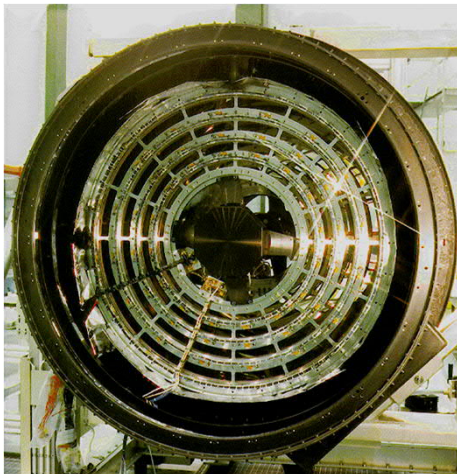
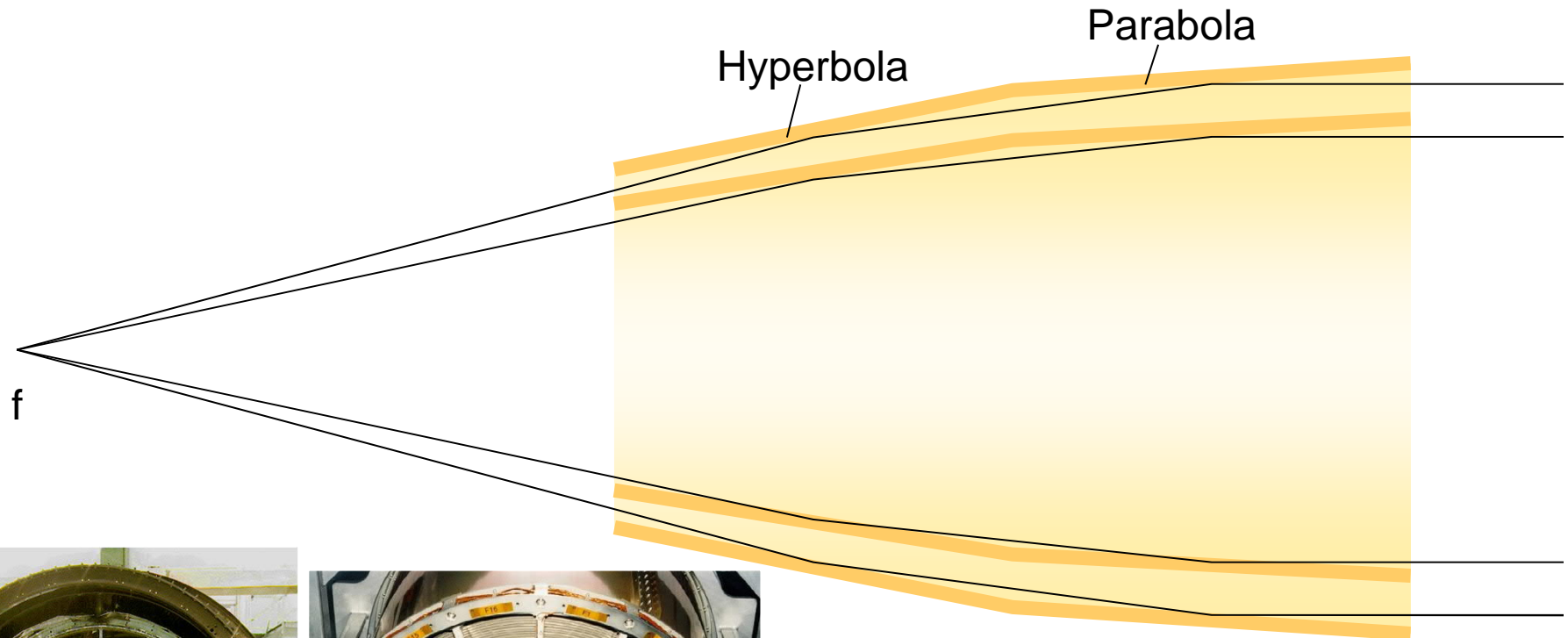
$E$  in keV

$\rho$  in  $\text{g/cm}^3$

## 2.3. Design Options

- *Nesting of Mirror Shells*
- *Segmented Optics*
- *Multi-Optic Telescopes*

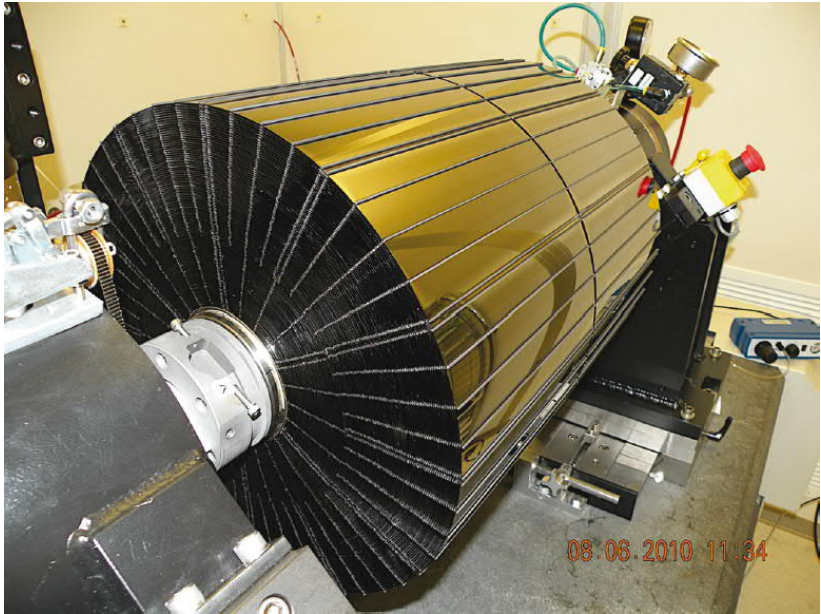
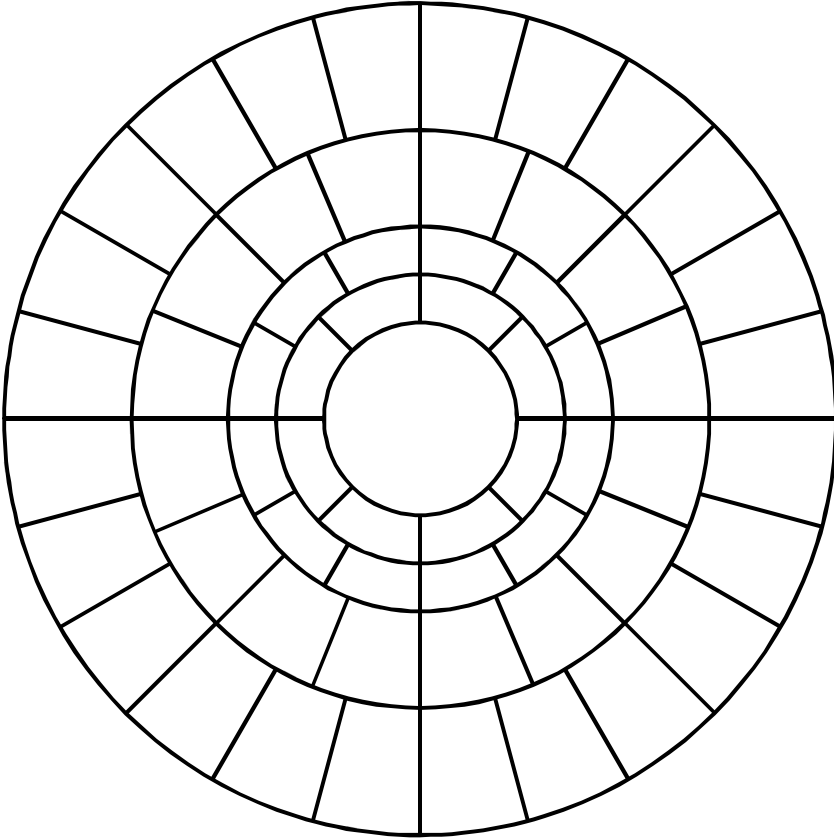
## Nesting of Wolter 1 Mirror Shells



$$a \approx 2\pi r \times l \sin \alpha$$

$a$ : projected area of one shell  
 $l$ : length of a mirror element  
 $\alpha$ : grazing angle

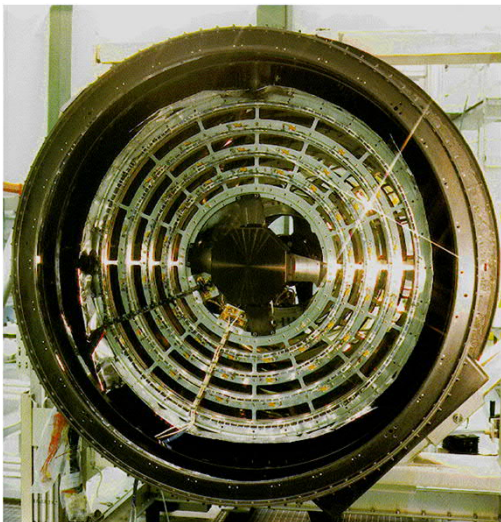
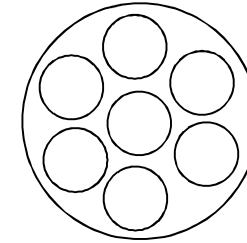
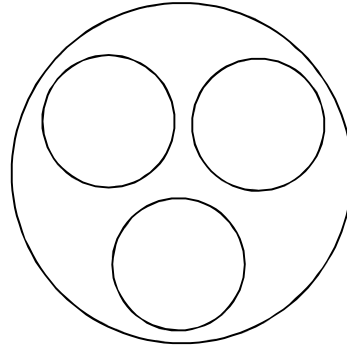
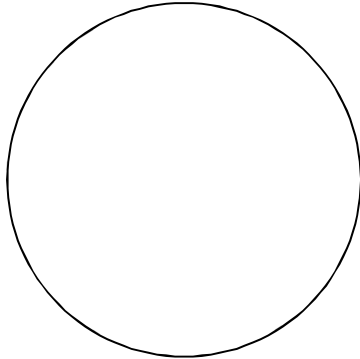
# Segmented Wolter Mirrors



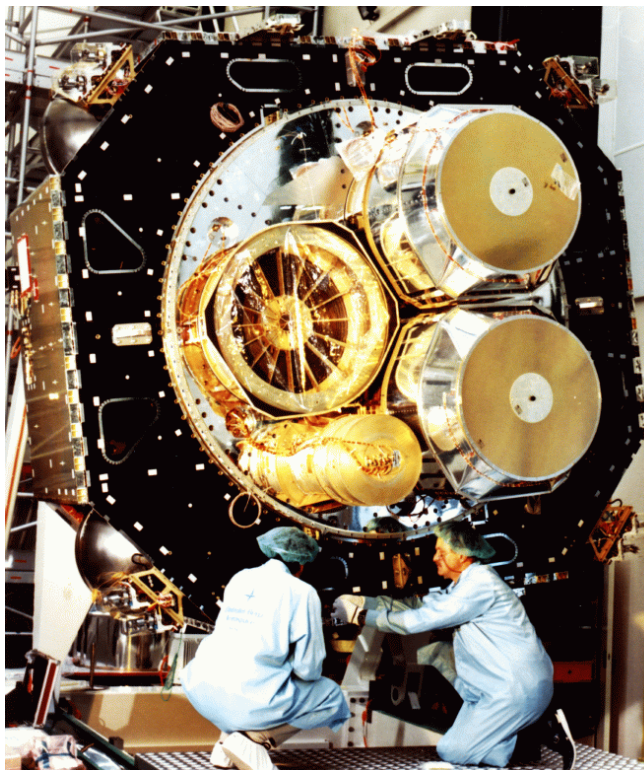
*Example: NuSTAR*



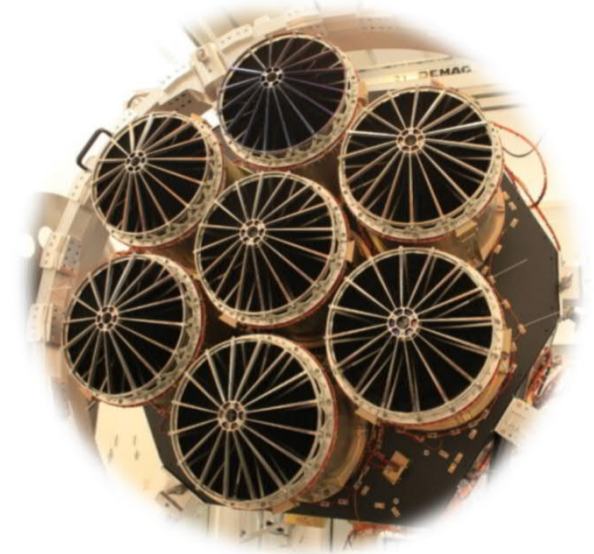
# Multi-Optic Telescopes



*Example: ROSAT*



*Example: XMM-Newton*

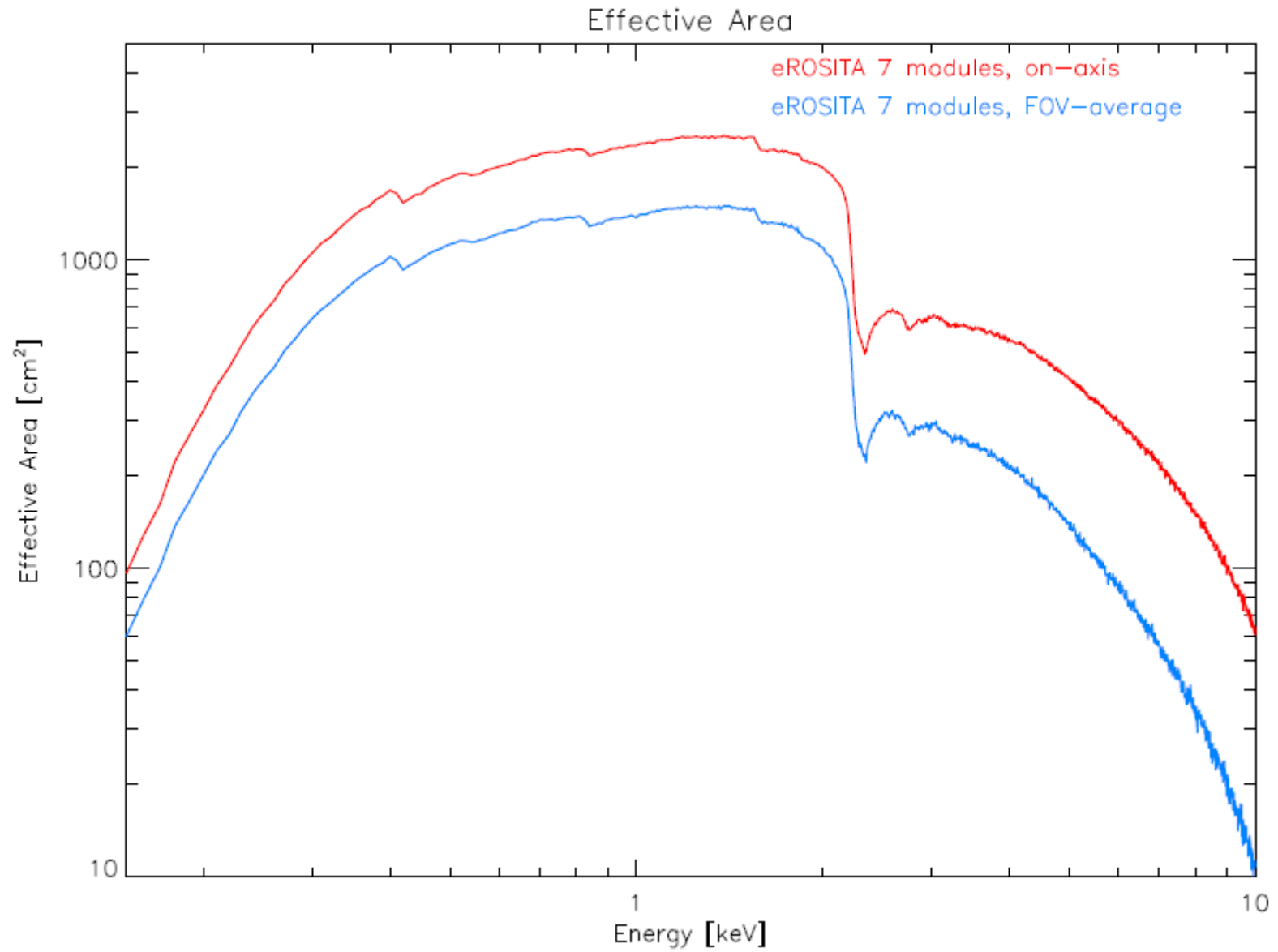


*Example: eROSITA*

## 2.4. Characteristics of X-Ray Telescopes

- *Effective Collecting Area*
- *Angular Resolution (Point-Spread Function)*
- *Surface Roughness (Micro-Roughness)*
- *Field-of-View: Vignetting and Off-Axis Blurring*
- *Straylight: Single Reflections (and how to prevent them)*

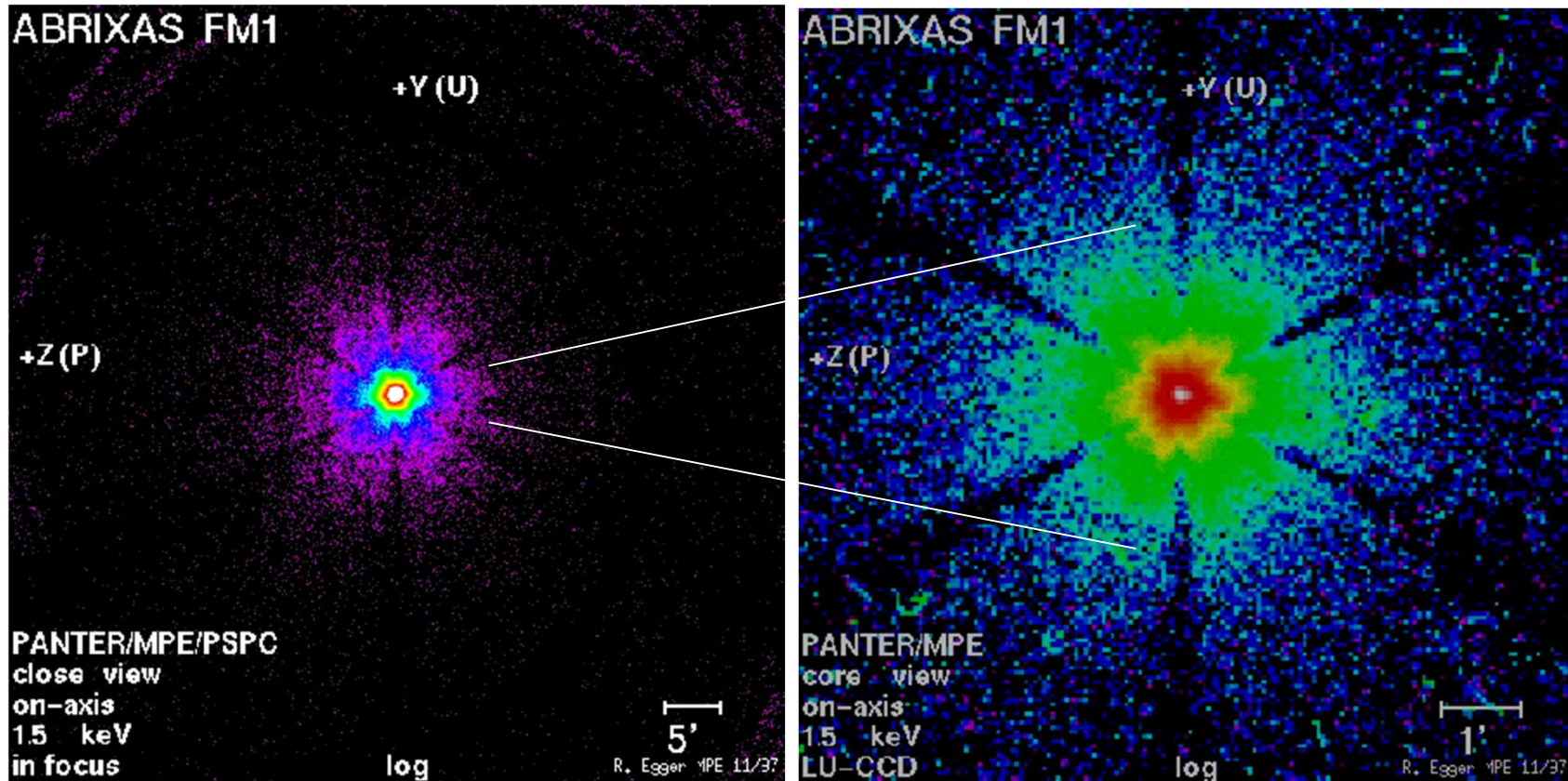
# Effective Area



# Point Spread Function (PSF)

**The wings of the PSF are due to**

- figure errors (lower spatial frequencies) → geometrical optics
- microroughness (higher spatial frequencies) → interference



## Surface Roughness (Micro-Roughness)

*A: Fractional energy in core:*

$$A = e^{-(2k\sigma \sin \alpha)^2}$$

*B: Total integrated scatter (TIS):*

$$B = 1 - A \rightarrow B = (2k\sigma \sin \alpha)^2 \quad \text{for small } B$$

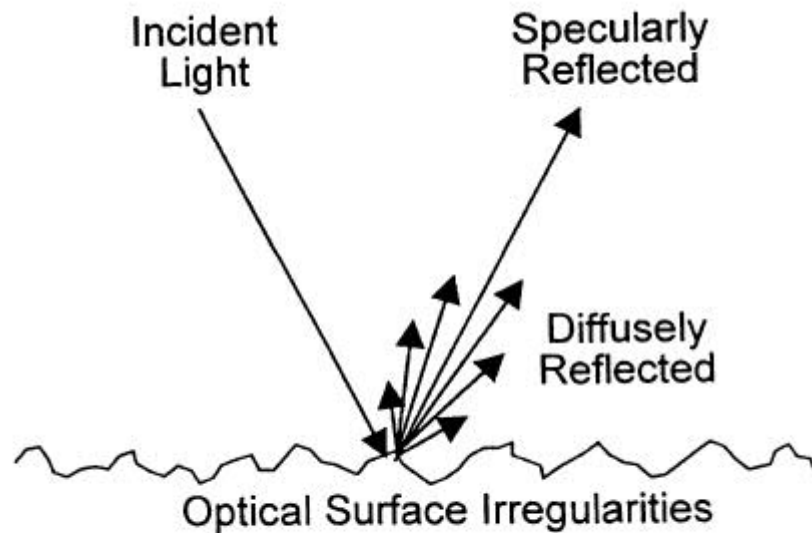


Figure 3. Optical surface irregularities result in both specularly reflected and diffusely reflected light.

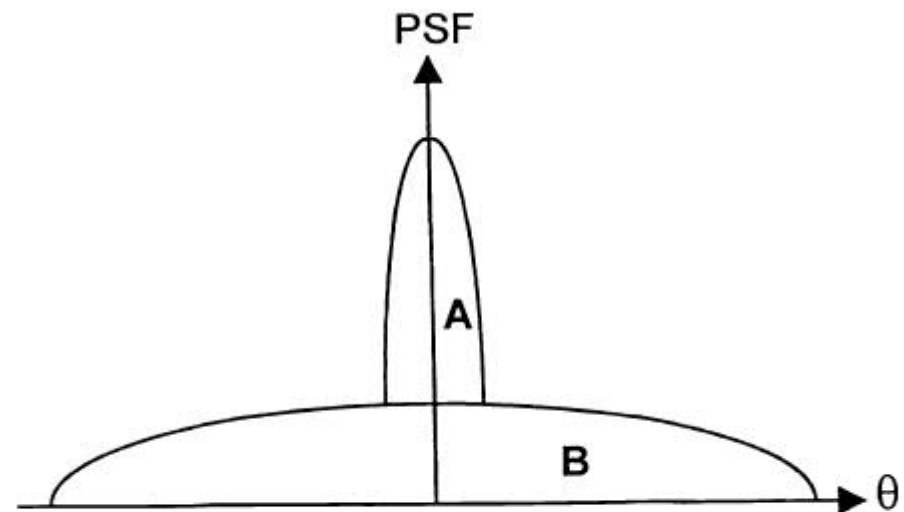
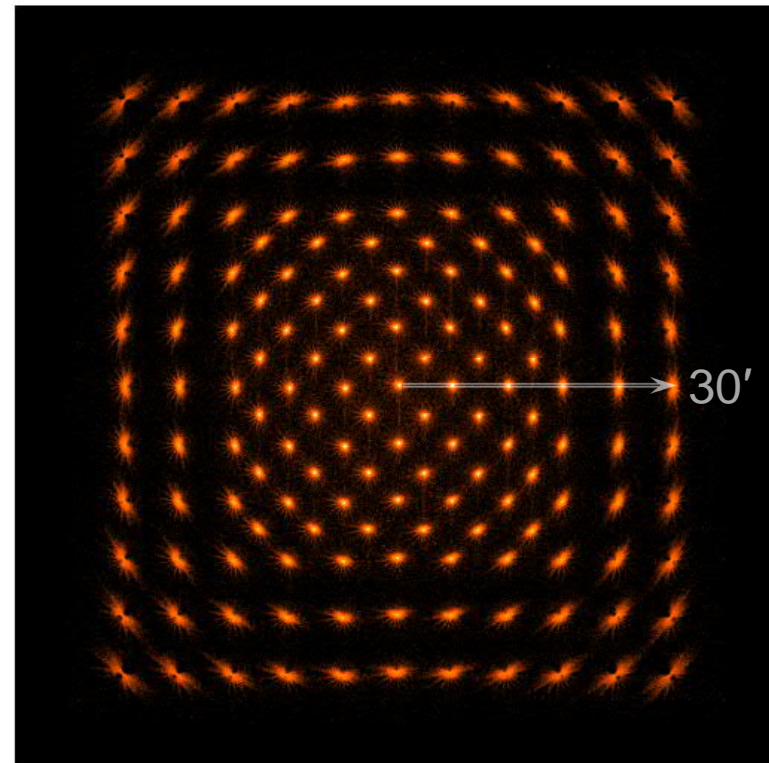
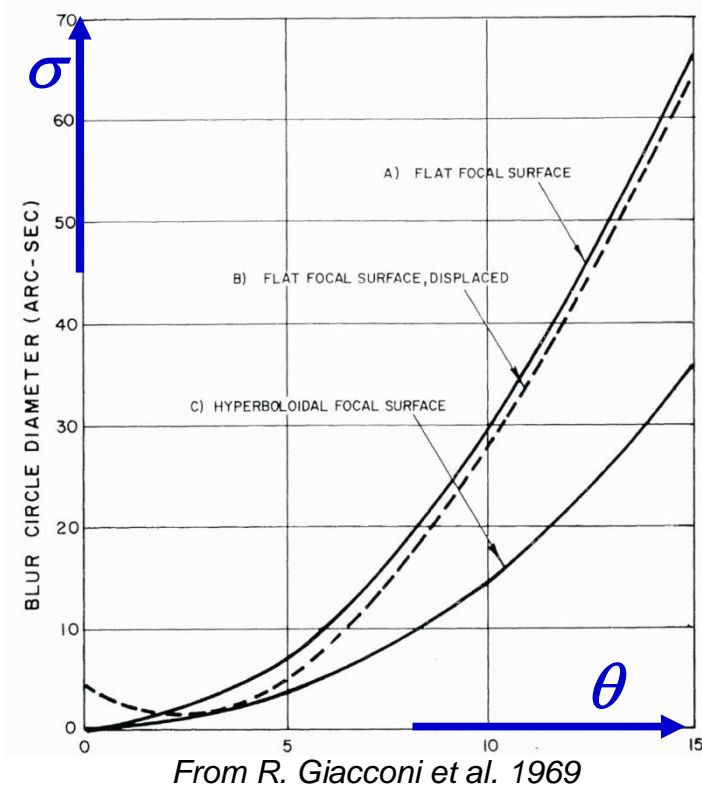
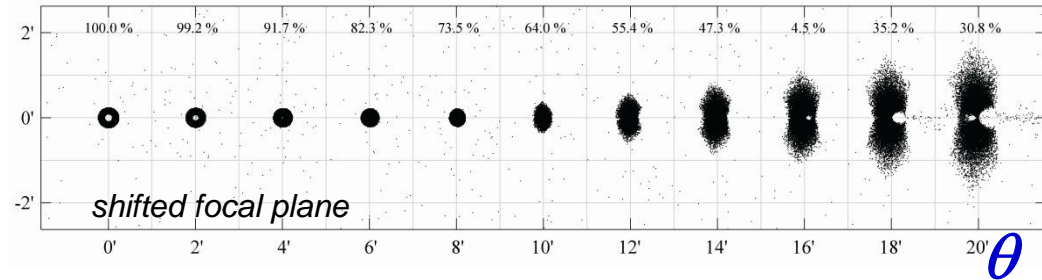
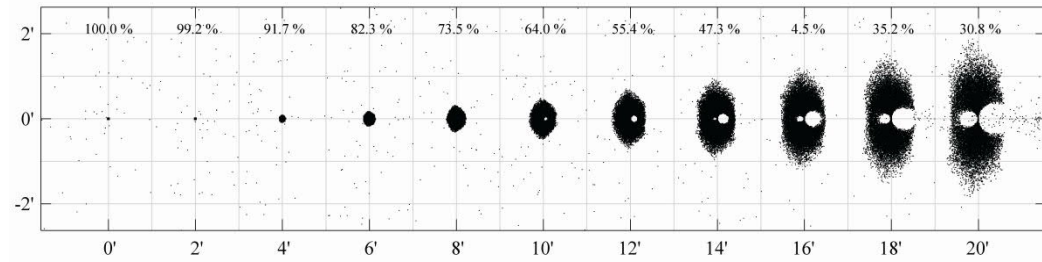


Figure 4. The image of a point source consists of a narrow image core surrounded by a scattered halo.

# Off-Axis Blurring and Vignetting

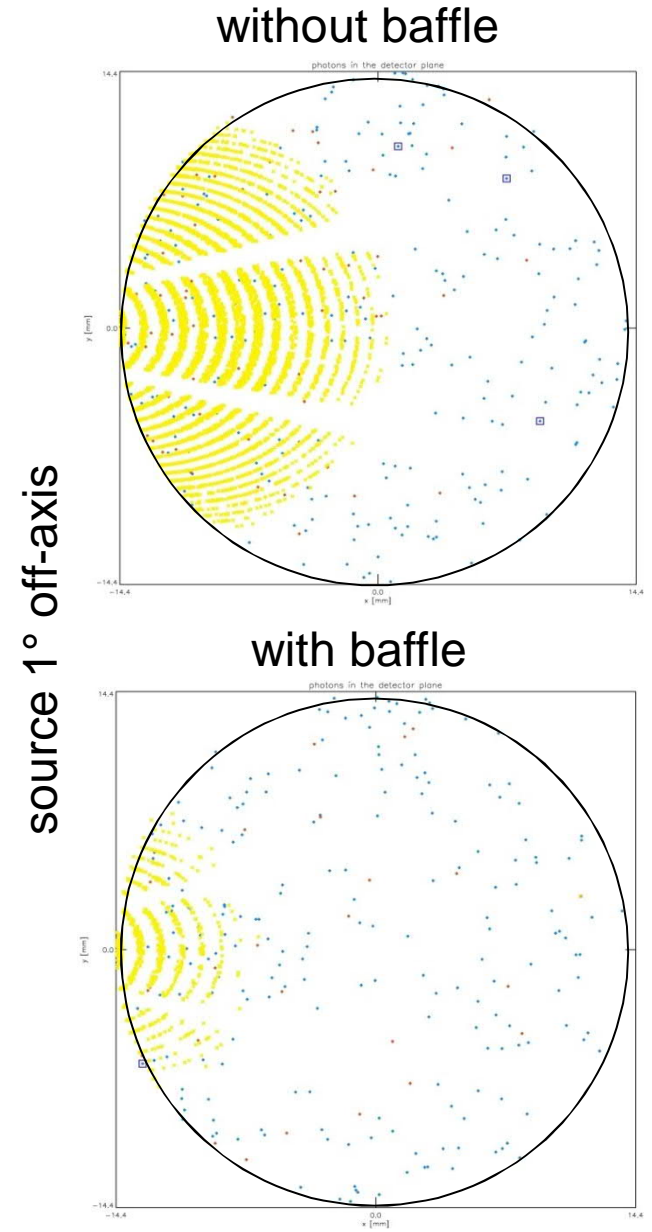
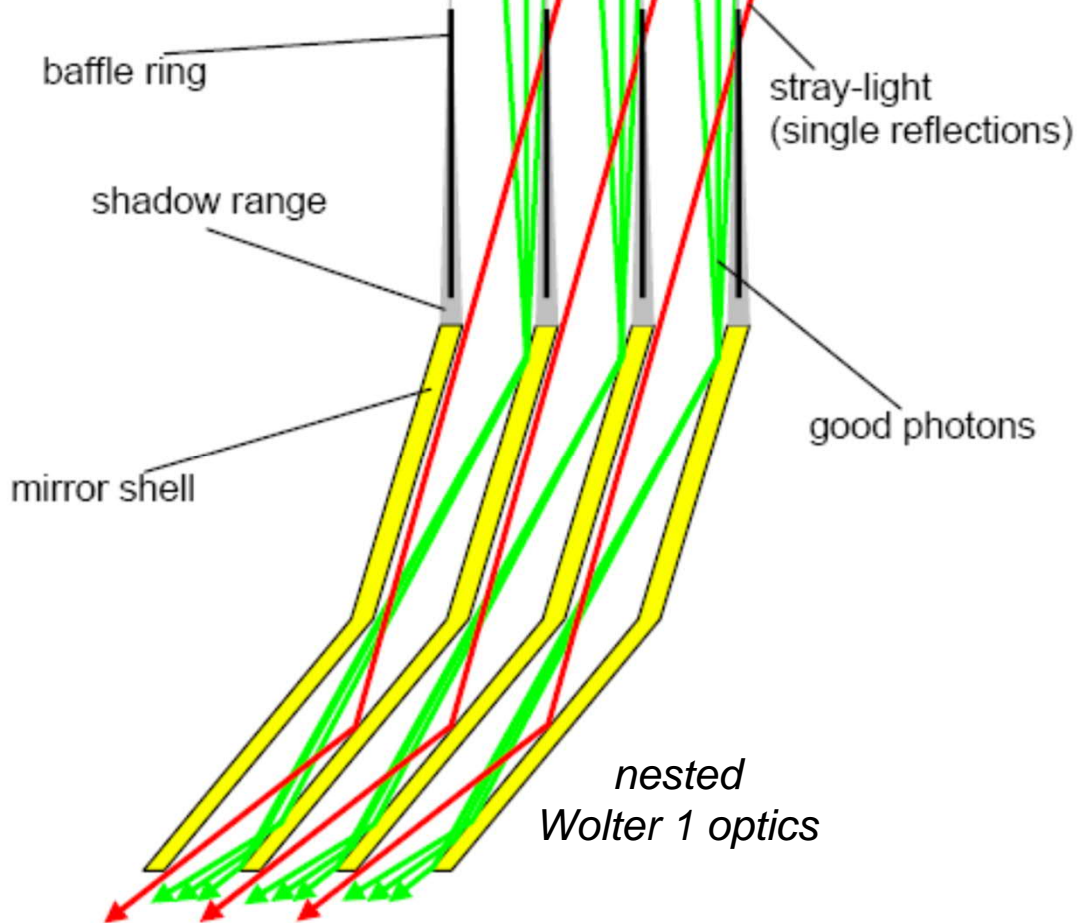
rms blur circle  $\sigma$ :

$$\sigma = 5 \times \frac{l}{f} \times \frac{\tan^2 \theta}{\tan \alpha} + 4 \tan \theta \tan^2 \alpha$$



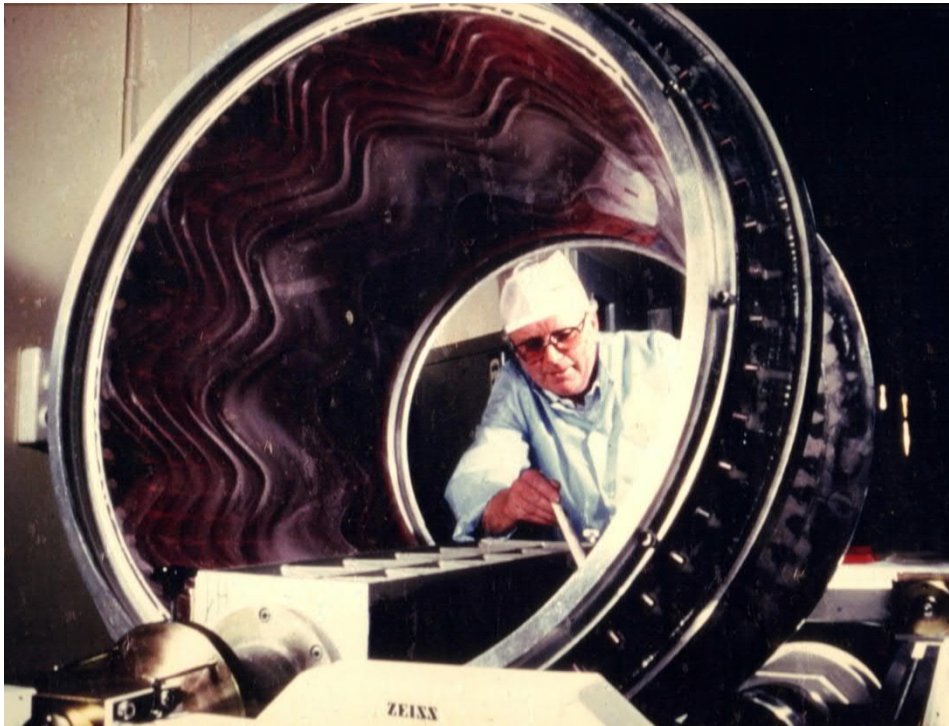
# Straylight: Single Reflections (and how to prevent them)

*X-ray baffle against straylight*

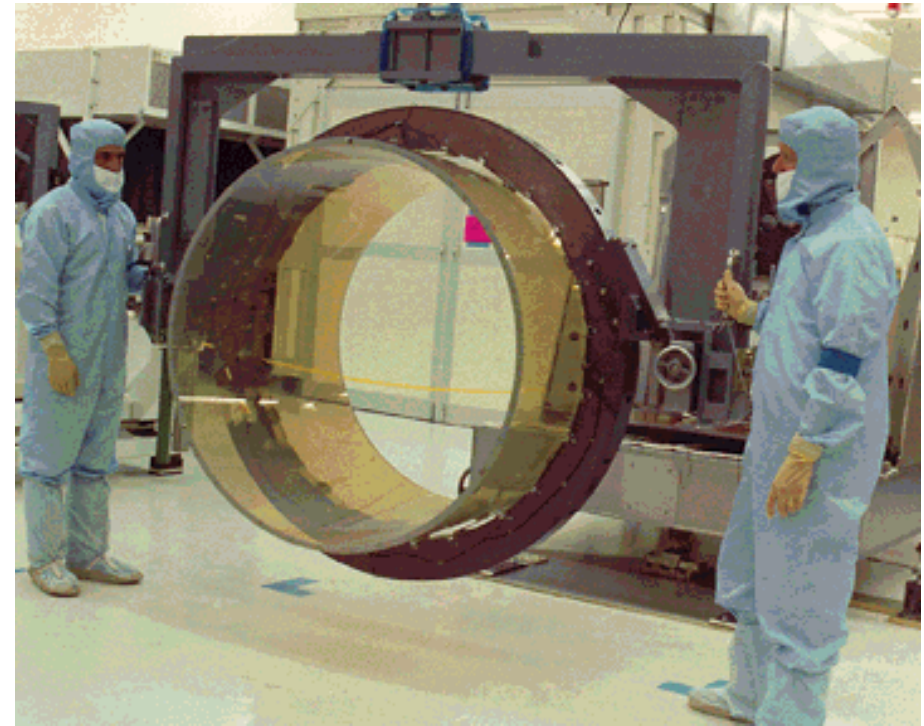


### 3.1. Zerodur and Quartz Mirrors

X-Ray Mirrors made of polished Zerodur: ROSAT and Chandra



ROSAT X-ray mirror (1 of 4)



Chandra X-ray mirror (1 of 4)



3.2. Nickel Replication (Electroforming)  
- *Super-Polished Mandrels*  
- *Coating*  
- *Galvanic Nickel Electroforming*



### 3.3. Foil Telescopes and other Replication Techniques

#### Segmented Foil Mirrors: Suzaku



*mandrels*

The Japanese X-ray satellite Suzaku and its precursors have telescopes made of aluminum foil segments which are replicated from glass mandrels using an epoxy layer in between.

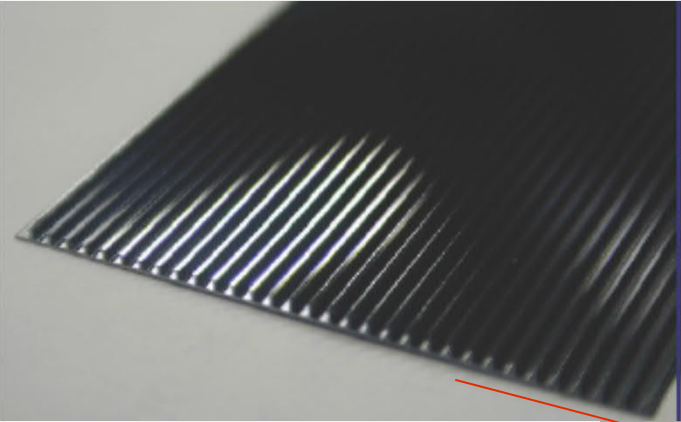
The coating is transferred from the mandrel to the foils.



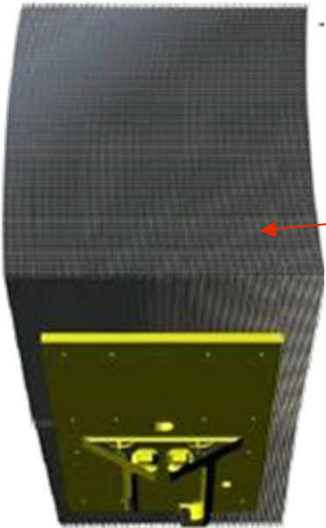
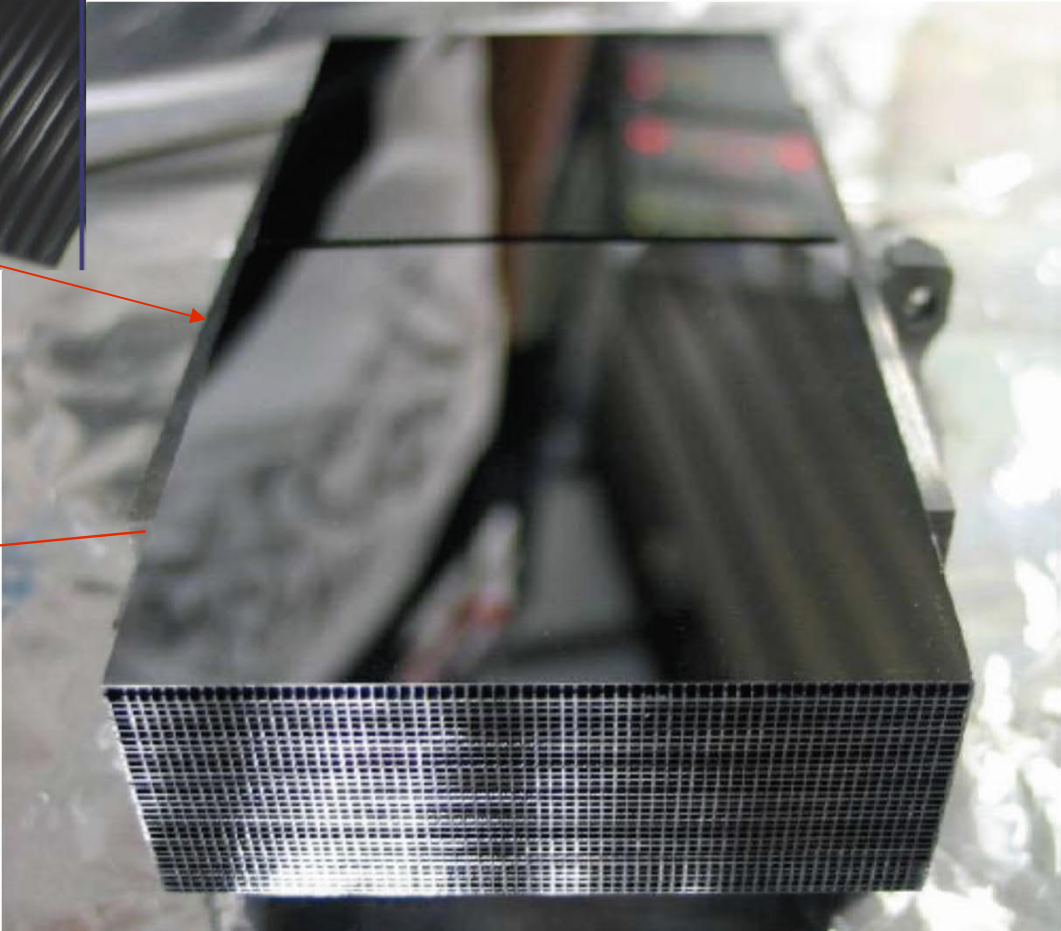
*replicated foil mirror segment*

The European X-ray satellite EXOSAT had two Wolter telescopes made in a similar way but with a beryllium substrate instead of aluminum foil.

3.4. Silicon Pore Optics



*based on Silicon Wafers*



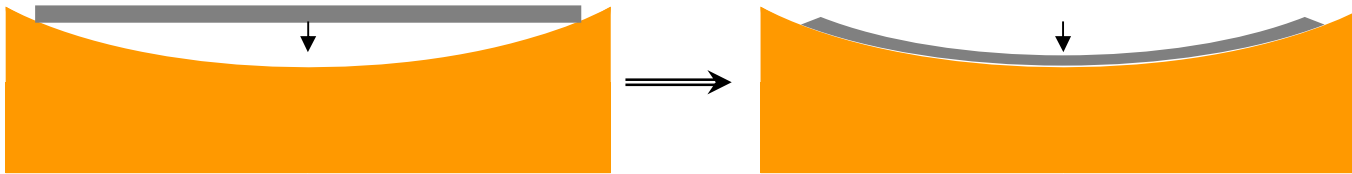
*prototype pore optics element with 2 reflections*

### 3.5. Slumped Glass

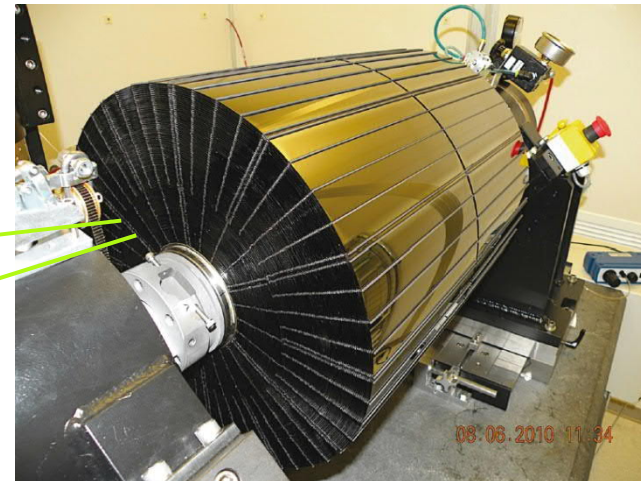
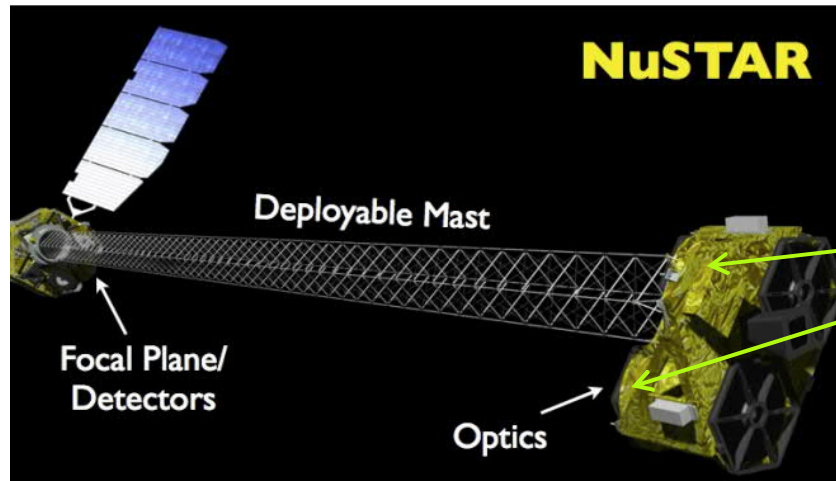
*Technique:*

*Glass sheets are heated above the annealing point (but below the melting point), the lowering viscosity let them slump into a given mould.*

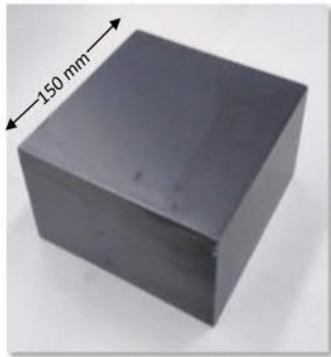
*The glass used for this process has a micro-roughness which is already good for X-ray reflection.*



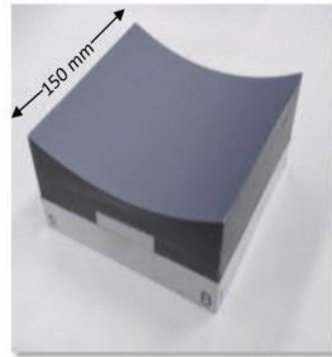
*NuSTAR is the first X-ray satellite in orbit with telescopes made of slumped glass (angular resolution: ~50 arc seconds).*



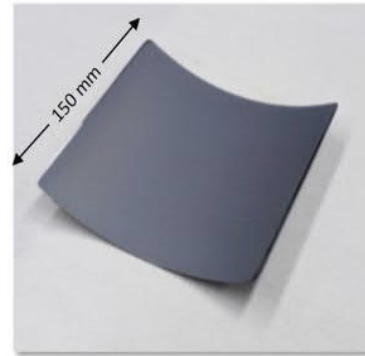
### 3.6. Polished Silicon Optics



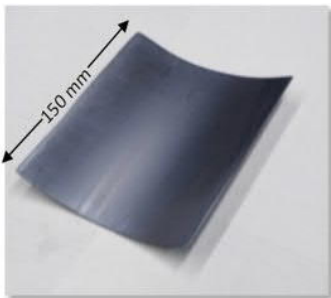
1. Mono-crystalline silicon block



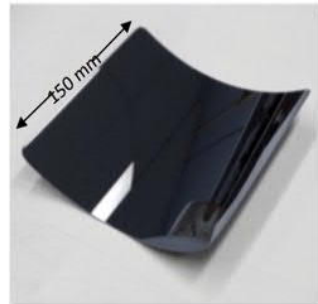
2. Conical form generated



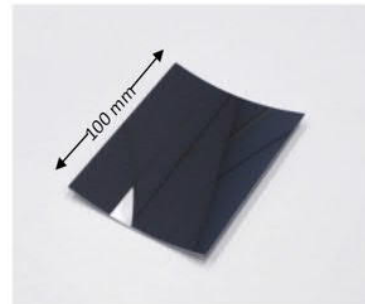
3. Light-weighted substrate



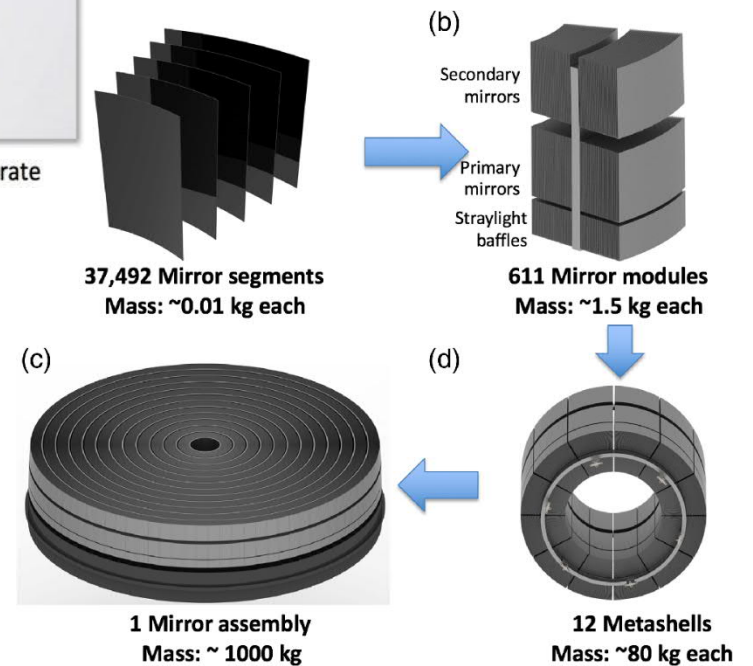
4. Etched substrate



5. Polished mirror substrate



6. Trimmed mirror substrate

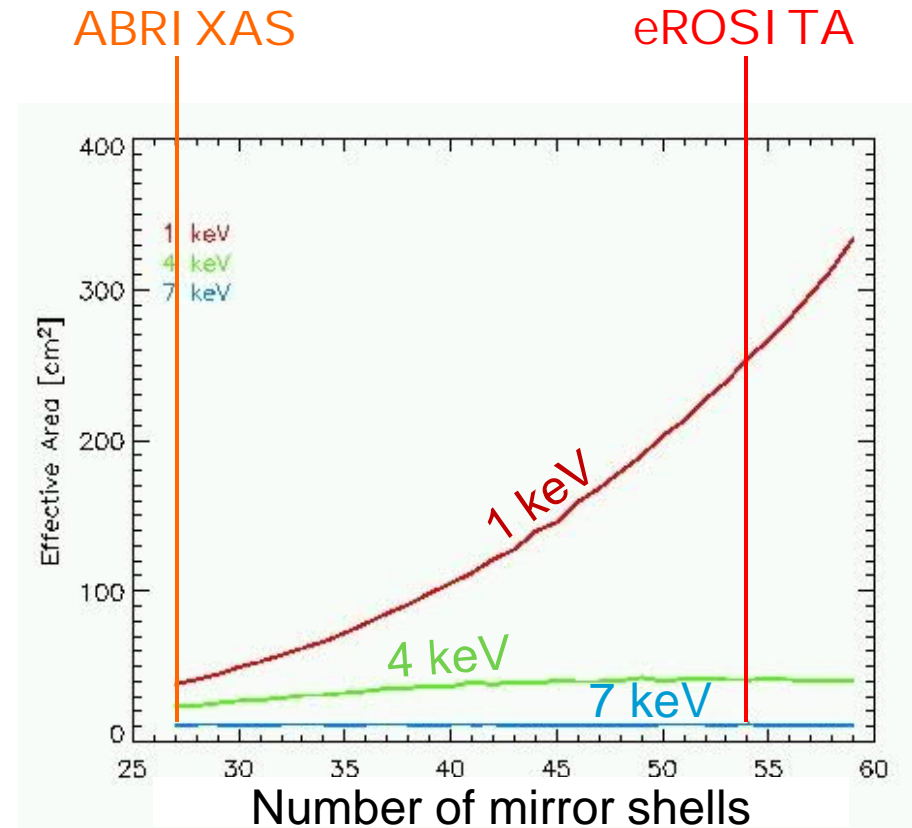
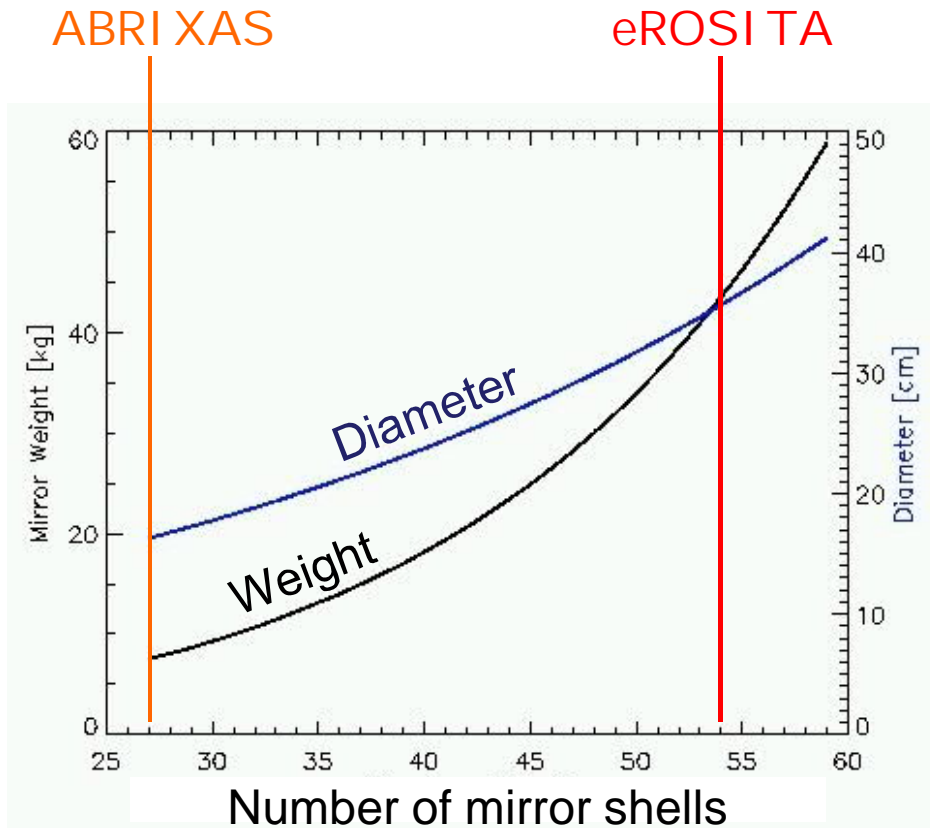
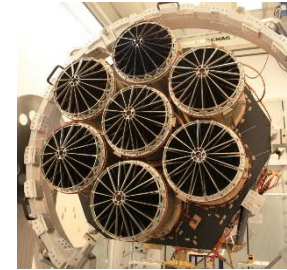


## 4.1. eROSITA Optics Design

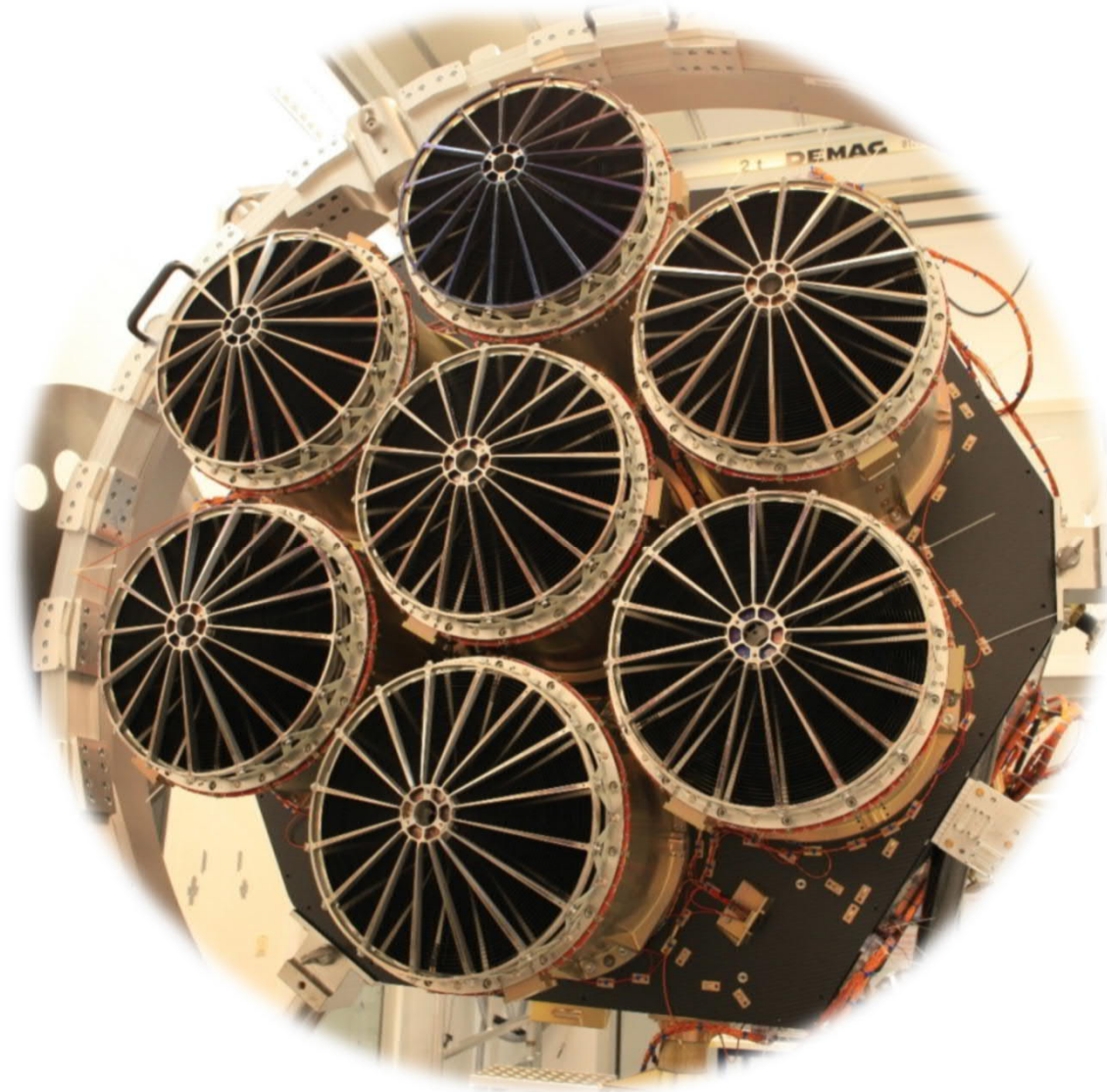


# Mirror Design

## From ABRIXAS to eROSITA



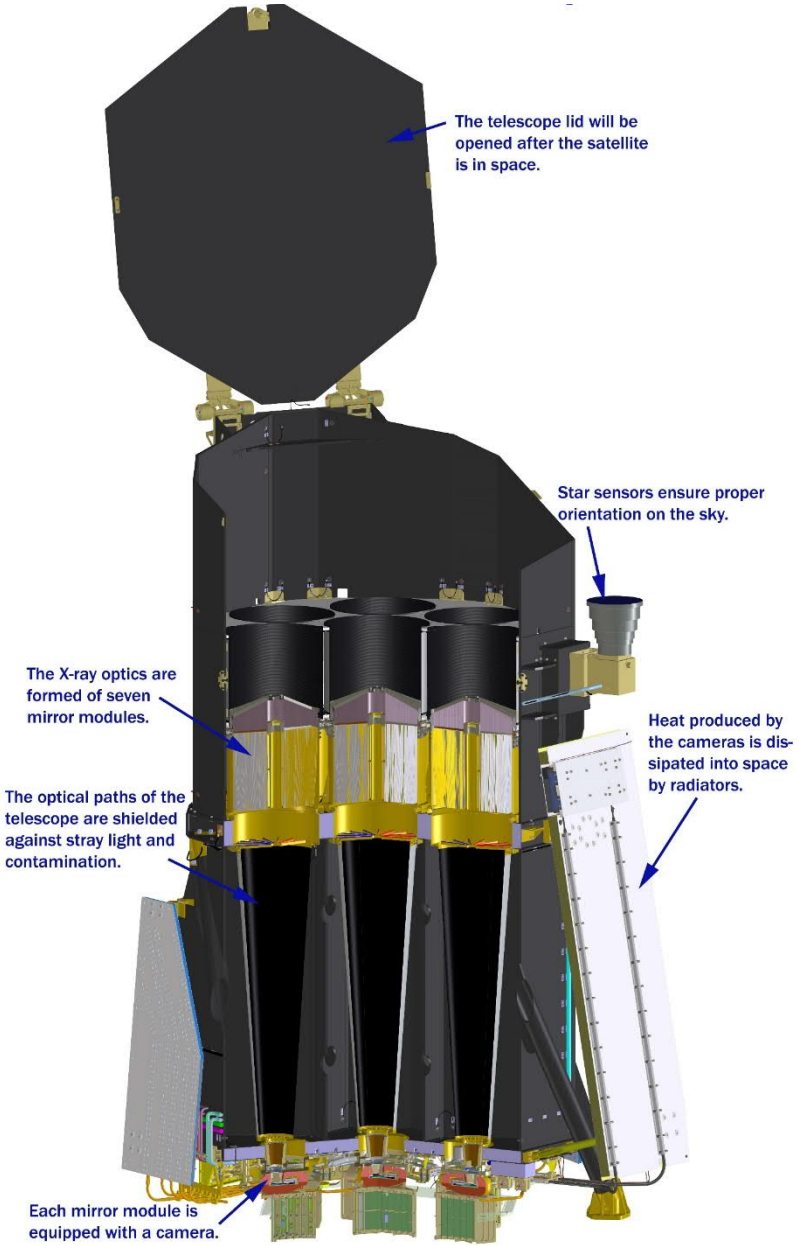
## The X-Ray Telescope eROSITA with its 7 Modules



eROSITA's X-ray telescope consists of 7 co-aligned mirror assemblies, each with 54 nested Wolter-1 electroformed mirror shells and an X-ray baffle made of concentric invar foils.



# The X-Ray Telescope eROSITA



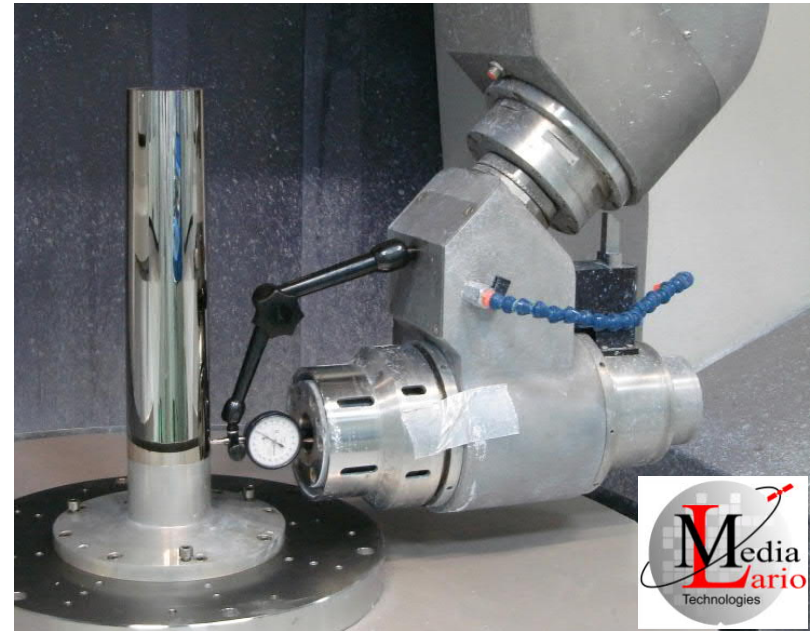
#### 4.2. Development phase and Demonstrator Model

- *Mandrel polishing and refurbishment*
- *Galvanic Nickel Electroforming (based on XMM experience)*
- *Vertical optical bench for mirror shell integration*
- *X-ray tests*

## Mandrels



Refurbished ABRIXAS mandrels



Polishing of new mandrels at Media Lario on on a Zeeko polishing machine

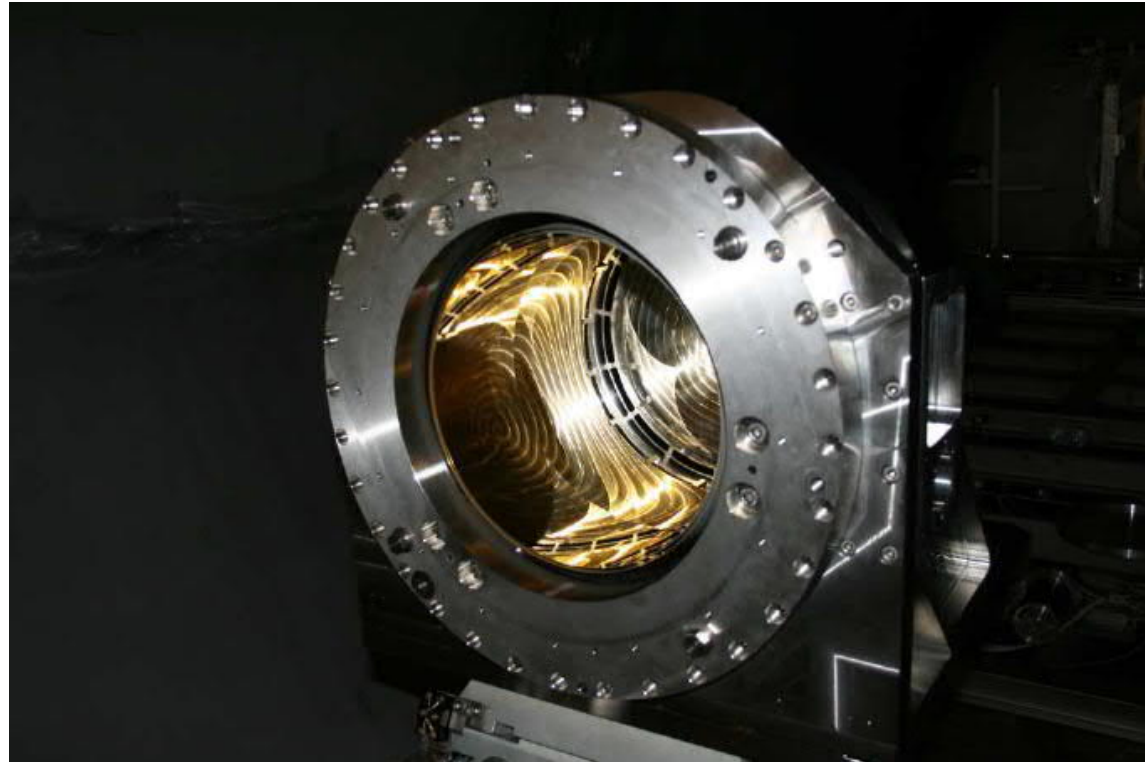


Early 2007: First Mirror Replications  
with refurbished ABRIXAS Mandrels #44 and #46

- **Mandrel #44 (Zeiss)**
  - refurbished ABRIXAS mandrel #17
  - first 2 replications with release problems
  - good release after outgassing procedure but shell has still large roundness errors
  - X-ray test: ~50" HEW
- **Mandrel #46 (Zeiss)**
  - refurbished ABRIXAS mandrel #19
  - 6 replications performed without problems
  - X-ray test: ~24" HEW

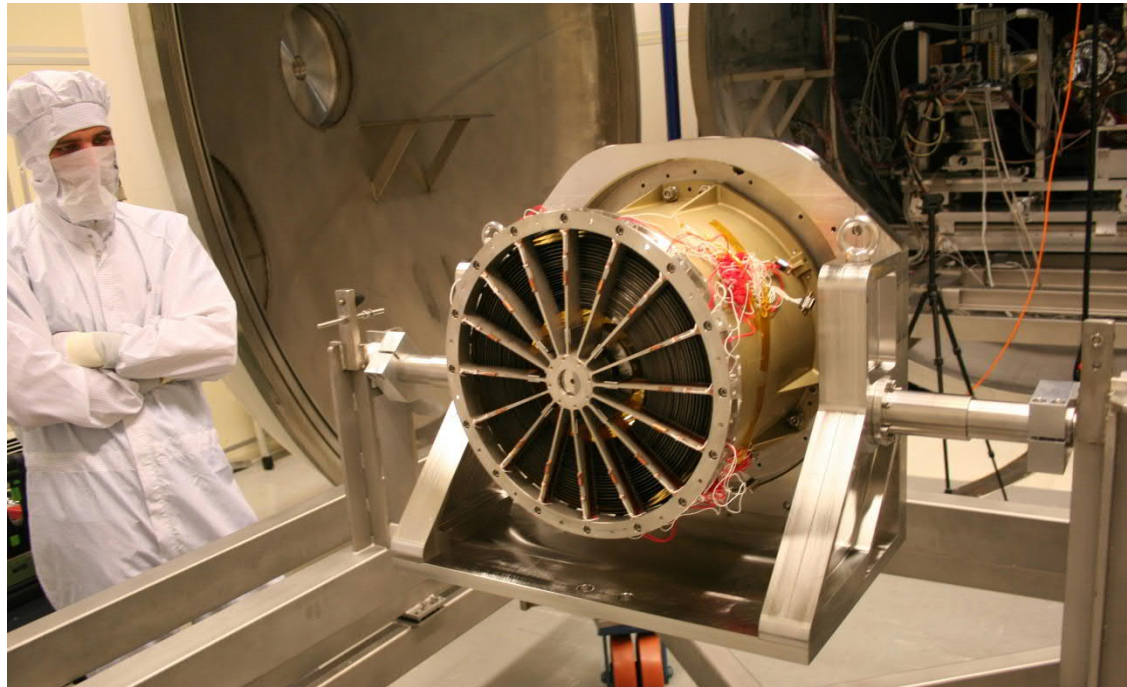


May 2008: Test Mirror Module „DU6“ with mirror shells #1 and #2



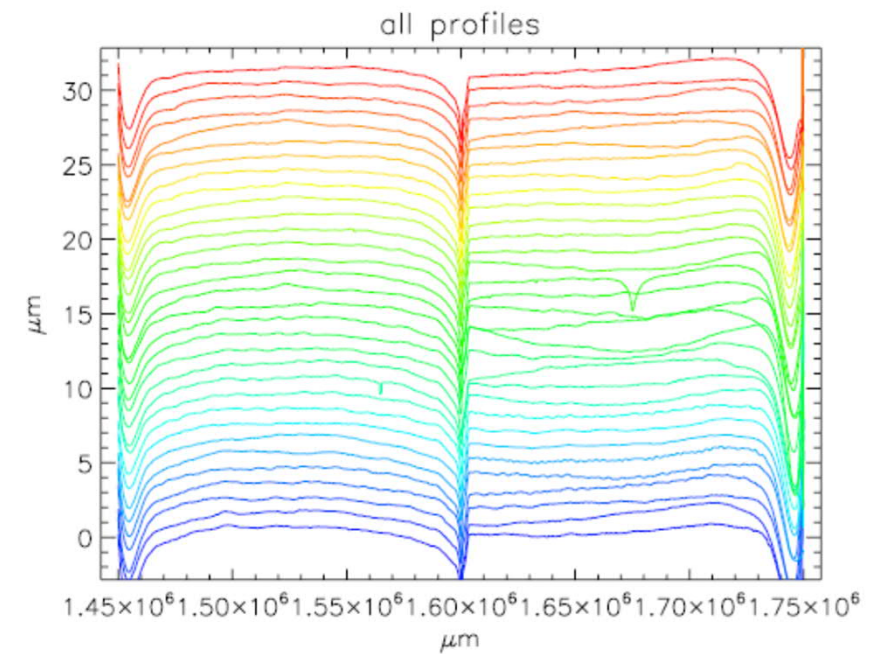
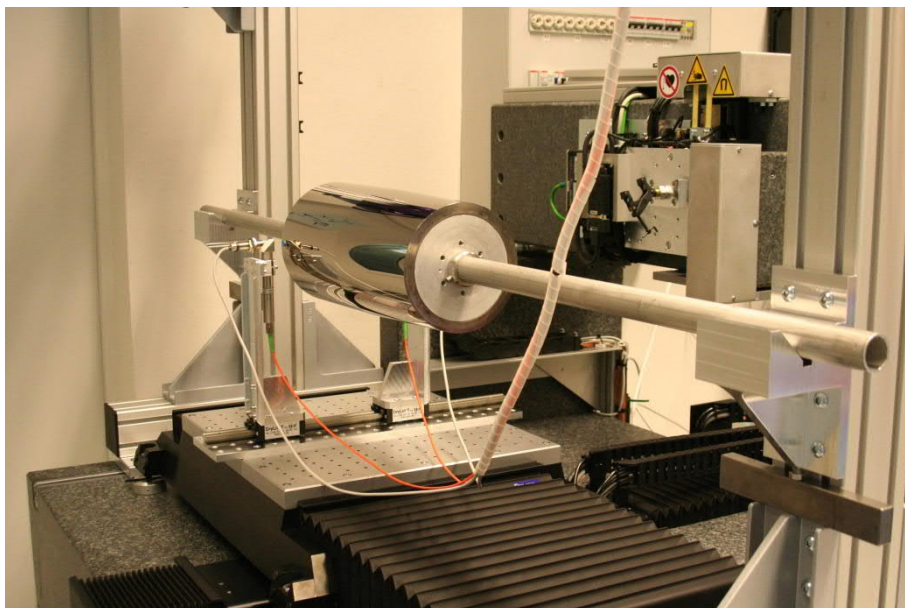
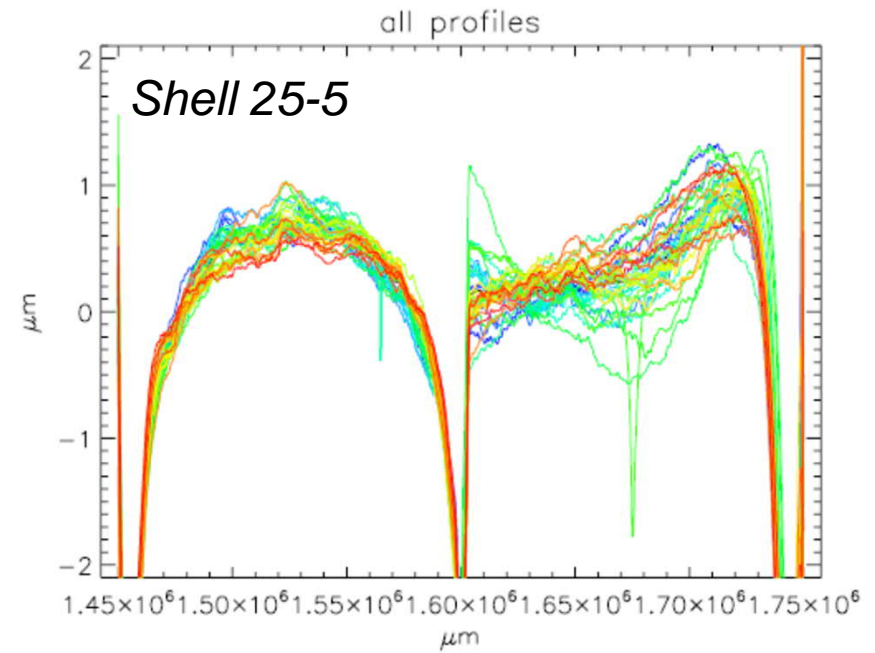
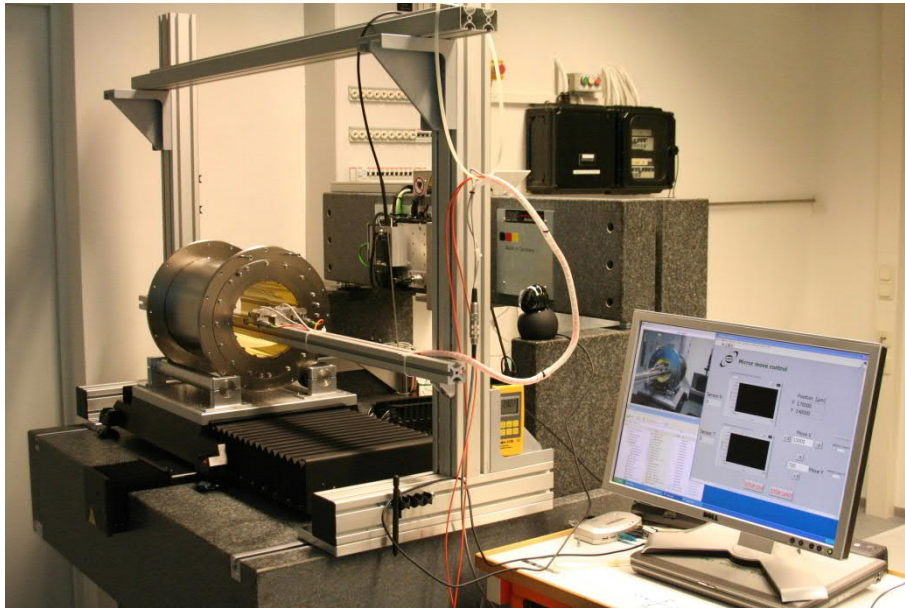
	<b>HEW @ 0.28 keV</b>	<b>HEW @ 1.49 keV</b>	<b>HEW @ 2.98 keV</b>
Shell #1	21.2"	36.2"	61.5"
Shell #2	29.4"	31.9"	43.0"

2009: X-ray tests with Demonstrator Model (Shells #1, #2, #27)

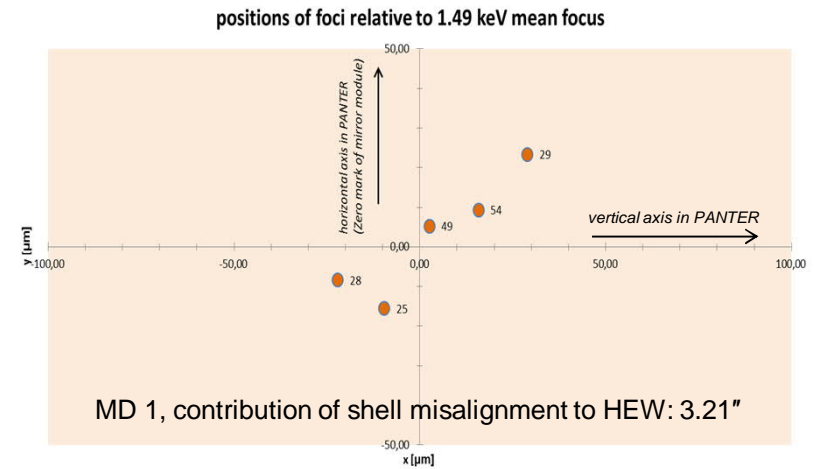
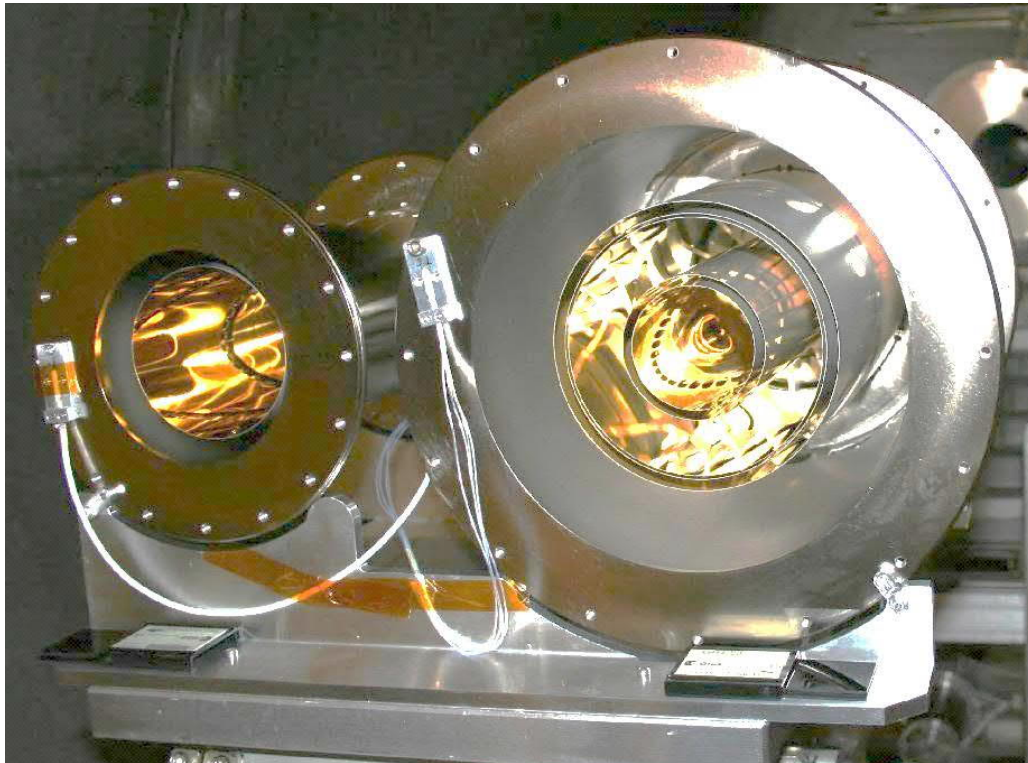


	HEW @ 0.28 keV	HEW @ 1.49 keV	HEW @ 2.98 keV
Shell #1	25.0"	33.5"	55.6"
Shell #2	33.0"	36.9"	58.2"
Shell #27	21.2"	27.7"	31.3"
all	40.0"	40.0"	

# 2009/10: Mirror Verification Phase, Metrology at MPE



## 2009/10: Mirror Verification Phase, X-Ray Tests with “Drums”

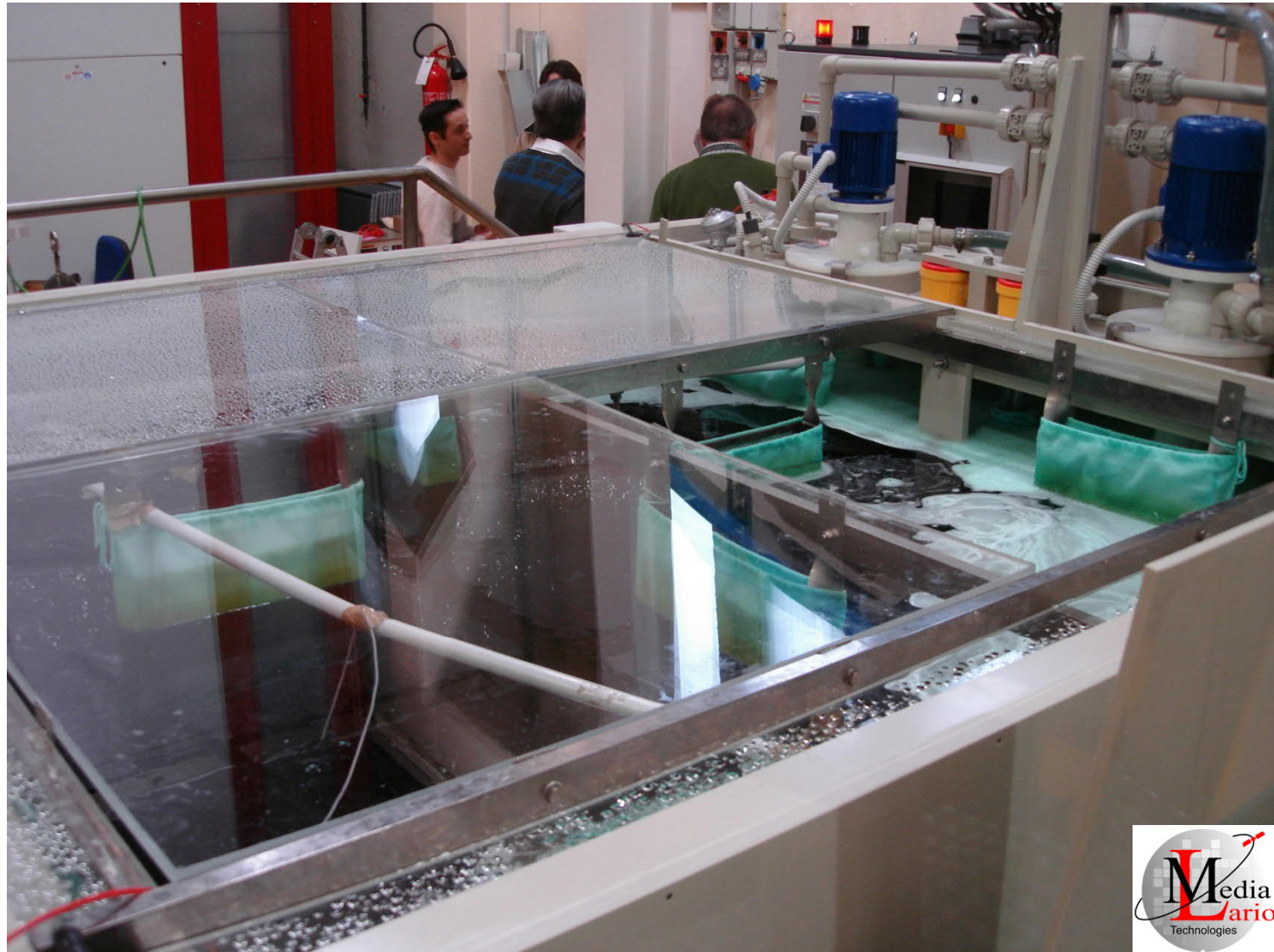


	HEW @ 1.49 keV	HEW @ 8.04 KeV
MD 1	18.4"	17.7"
MD 2	23.4"	20.5"
MD 3	25.6"	28.8"
MD4	19.6"	21.8"

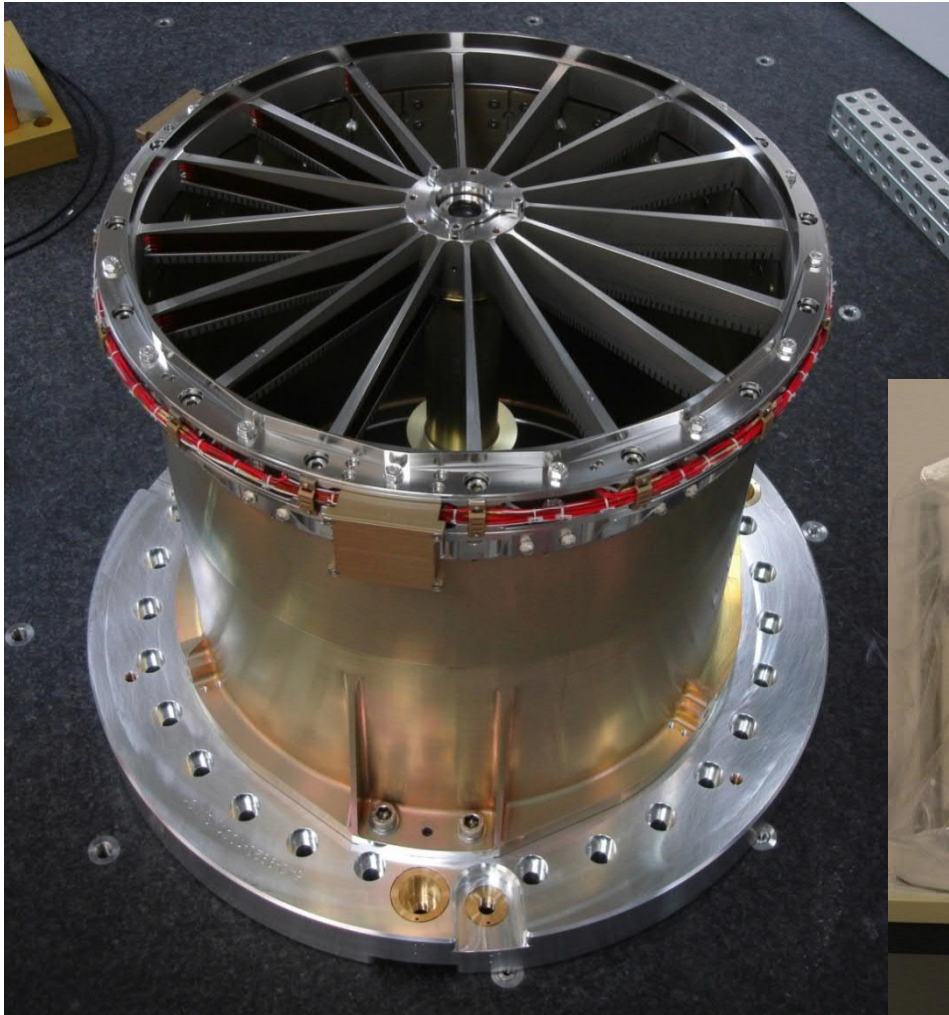
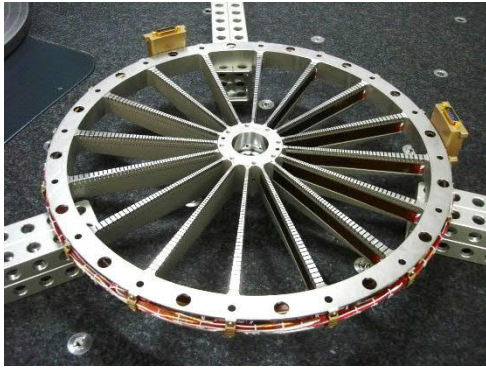


### 4.3. Mirror shell production and integration

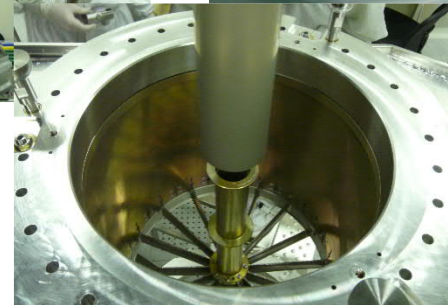
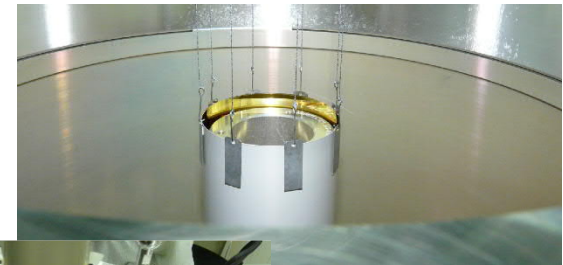
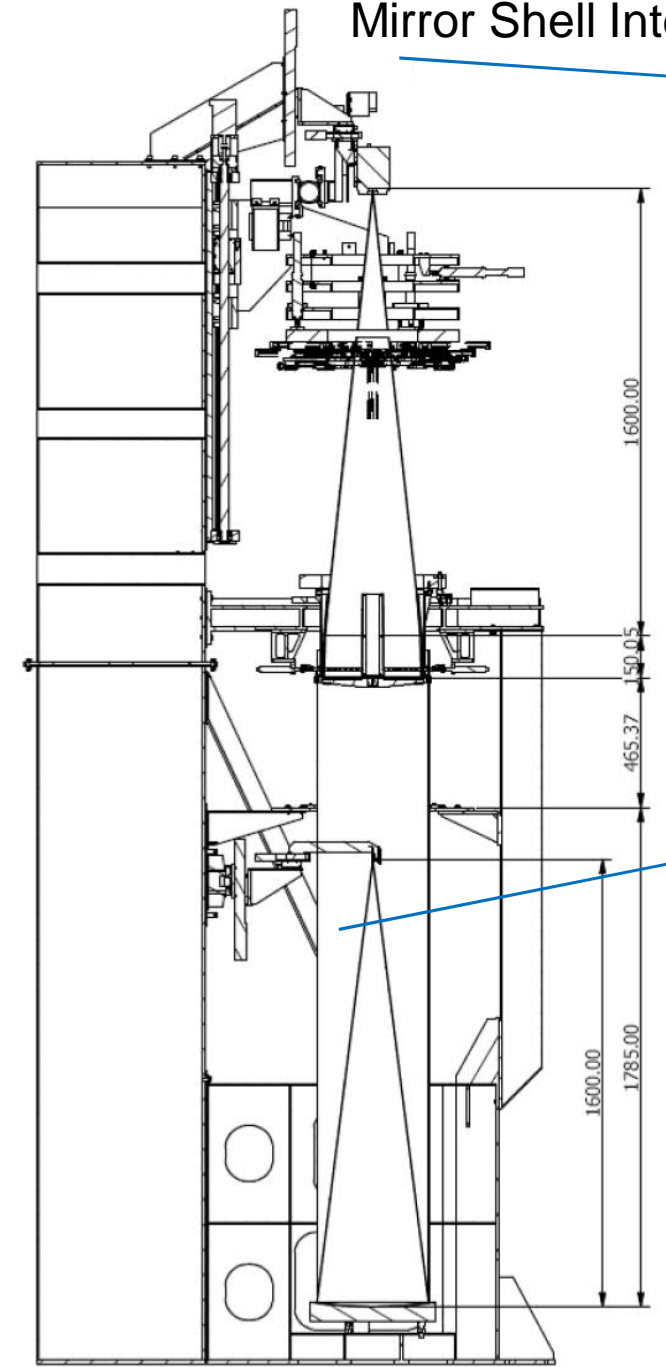
## Electroforming Baths



# Mirror Module Structure

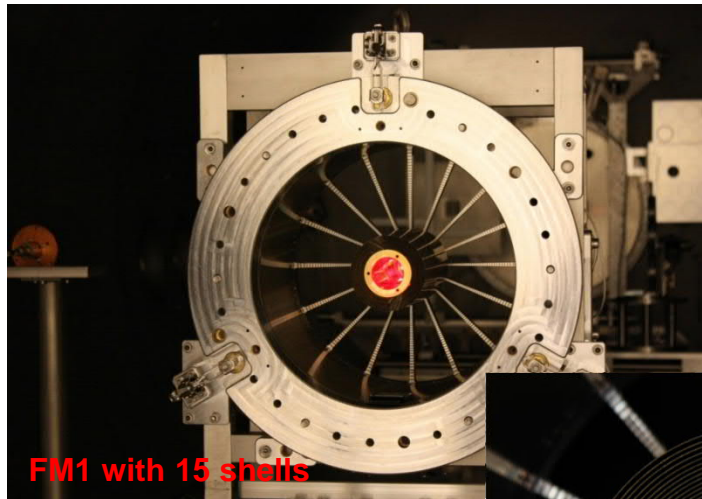


# Mirror Shell Integration on Vertical Optical Bench

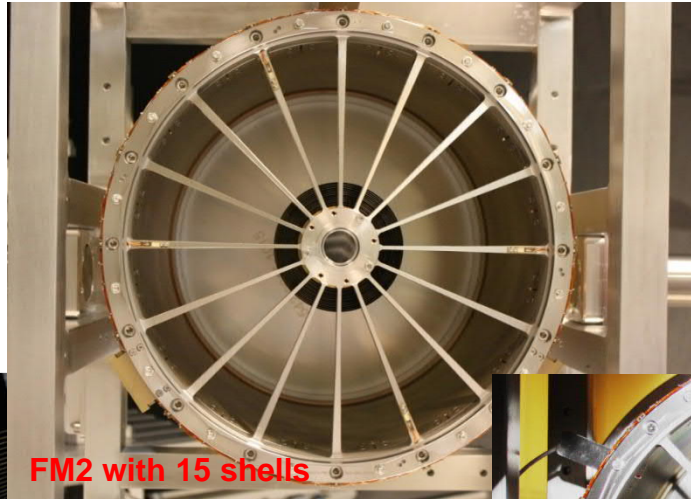


Integration of first mirror shell

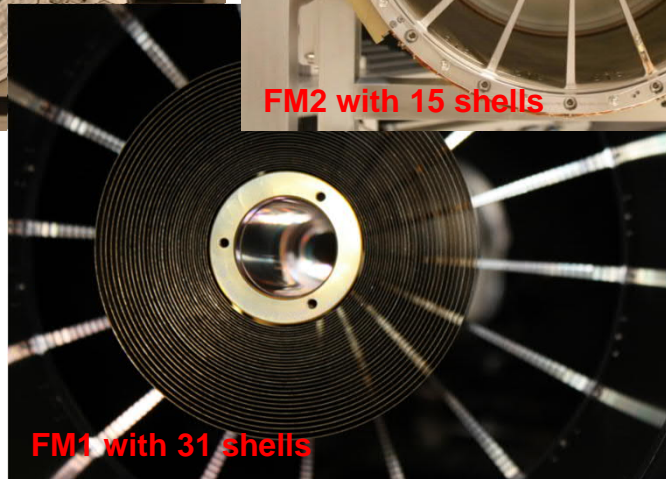
## 2011/12: FM X-Ray Tests with partially integrated modules



FM1 with 15 shells



FM2 with 15 shells



FM1 with 31 shells

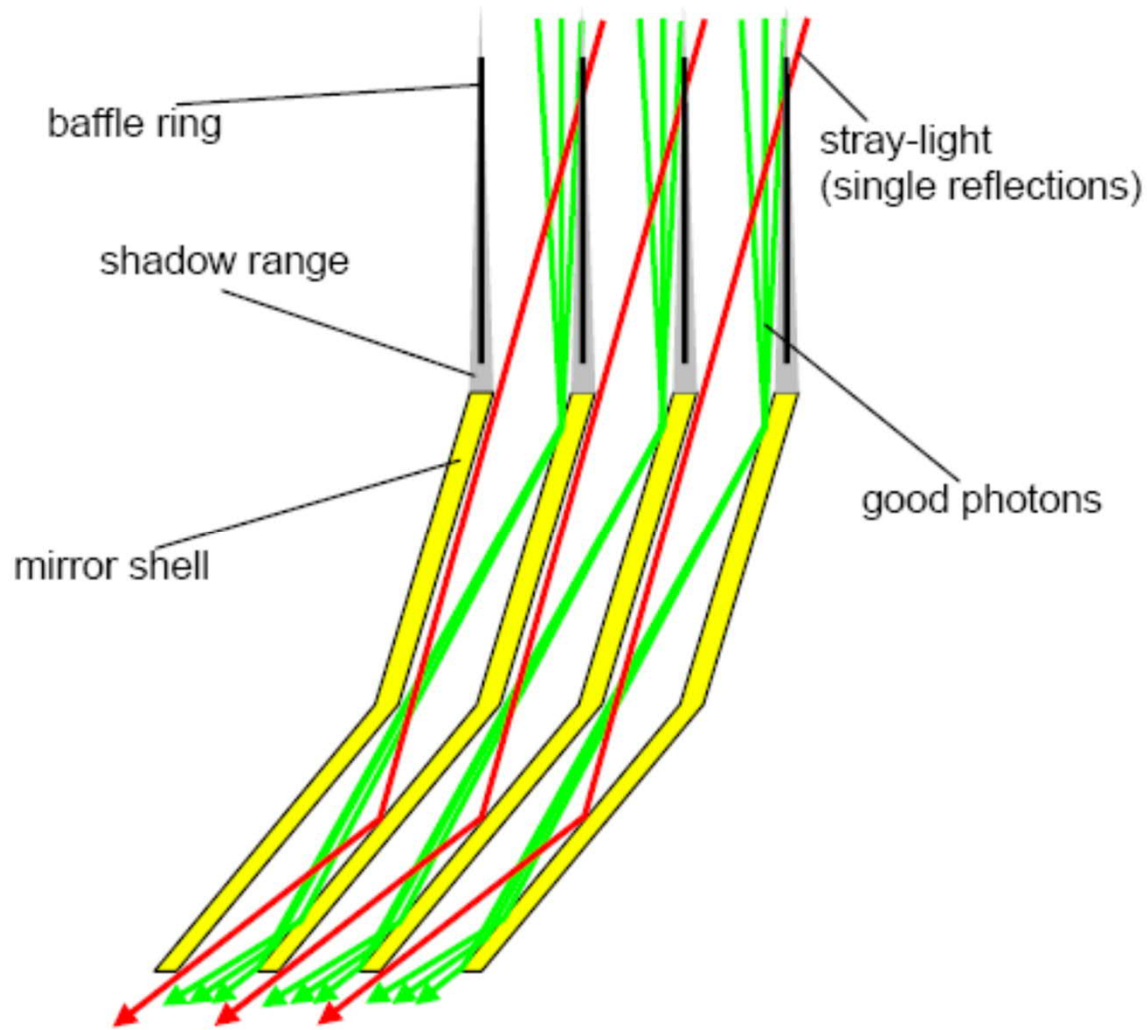


FM3 with 39 shells

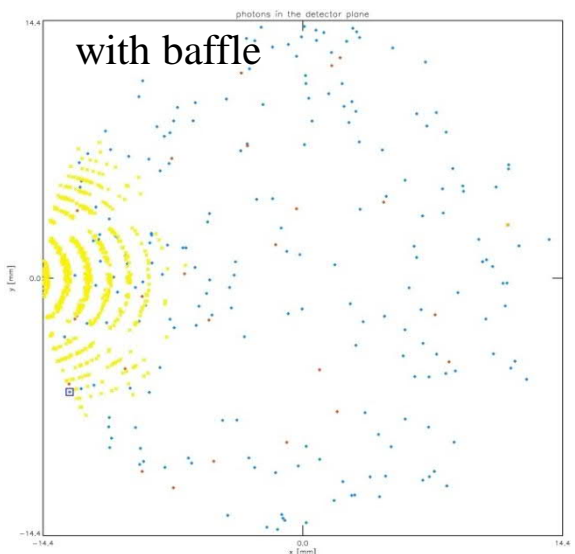
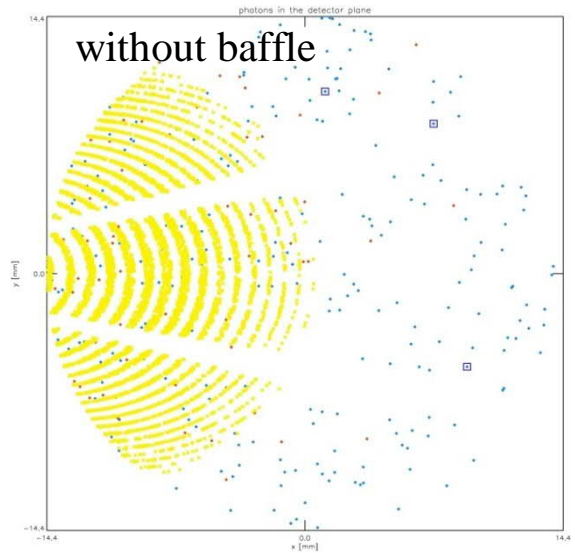
Mirror Module	Test Date	PSF	
		HEW @ 1.5 keV	HEW @ 8.0 keV
FM1 (shells 40-54)	March 2011	13.9±0.1 arcsec *	15.0±0.3 arcsec (all)*
FM2 (shells 40-54)	May 2011	14.4±0.1 arcsec *	15.7±0.4 arcsec (all)*
FM1 (shells 24-54)	June 2011	16.2±0.4 arcsec *	15.5±0.3 arcsec (all)*
FM3 (shells 16-54)	January 2012	16.2±0.4 arcsec *	15.7±0.4 arcsec (all)*

#### 4.4. X-ray baffle against straylight

# X-Ray Baffle Functionality (Ray-Tracing Simulations)

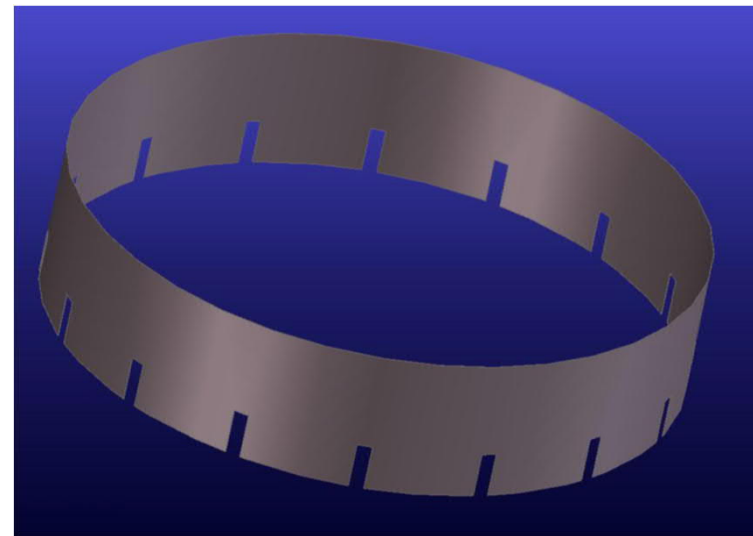
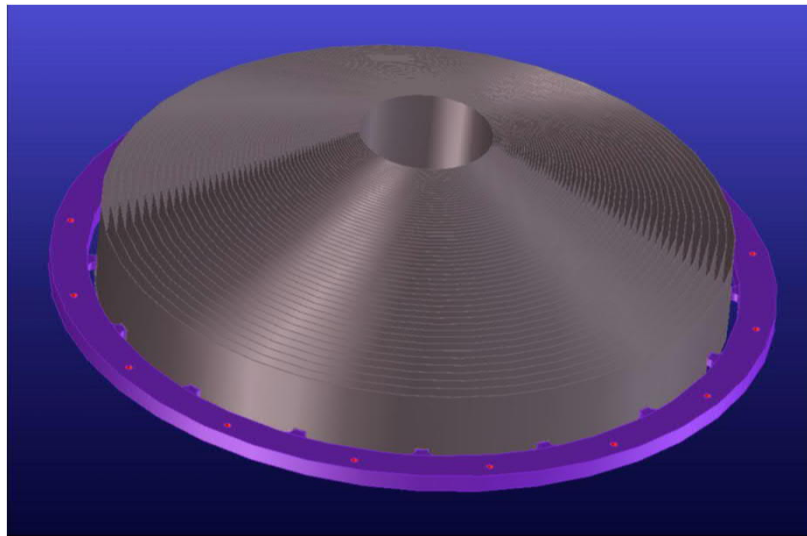


Light source 1° off-axis (i.e. out of FoV)



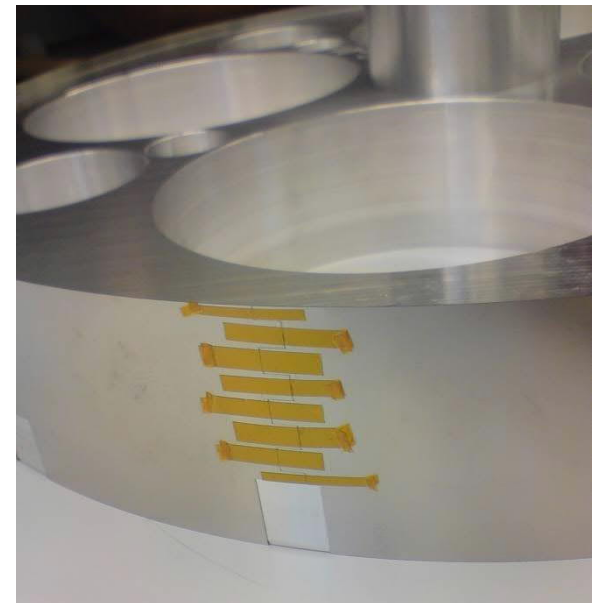
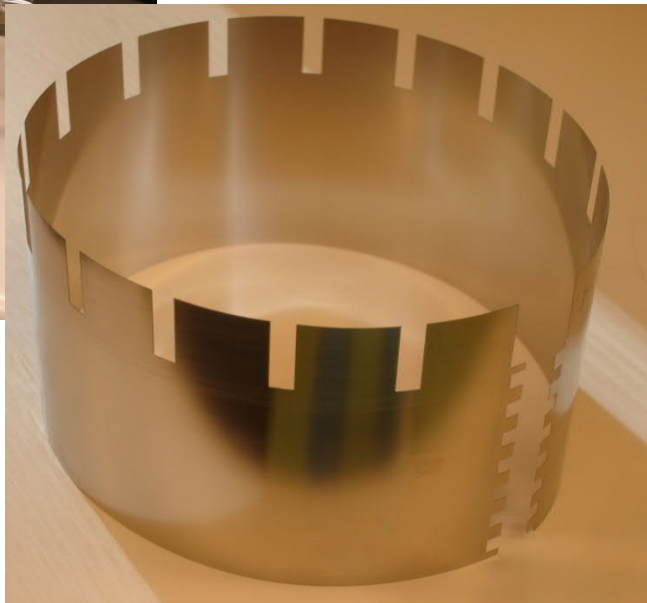
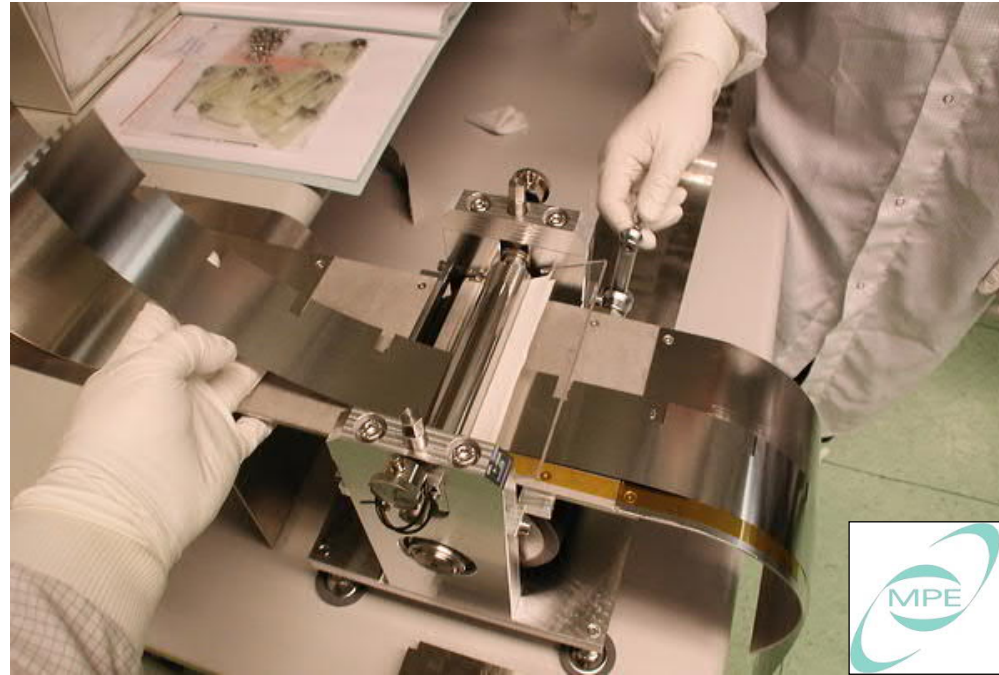
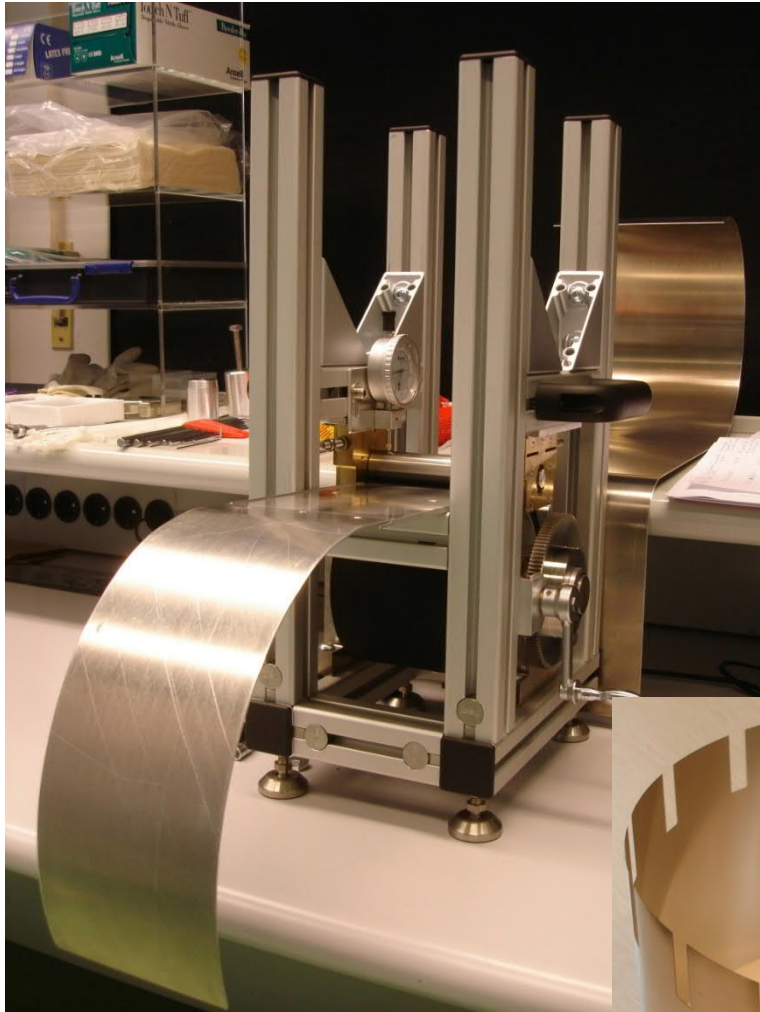
## X-Ray Baffle: Basic Design

- System of 54 cylindrical shells
  - height outer 50 mm, height inner 110 mm, wall thickness 125  $\mu\text{m}$
- Straylight reduction of 95% @1keV (~90% @4keV)

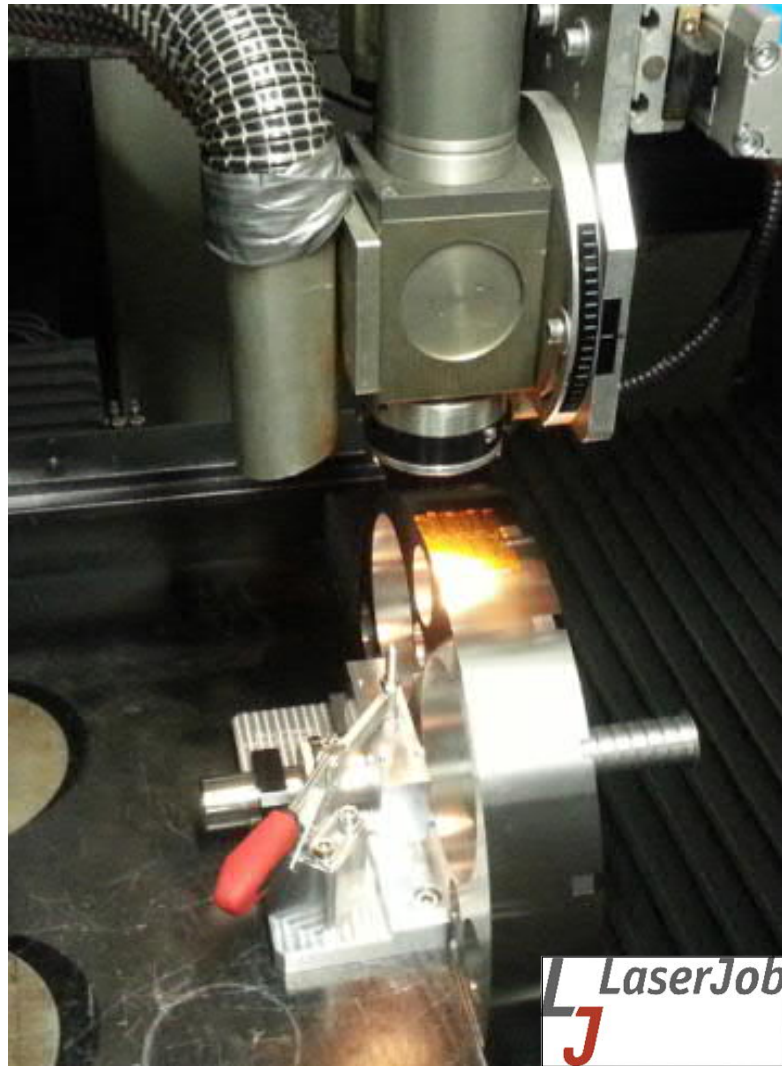




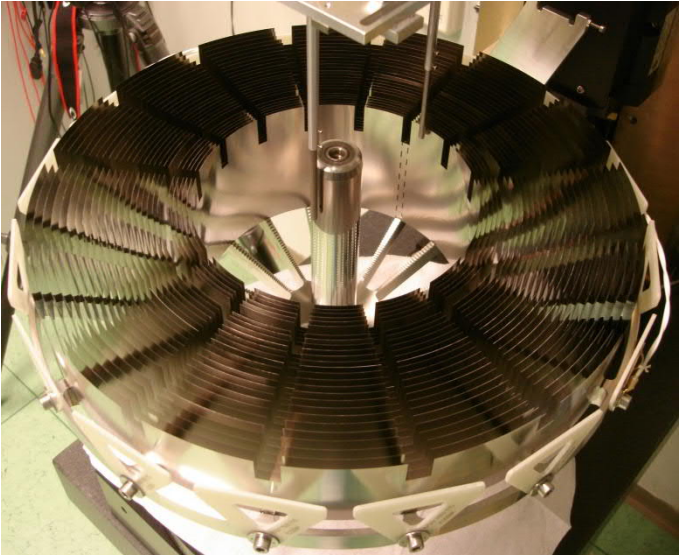
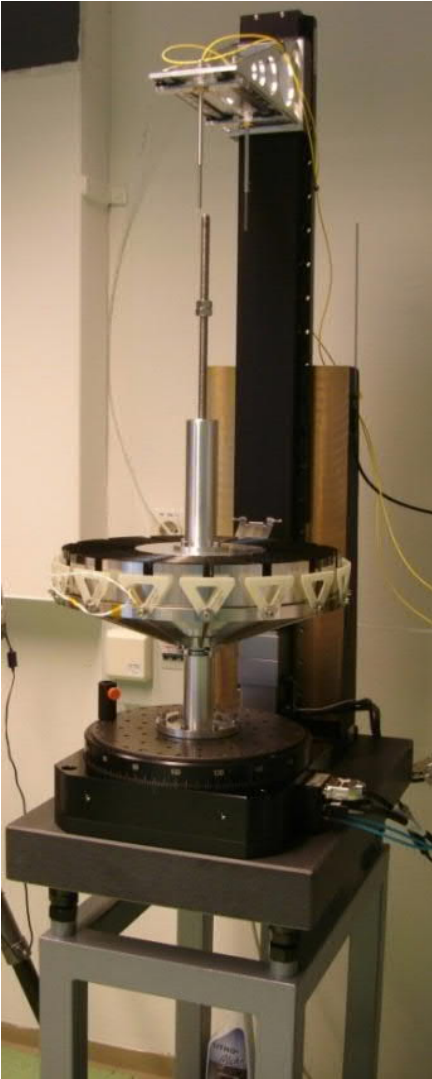
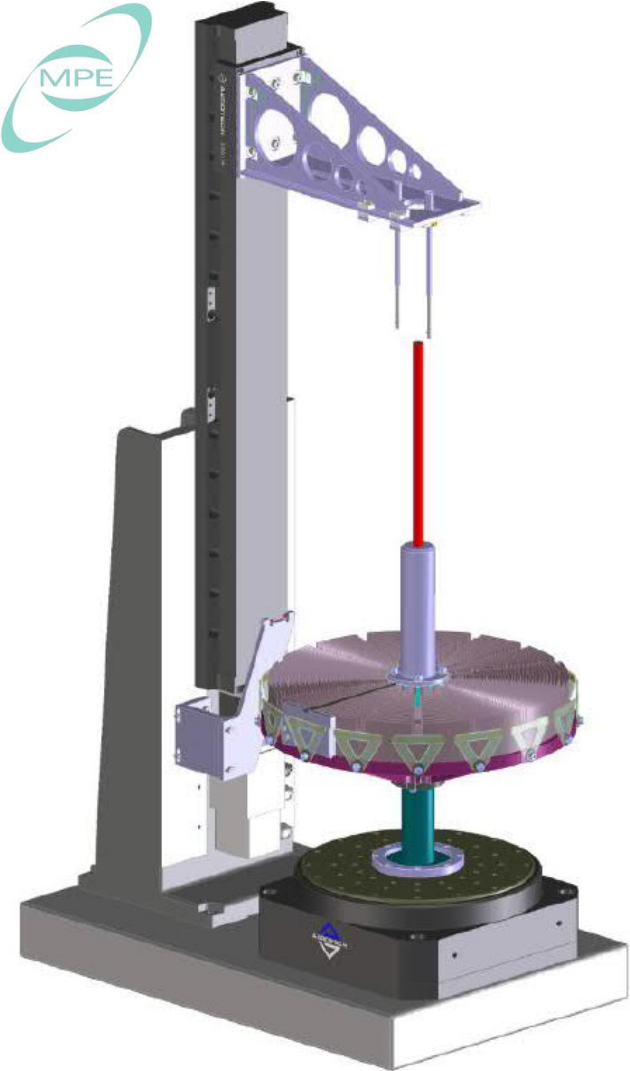
## X-Ray Baffle Manufacturing: Rolling



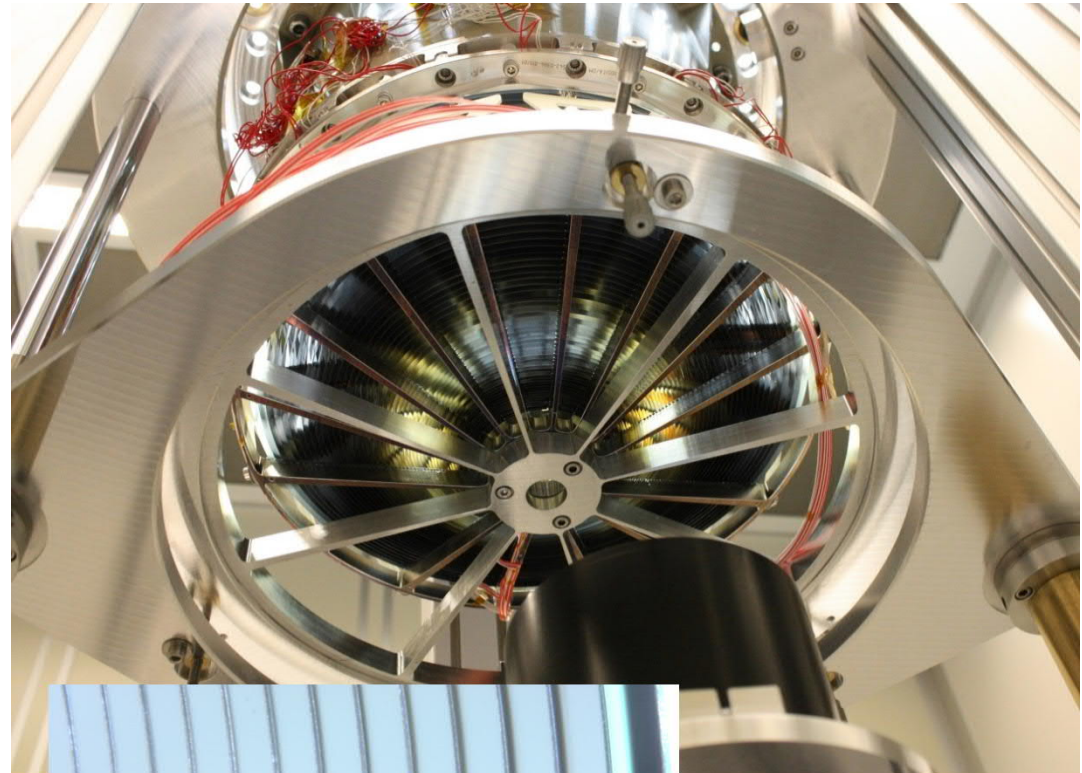
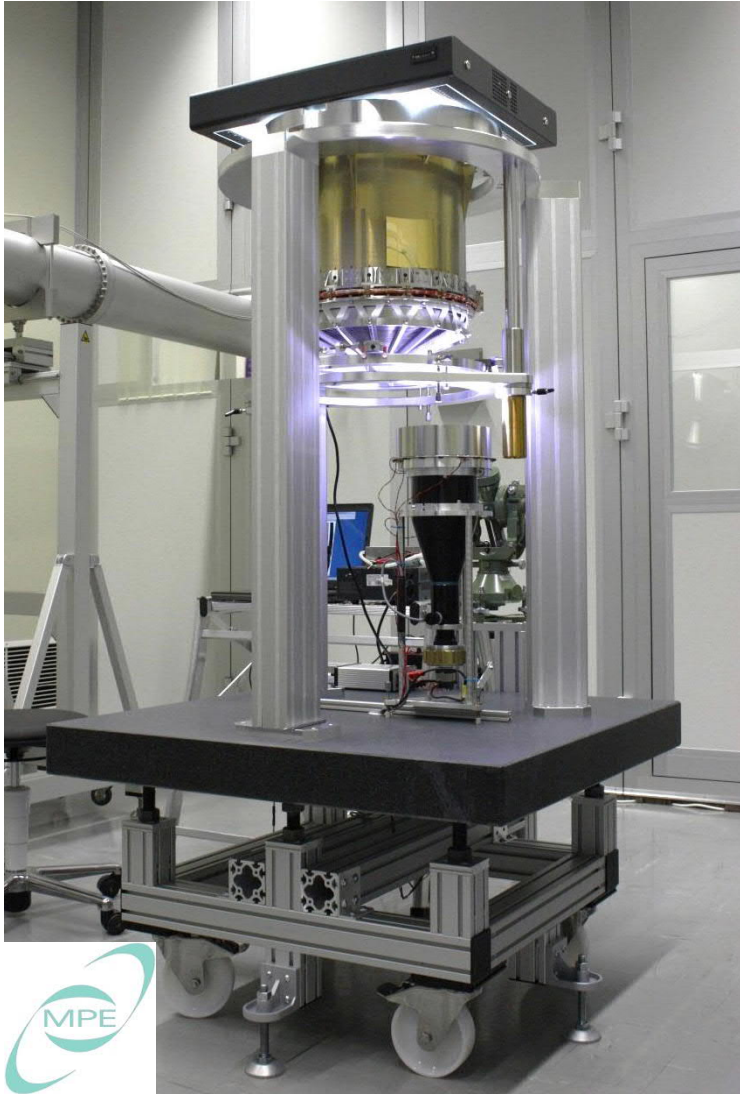
## X-Ray Baffle Manufacturing: Laser Welding



# X-Ray Baffle Integration Stand



## X-Ray Baffle Alignment / Mounting



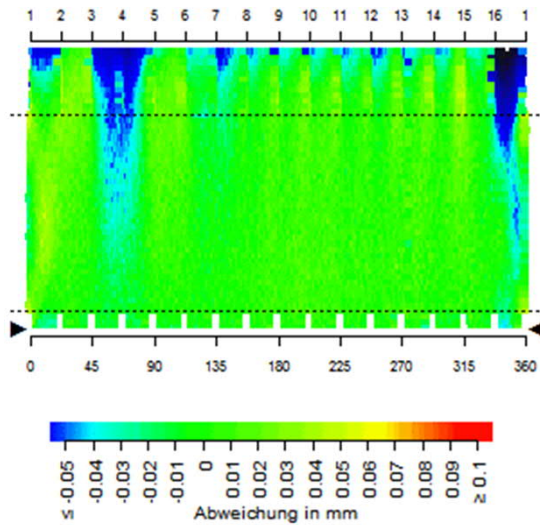
control



alignment to MM...

# X-Ray Baffle Performance

Performance prediction from roundness measurements on baffle integration stand:



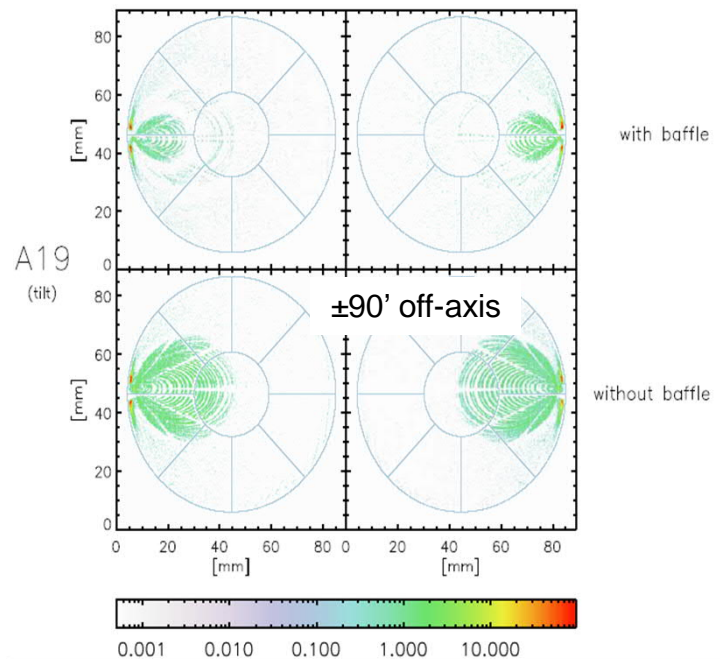
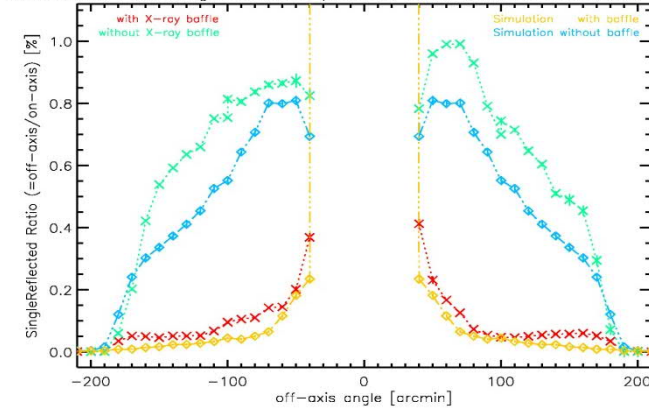
Stray-light (single refl.) reduction: 91-92% (ideal: 95%, accepted 90%)

Relative Loss of effective area: ~2% (still above specification)

X-Ray Baffle	Mirror Assembly	Loss of collecting area	Stray-light reduction
FM1	FM1	2,4%	91,3%
FM3	FM2	2,4%	91,5%
FM4	FM3	2,6%	92,1%
FM5	FM5	2,2%	91,4%
FM6	FM4	2,5%	91,2%
FM7	FM6	2,3%	91,0%
FM8	FM8	2,4%	90,6%
FM9	FM7	2,1%	91,9%

# MA FM1 X-ray measurements

eROSITA MA FM1: Single reflected photons within eROSITA FieldOfView at Al-K



#### 4.5. Tests and Calibration

- *X-ray test facility*
- *Imaging performance (PSF)*
- *Effective collecting area*
- *Focal length measurements*

## Calibration: Overview

PSF

– on-axis

– off-axis mapping

→ verification of performance

→ Input for eSASS and simulations  
(shapelet reconstruction of PSF)

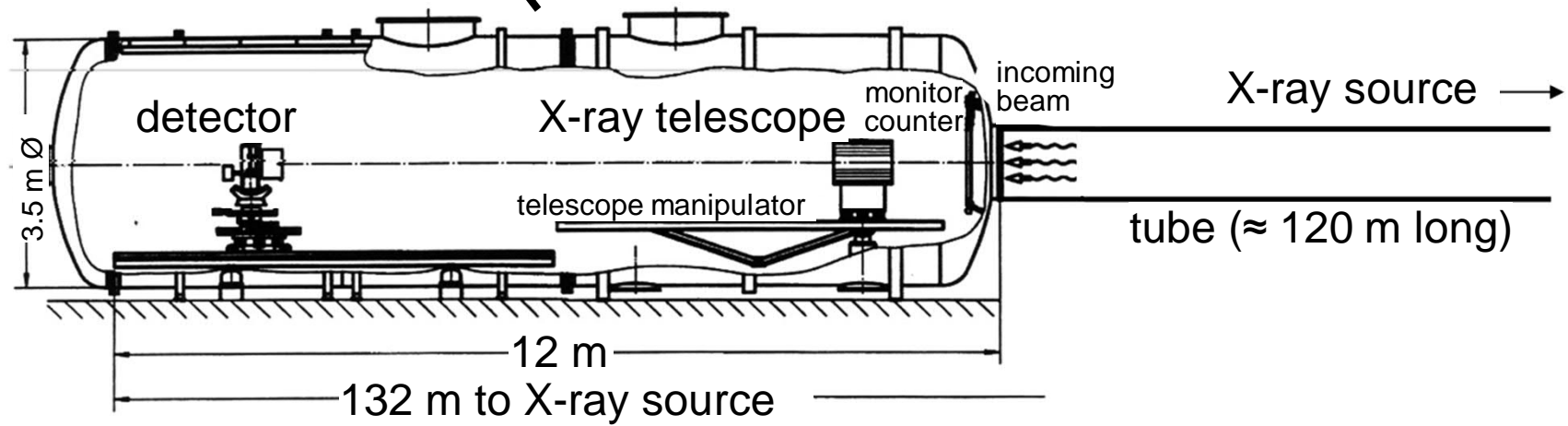
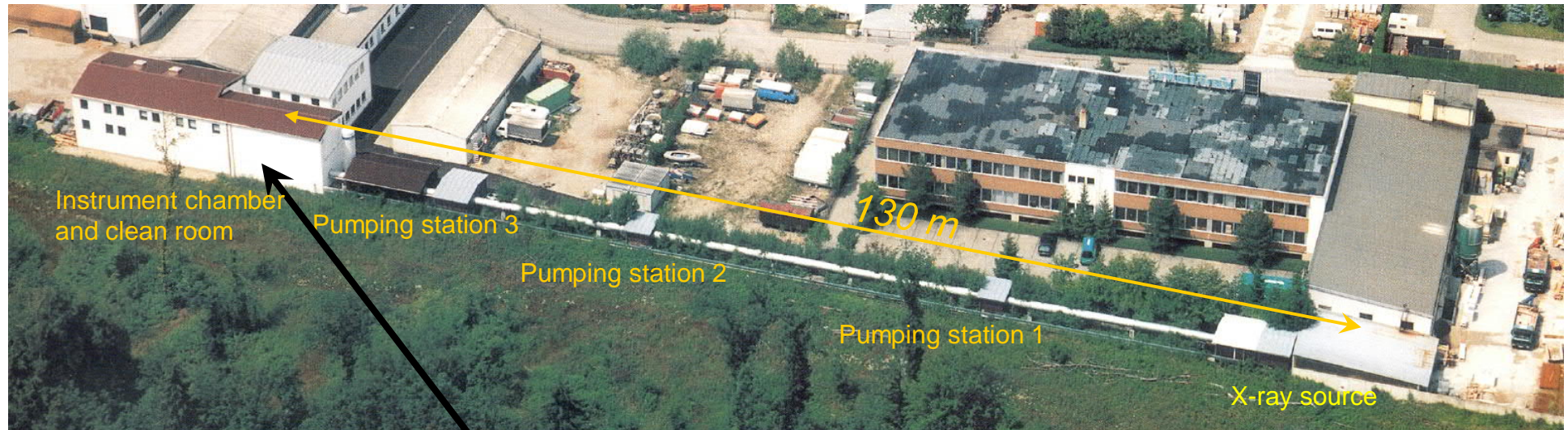
Effective Area (on- /off-axis)  
(difficult / time consuming in orbit)

→ Input for eSASS and for more realistic  
simulations, for prediction of  
sensitivity, number of detectable  
objects

Focal length

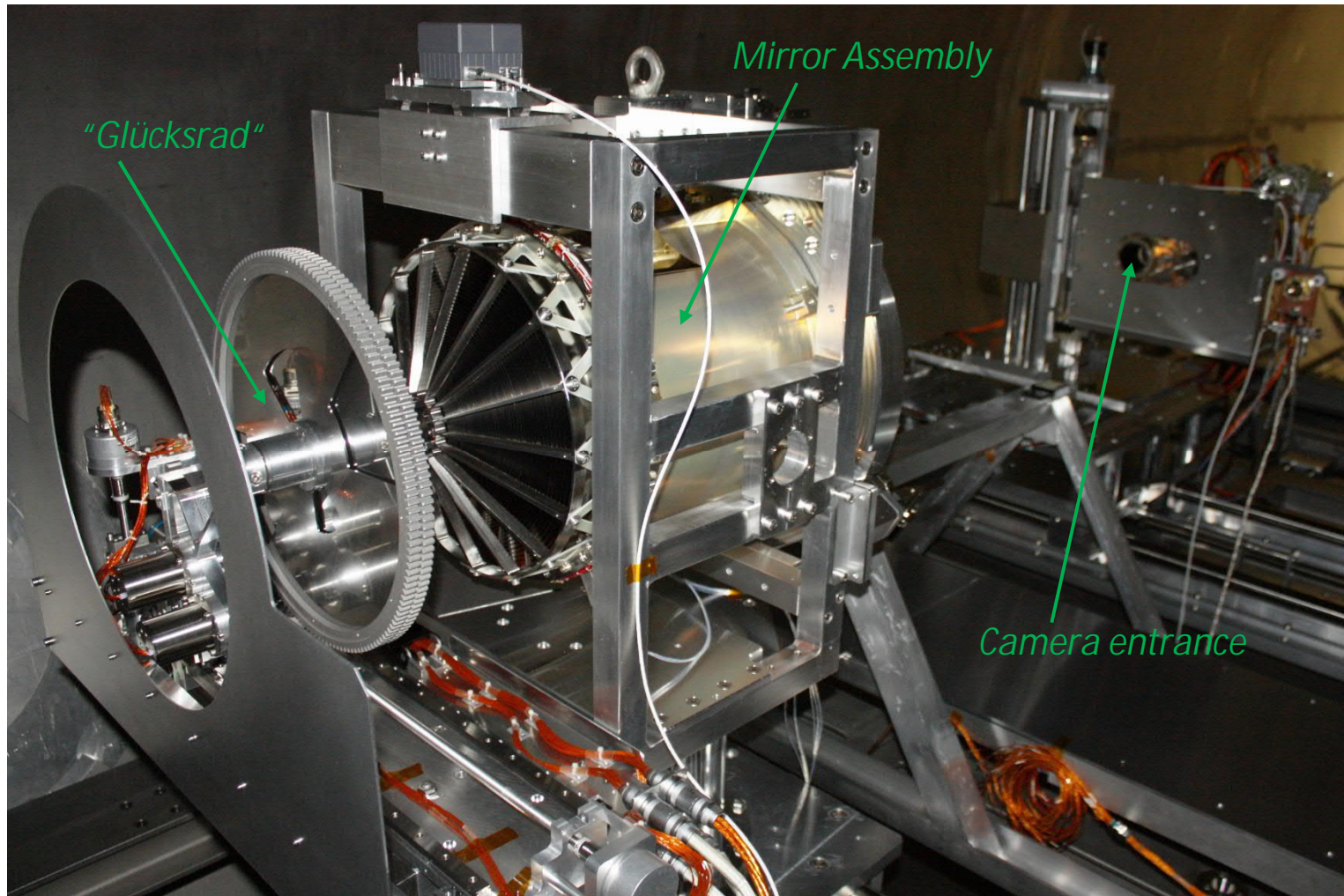
→ Essential input for positioning of the  
cameras in focus, tolerance  $<0.2$  mm

# MPE X-Ray Test Facility „PANTER“



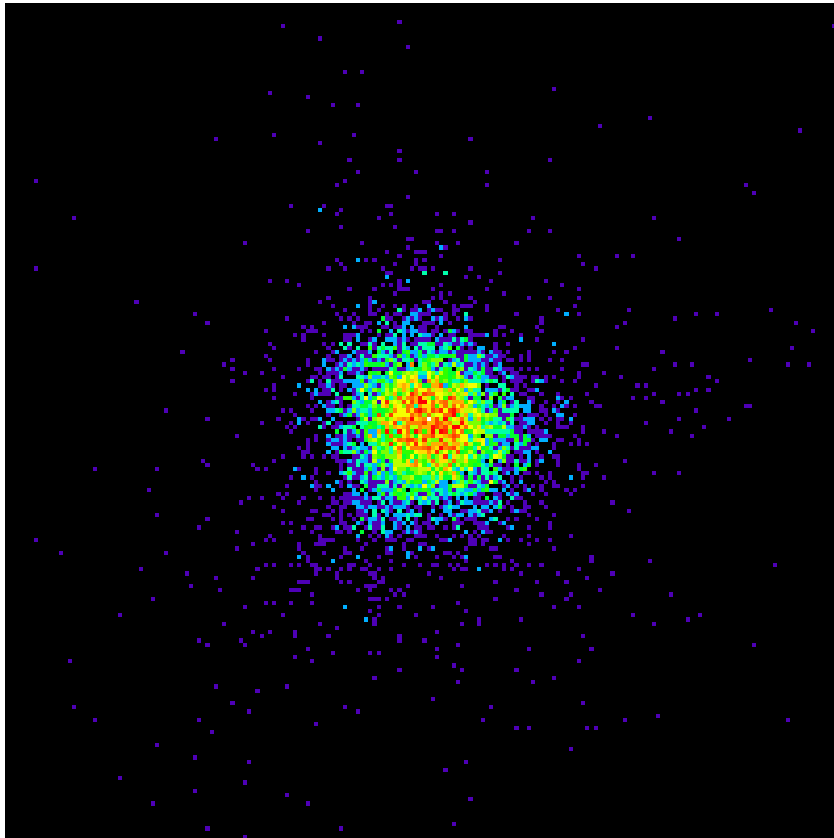


## Setup in PANTER for FM Calibration

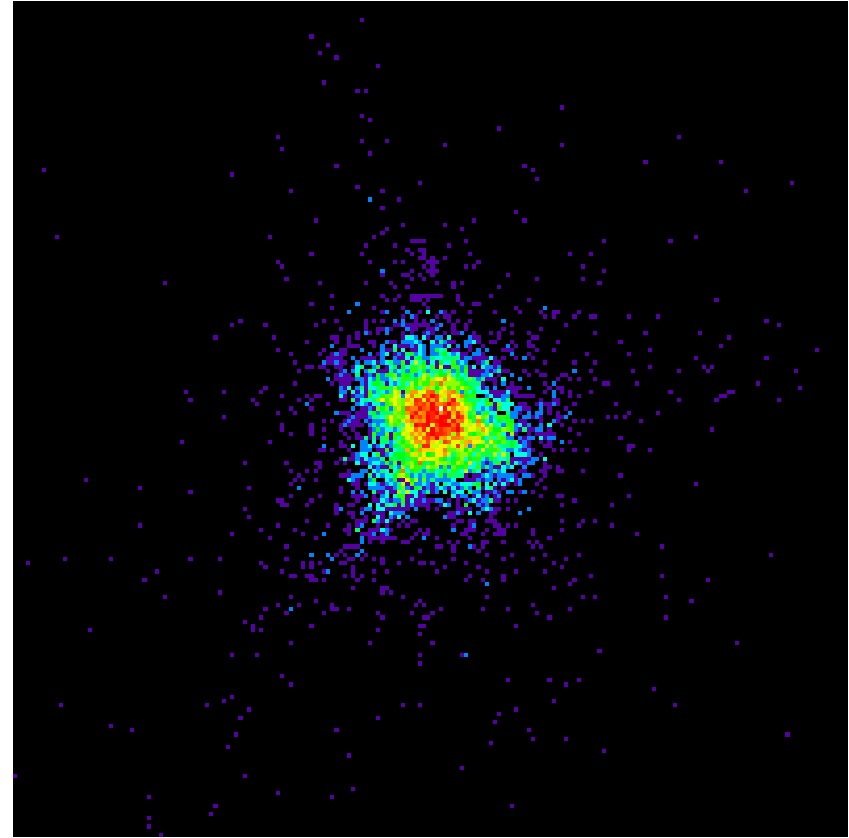


Setup in PANTER vacuum chamber, here Mirror Assembly FM1

# Point spread function (PSF)



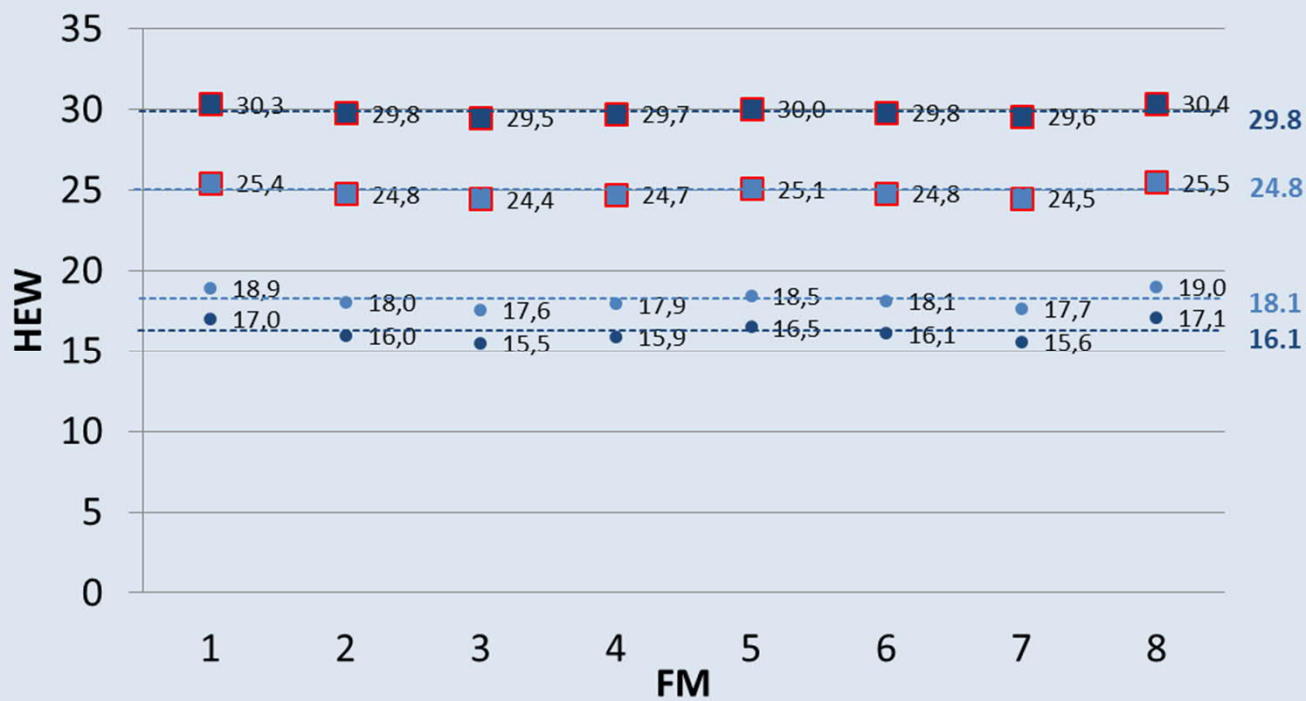
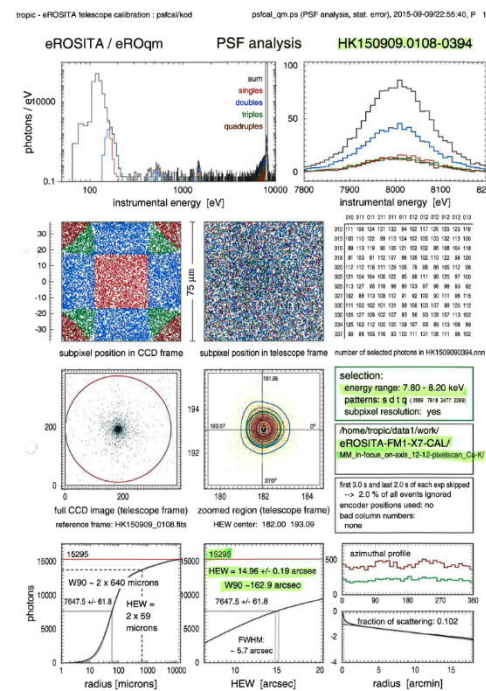
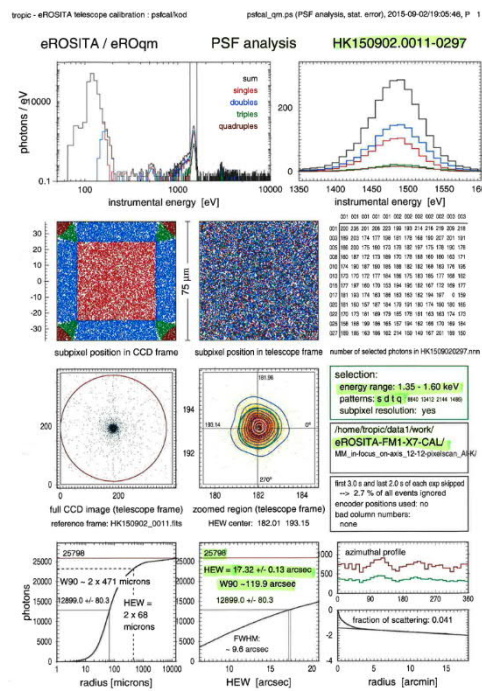
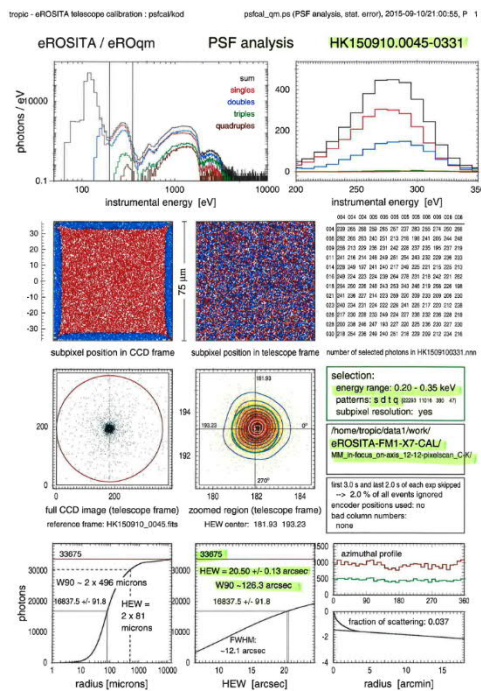
75  $\mu\text{m}$  pixel (ca. 10") resolution: 17.3" HEW



Sub-pixel resolution: 14.7" HEW

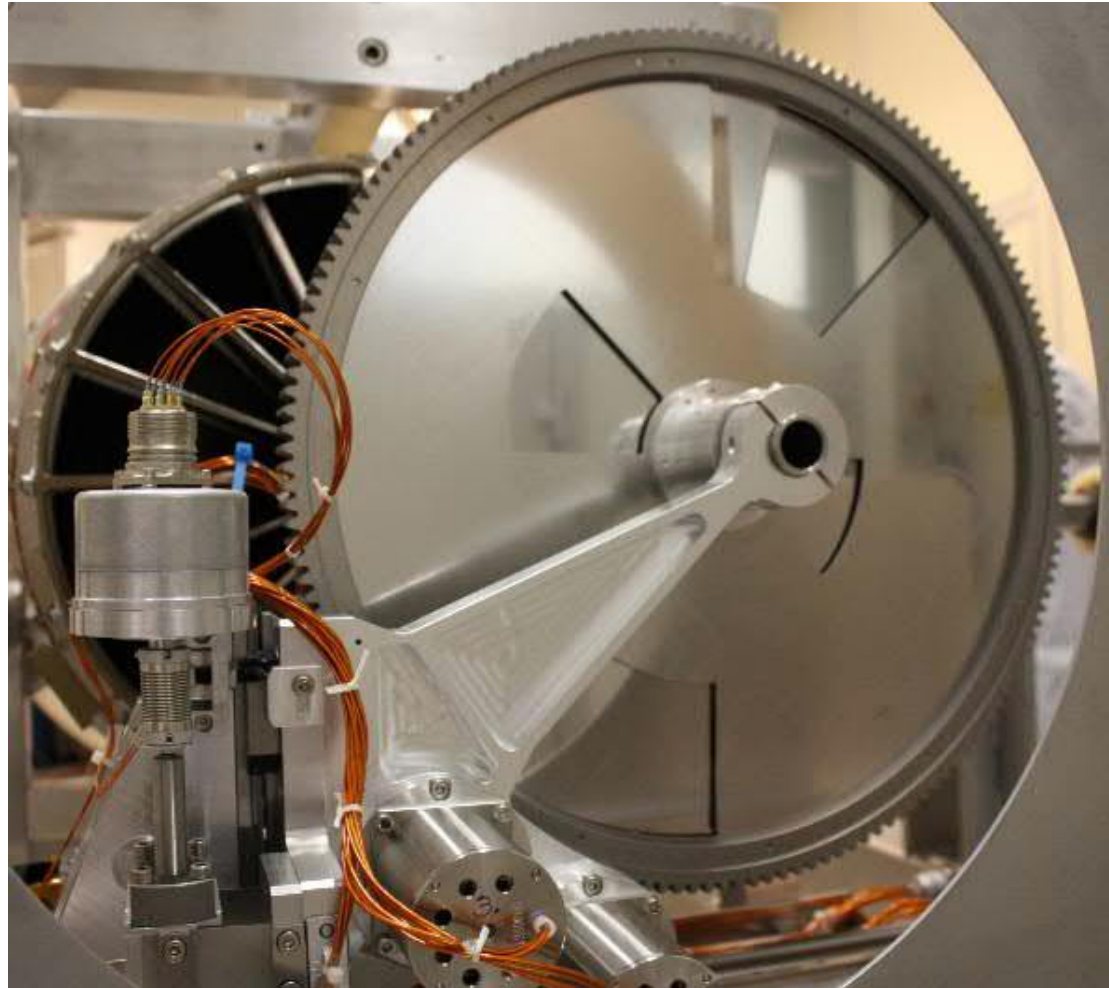
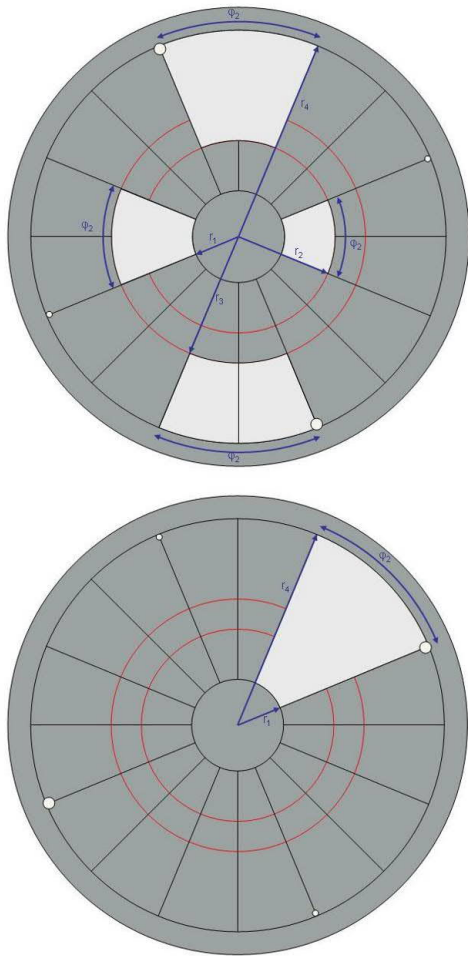


# PSF on-axis



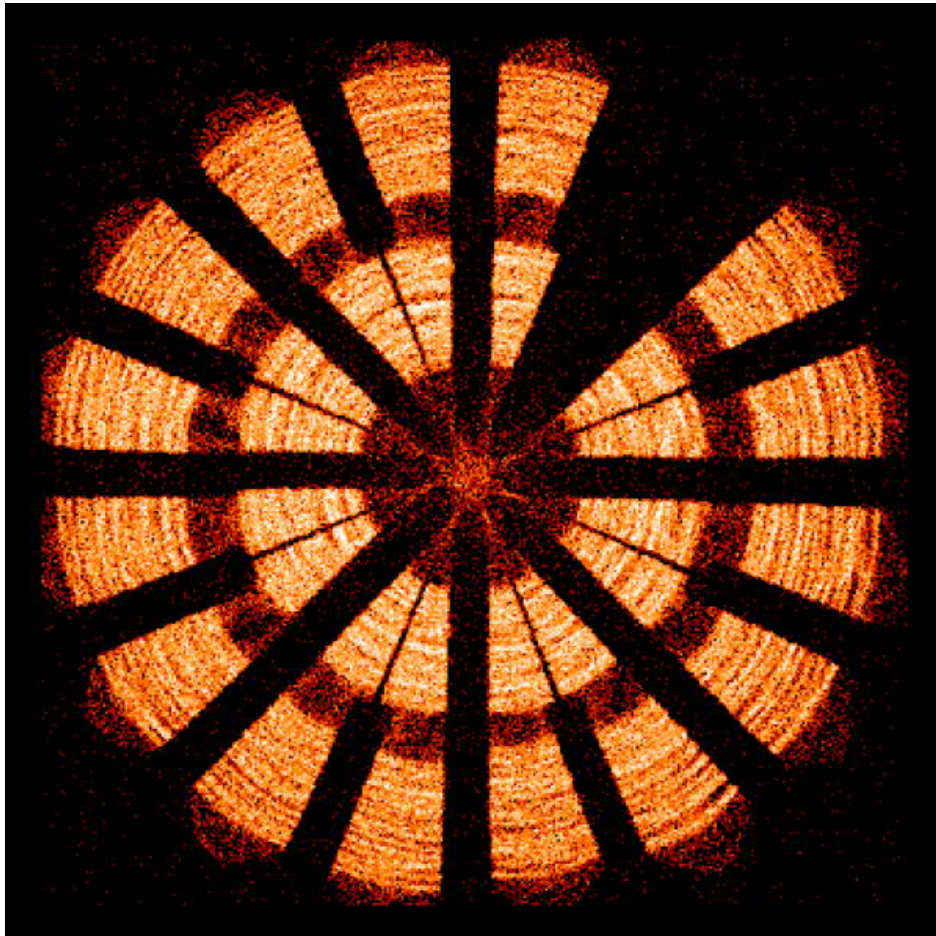
- on-axis / no shift
- FoV / no shift
- on-axis 0.4 mm shift
- FoV / 0.4 mm shift

## Calibration: Setup for Effective Area on-axis measurements

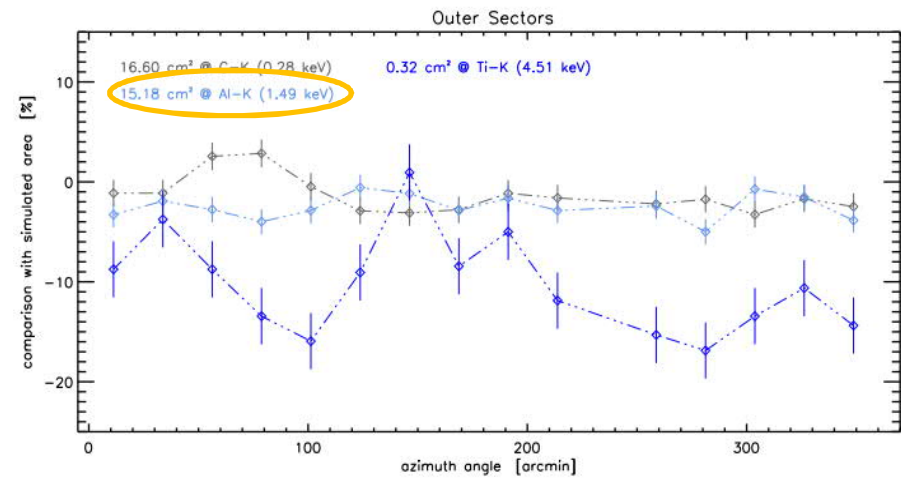
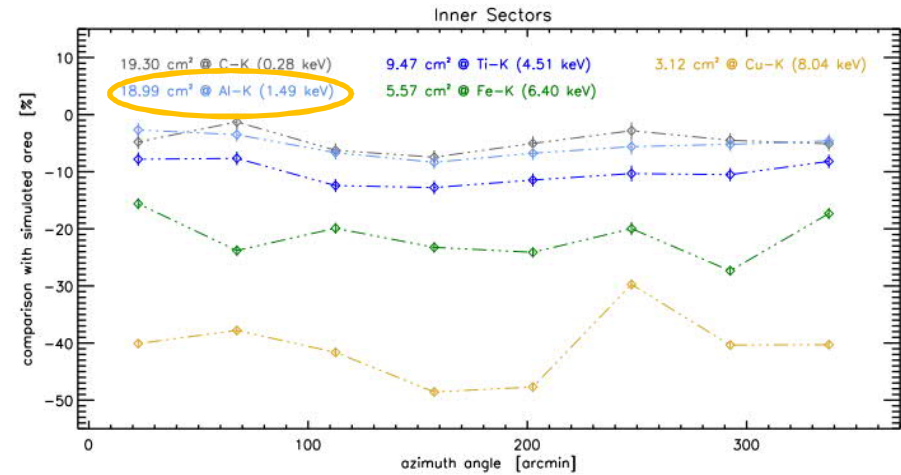


Quasi parallel beam with the “Glücksrad” configuration

# Calibration: Effective Area on-axis, results for 1.5 keV



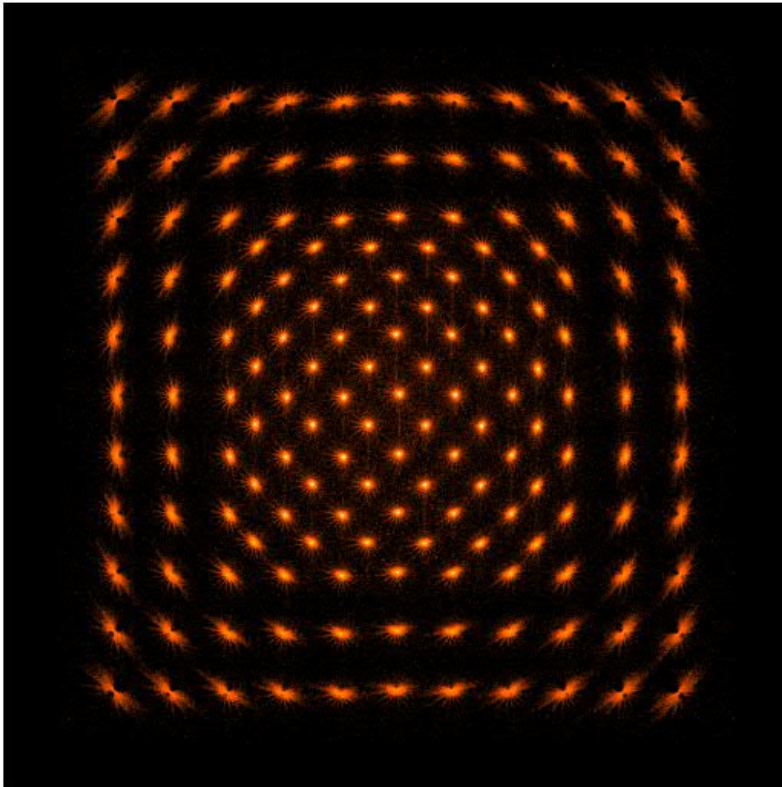
Al-K 1.49 keV



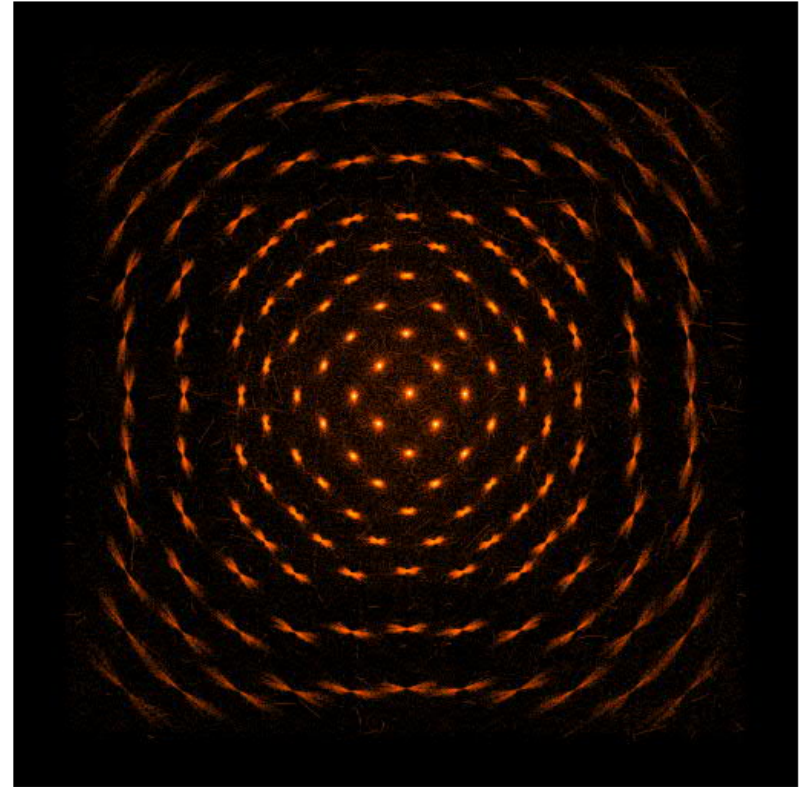
from Gisela Hartner (MPE, PANTER)

Quasi parallel beam with the “Glücksrad” configuration

Calibration: Effective Area off-axis



Al-K 1.49 keV

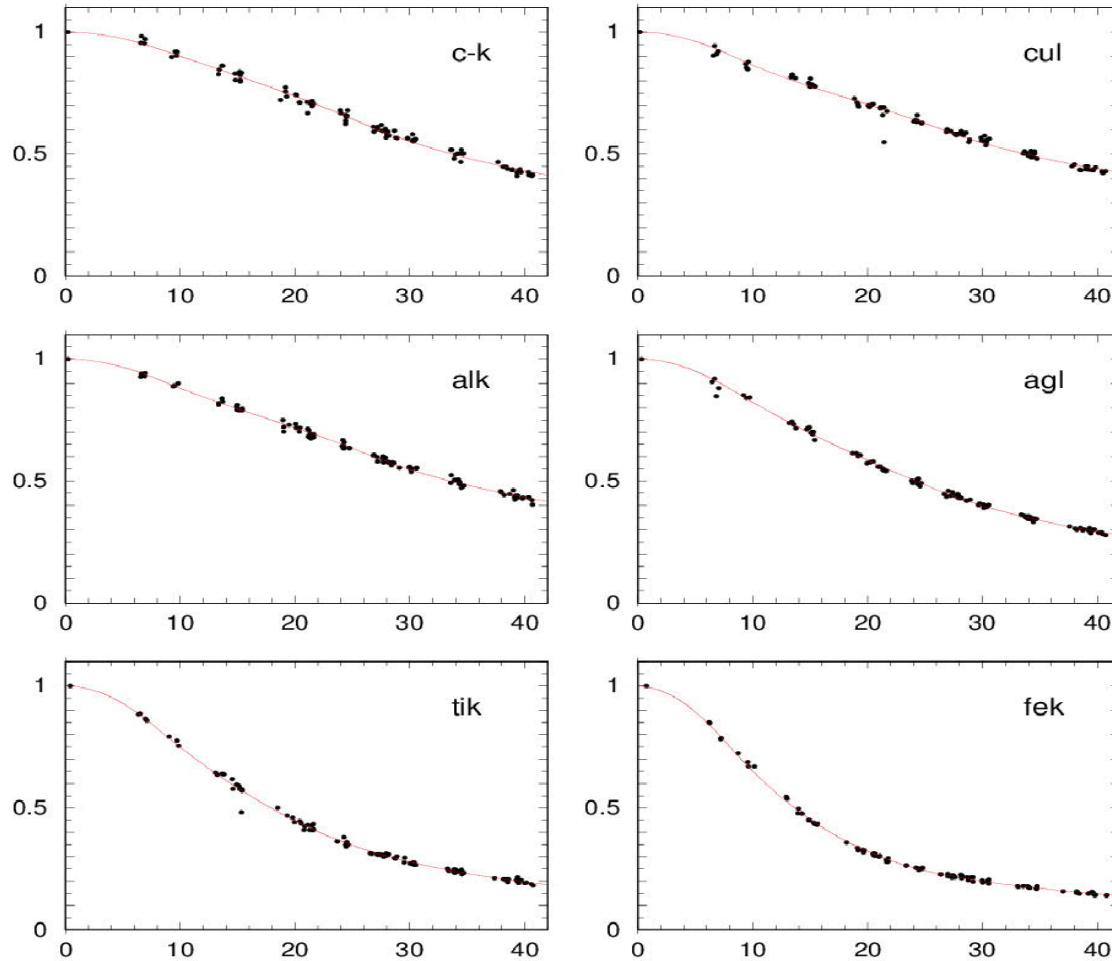


Fe-K 6.40 keV

*from Konrad Dennerl (MPE)*

Focal plane mapping for different energies

## Calibration: Effective Area off-axis

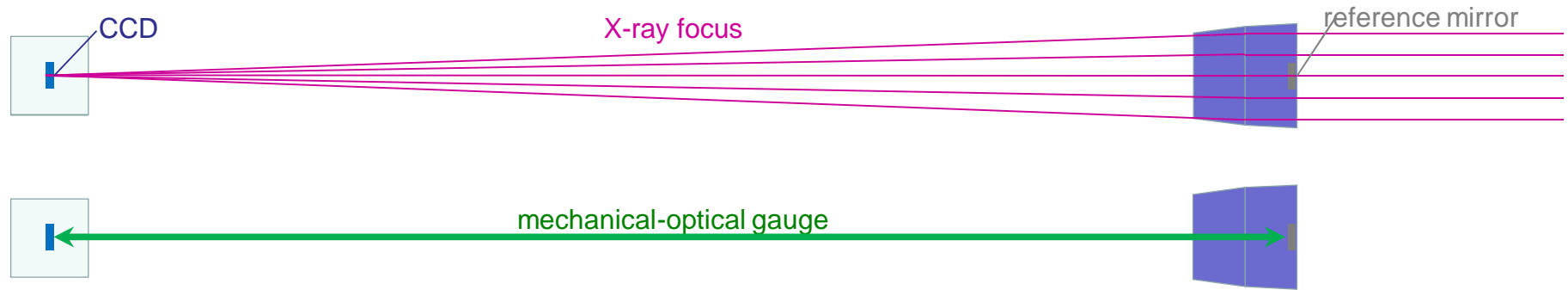


*from Konrad Dennerl (MPE)*

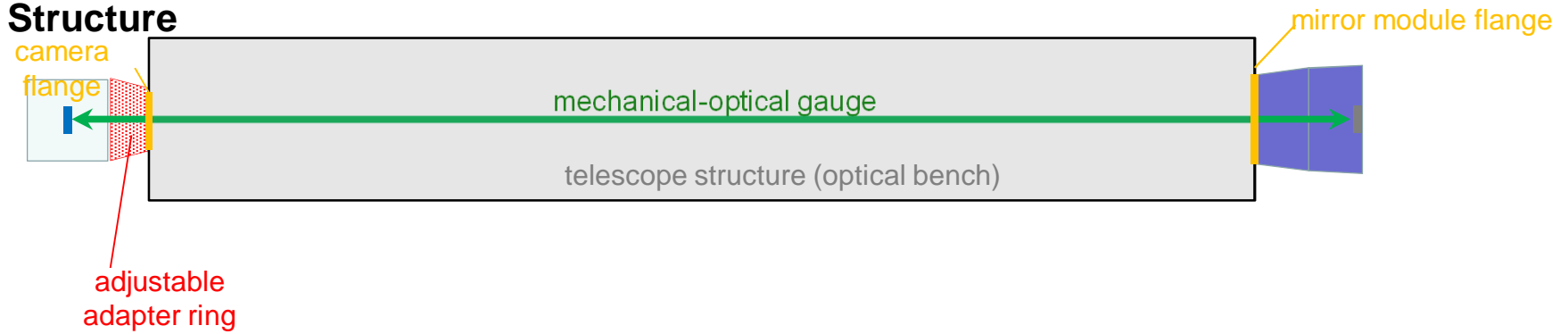
Focal plane mapping for different energies → vignetting function

# Focal Length

## (1) X-Ray Calibration



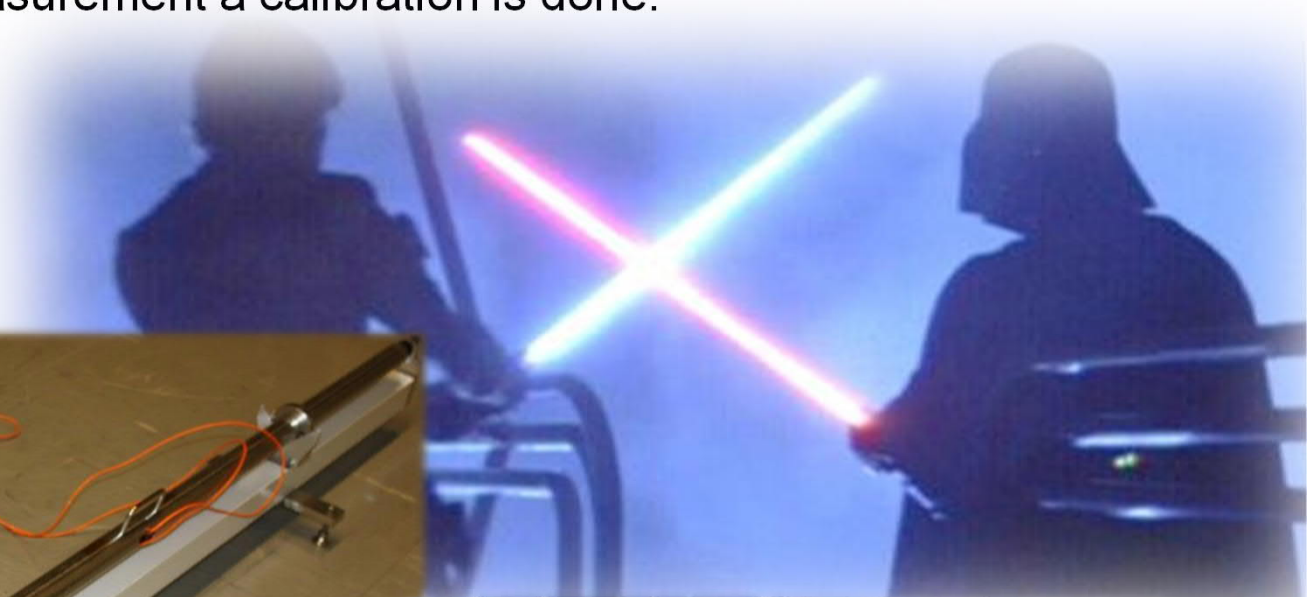
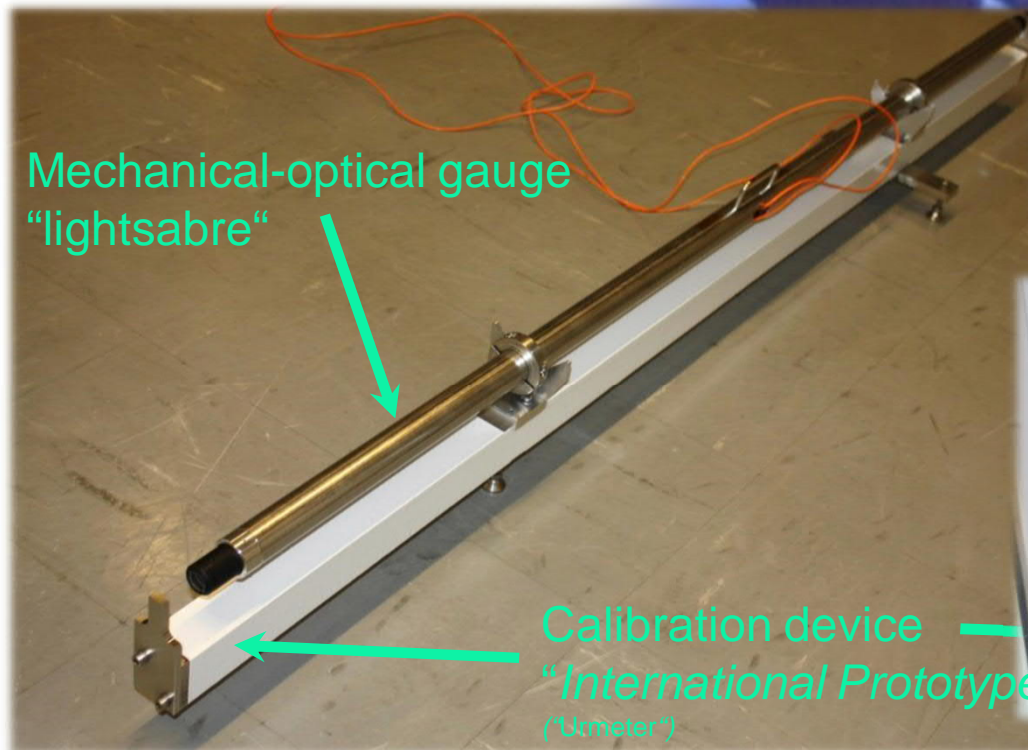
## (2) Mounting into Telescope Structure



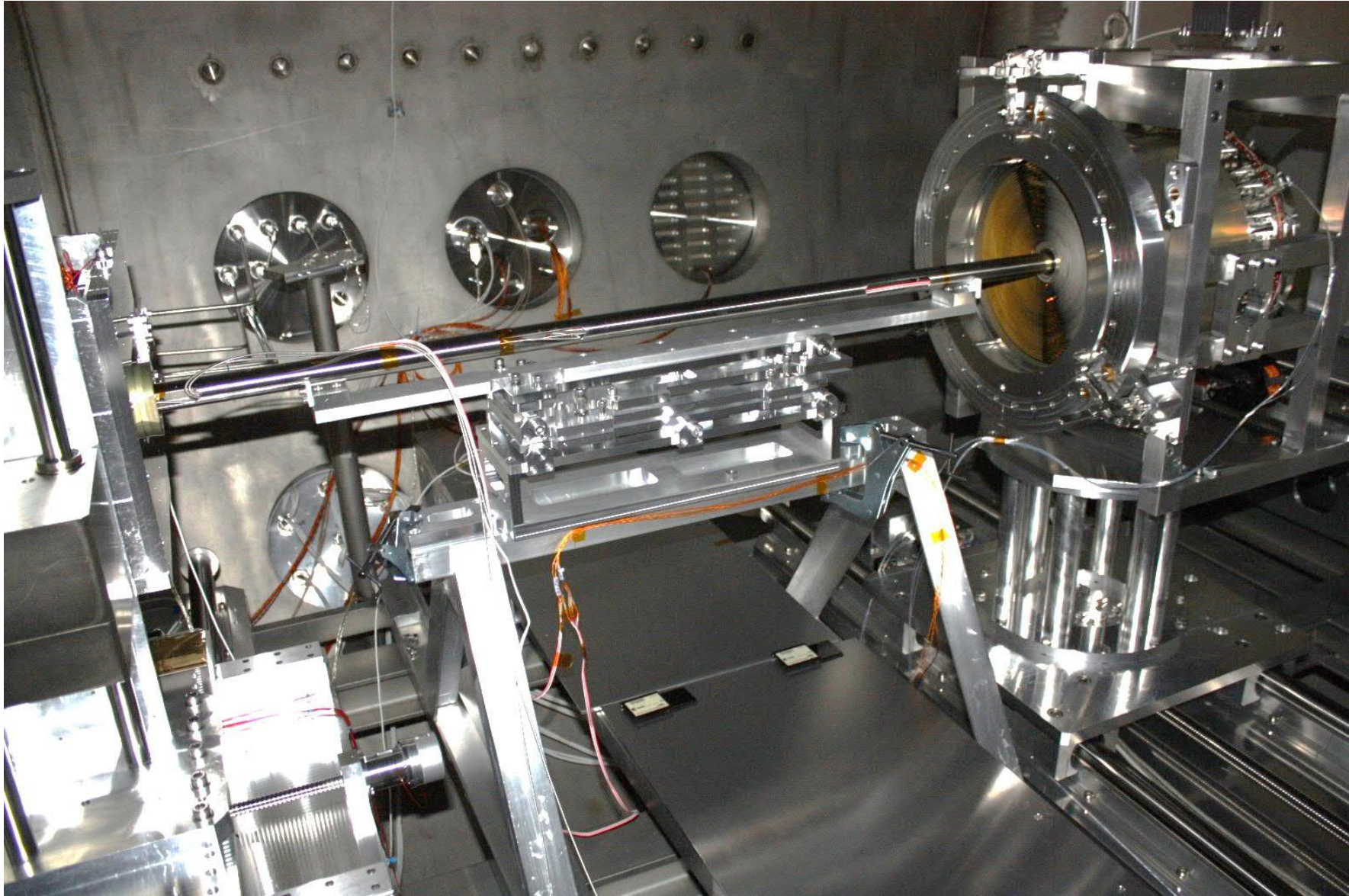


## Focal Length Gauge

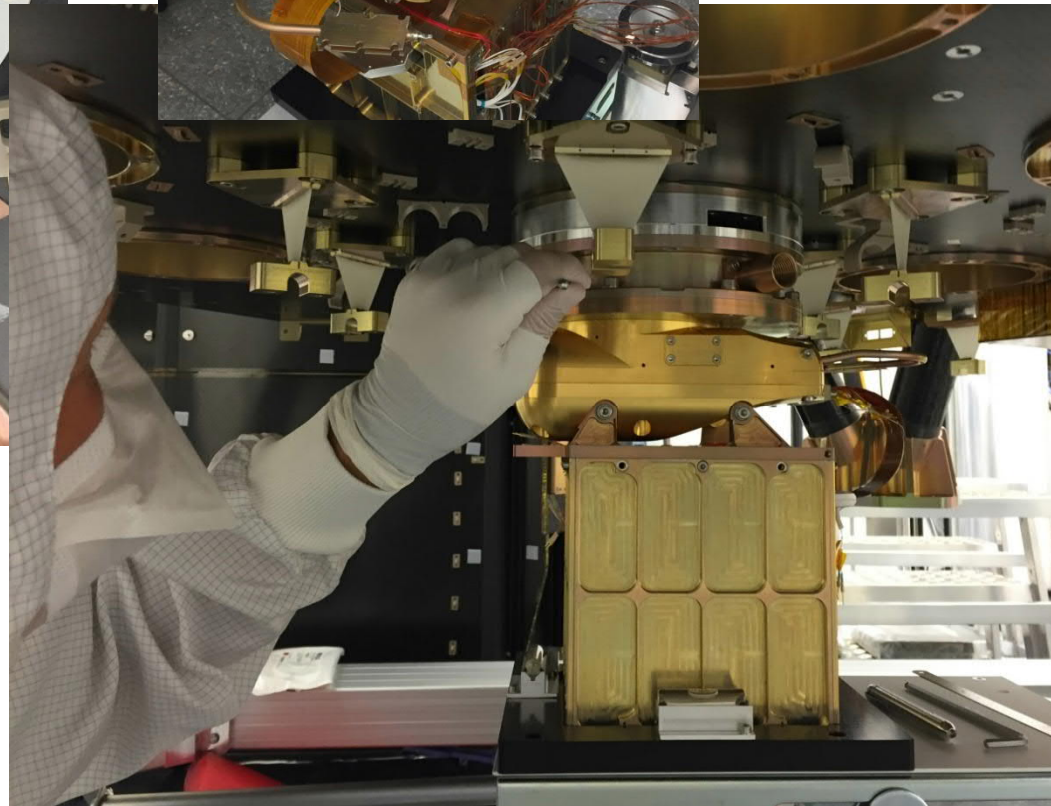
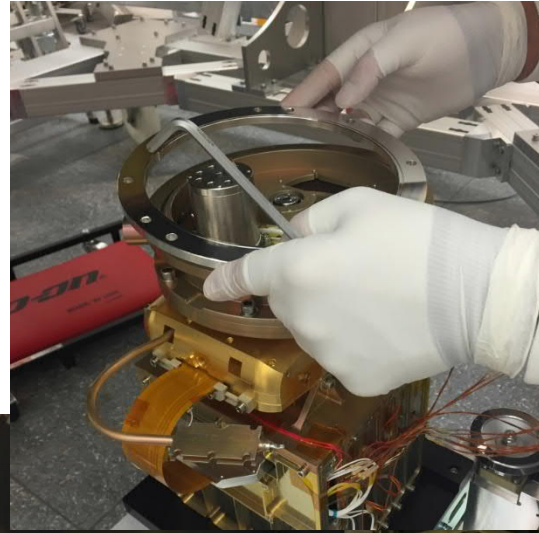
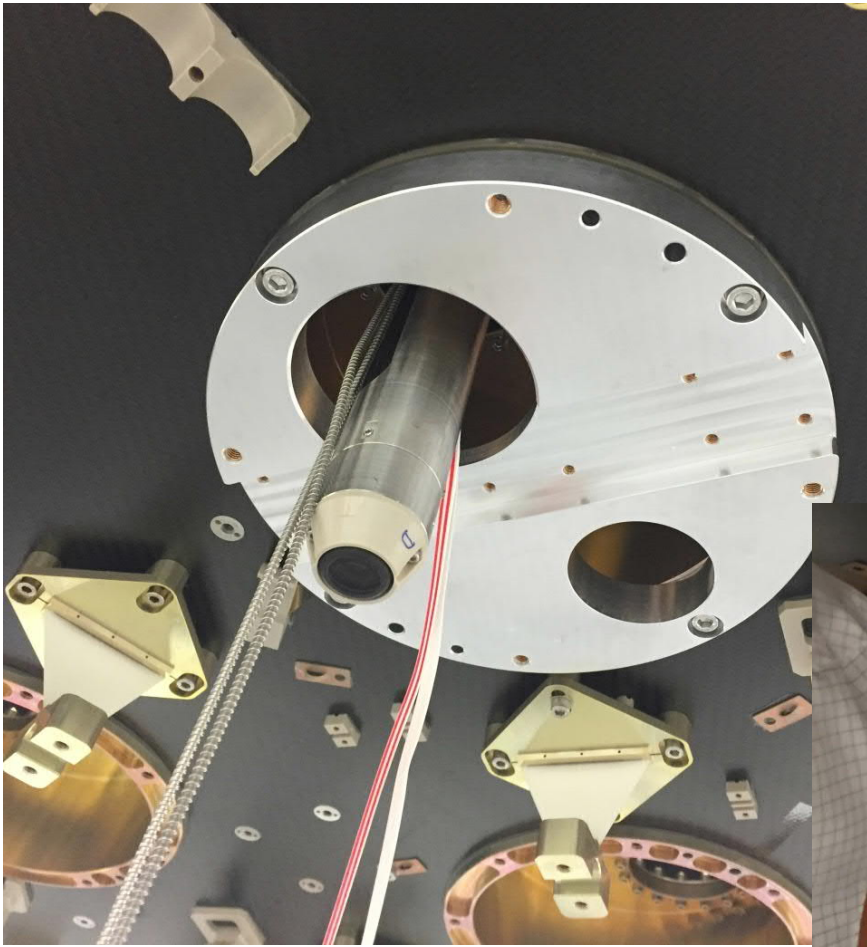
The focal length is measured with a mechanical-optical gauge giving the distance between the in-focus position of the detector and the reference mirror in the MM; before and after each measurement a calibration is done.



## New Gauge (vacuum proof)

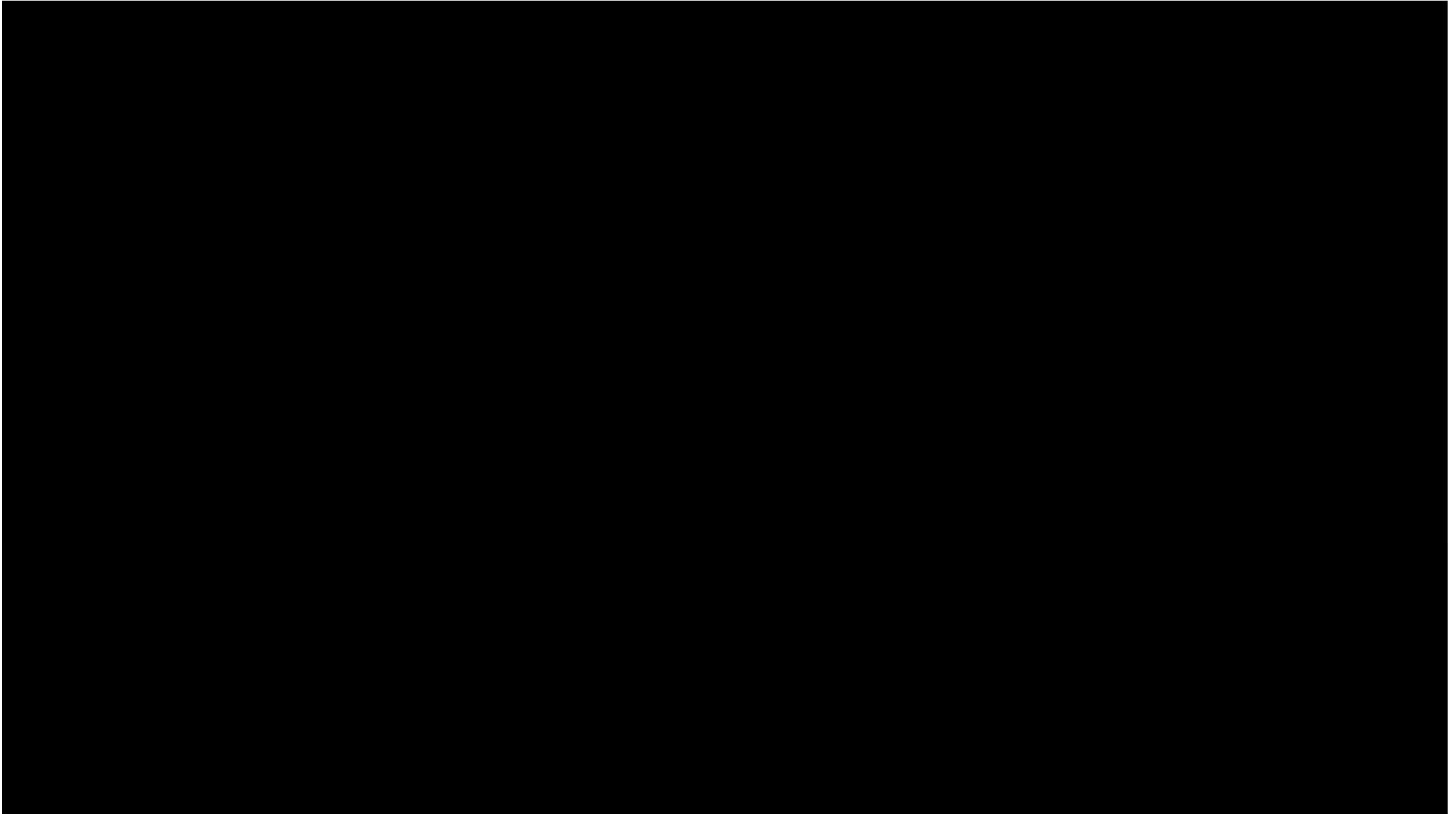


## Focal Length Adjustment in the Telescope Structure



## 4.6. Telescope assembly

Movie: Integration of the final Telescope Module



# eROSITA at NPO Lavochkin in Moscow

